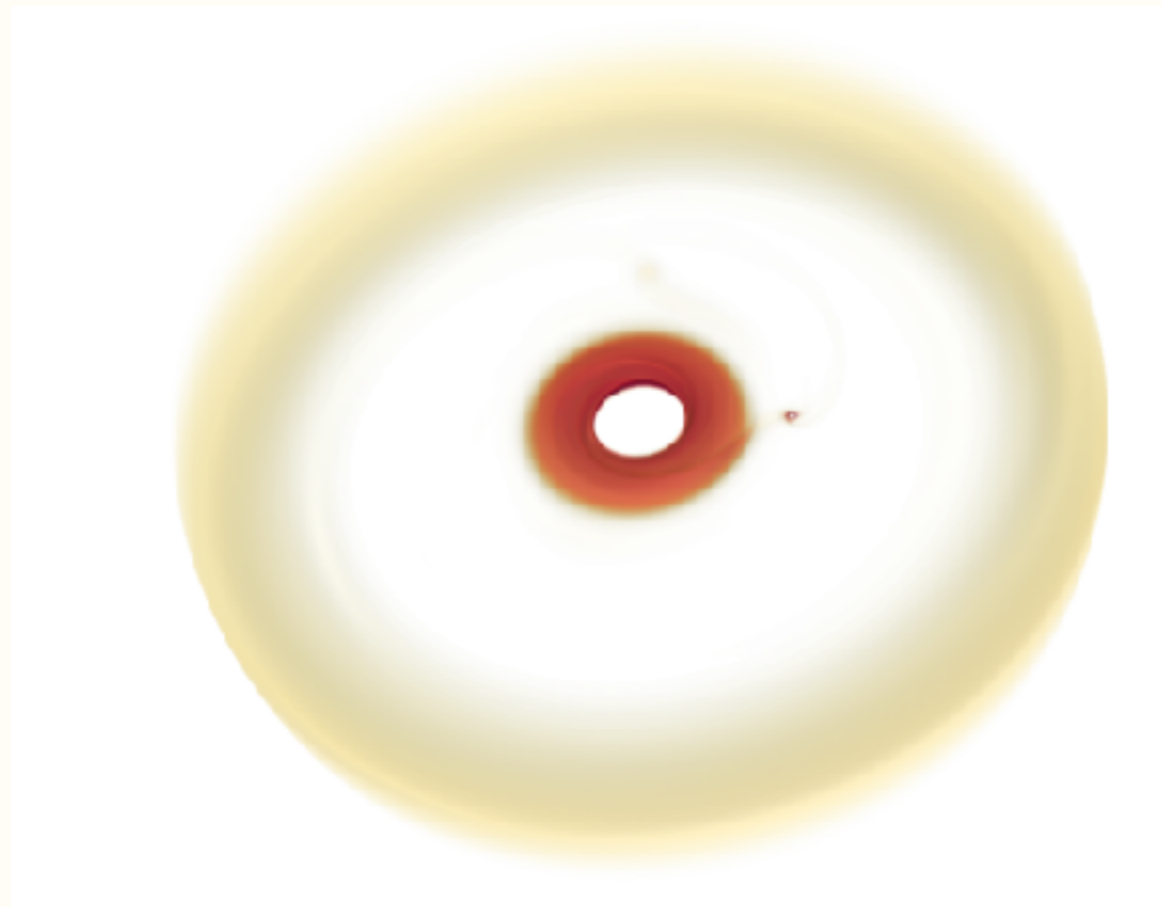


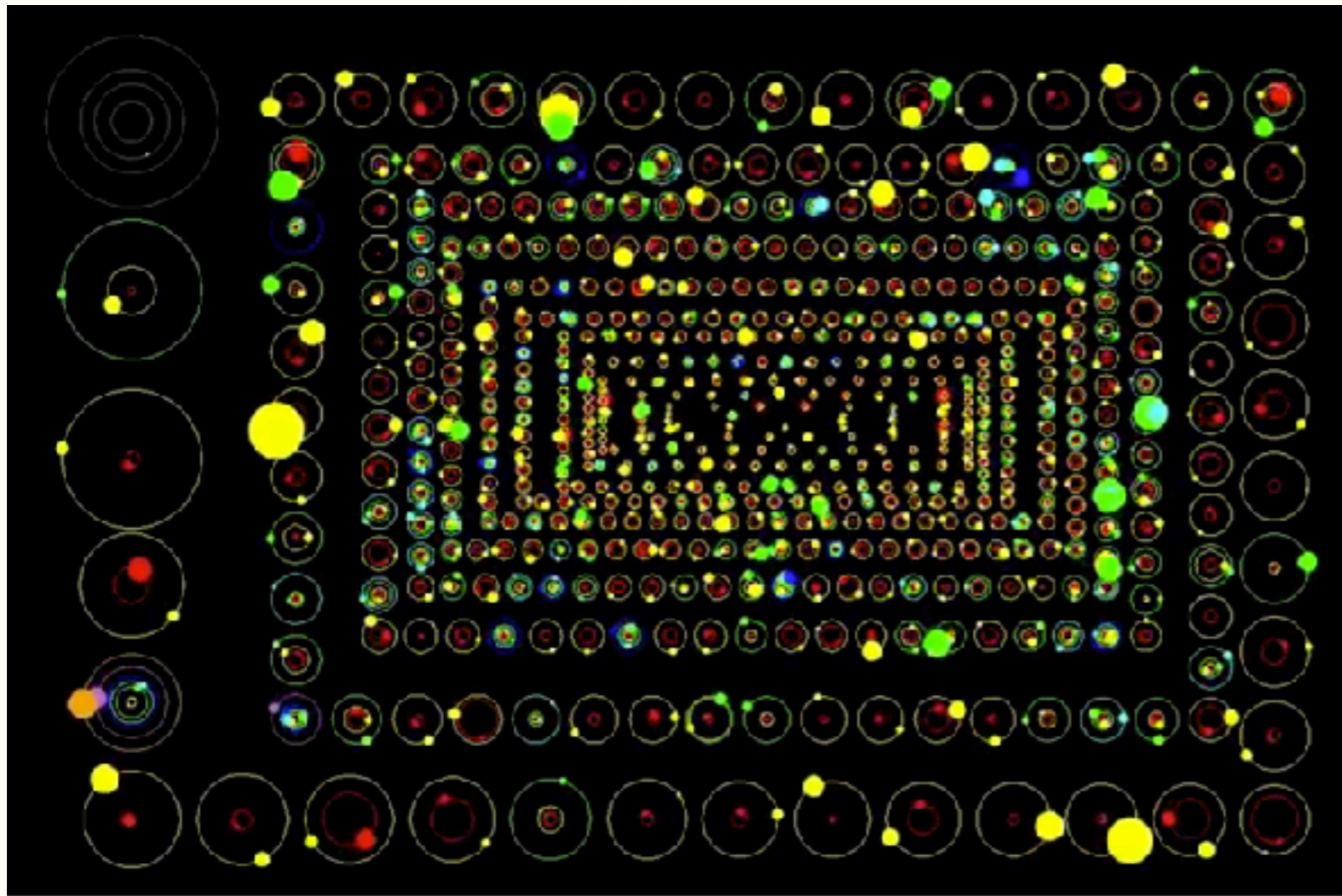
Indirect Observational Signatures of Young Planets

Myriam Benisty (U. Grenoble & U. Chile)

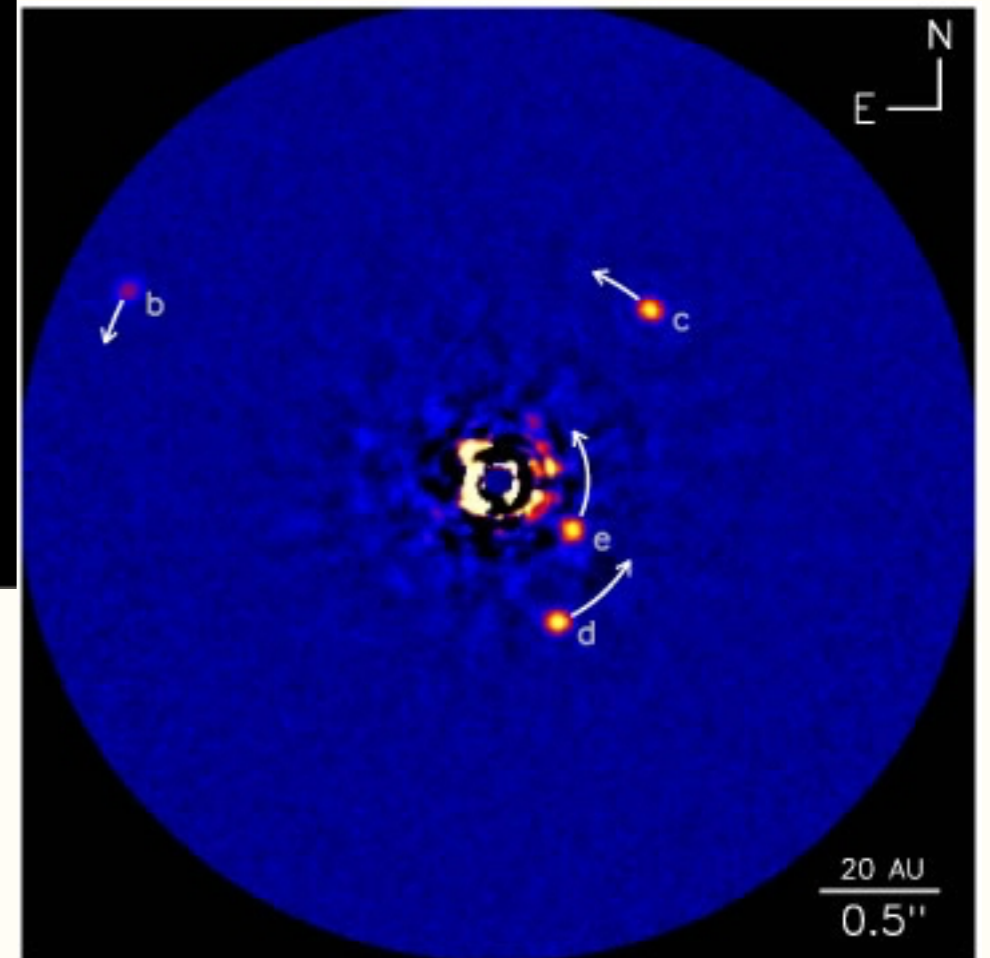
Zhaohuan Zhu (U. of Nevada, Las Vegas)



Exoplanets are **common** and **diverse**

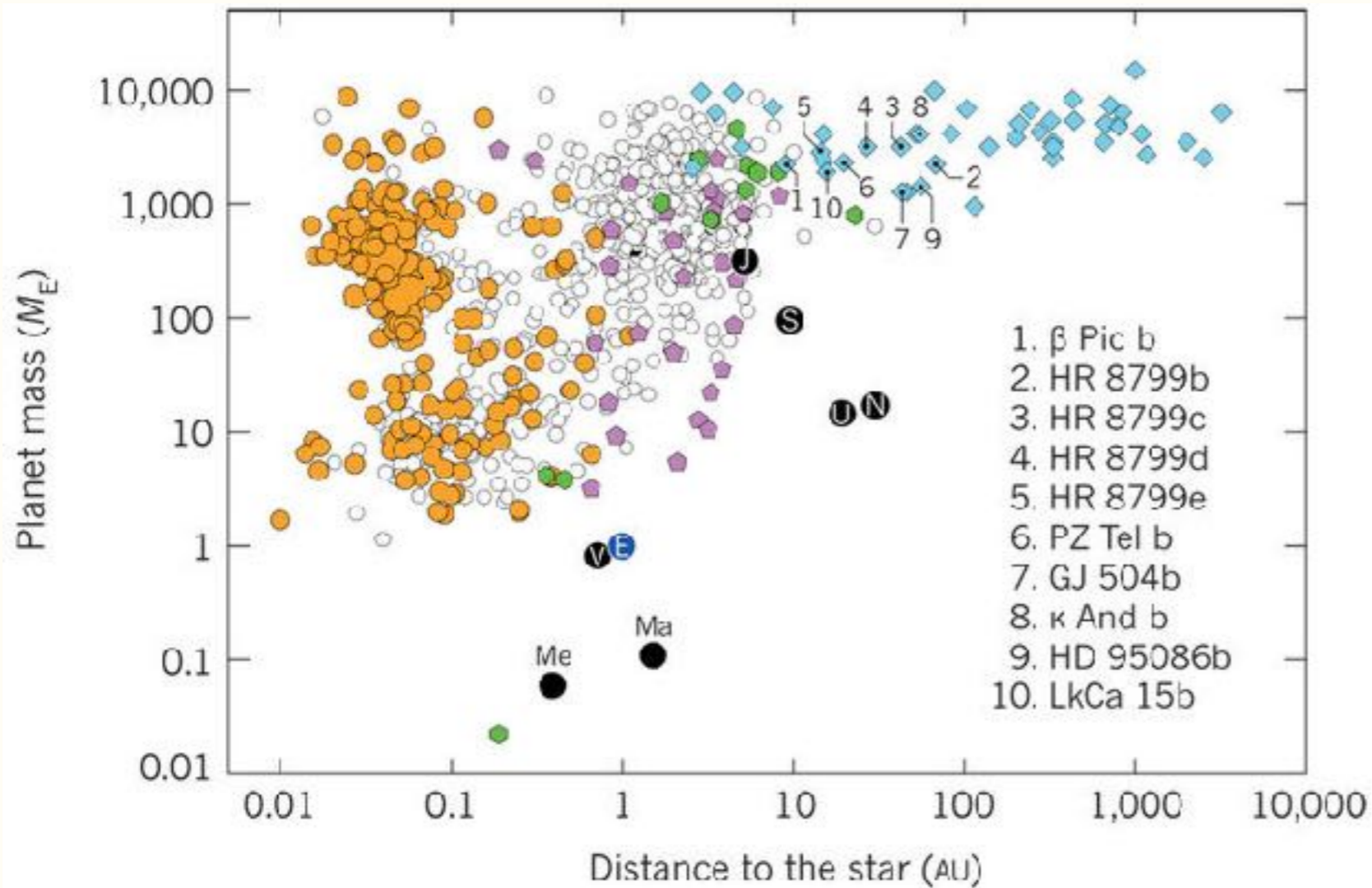


Kepler Orrery III by Daniel Fabrycky

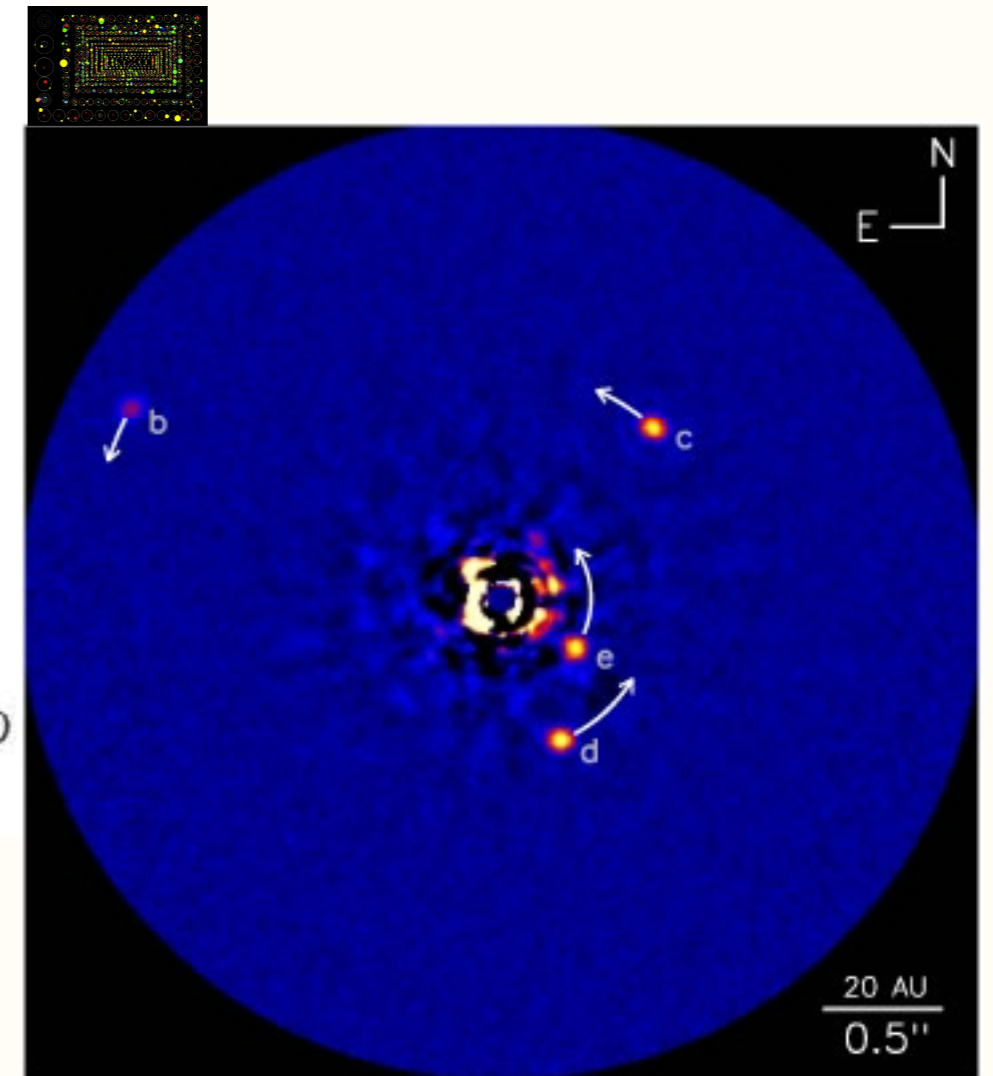


Credit: NRC/HIA, C. Marois, and Keck Observatory

Exoplanets are common and diverse



Pepe+ 2014

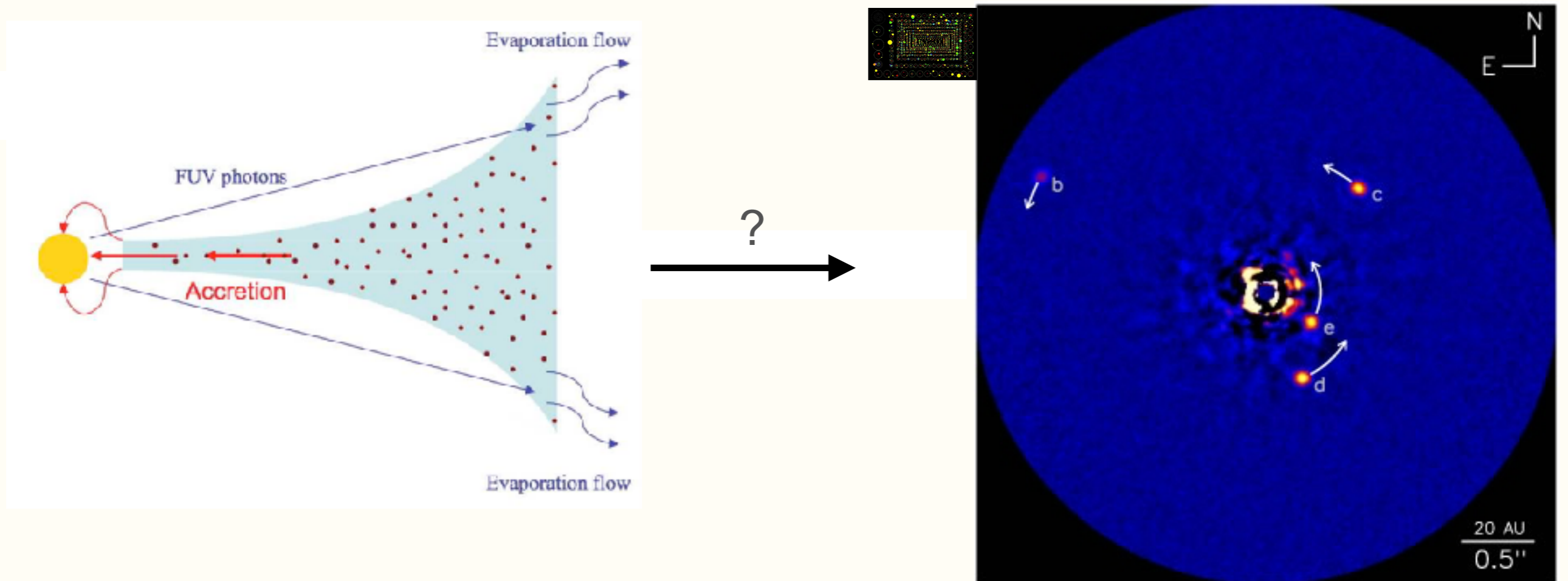


Credit: NRC/HIA, C. Marois, and Keck Observatory

Disk evolution and planet formation

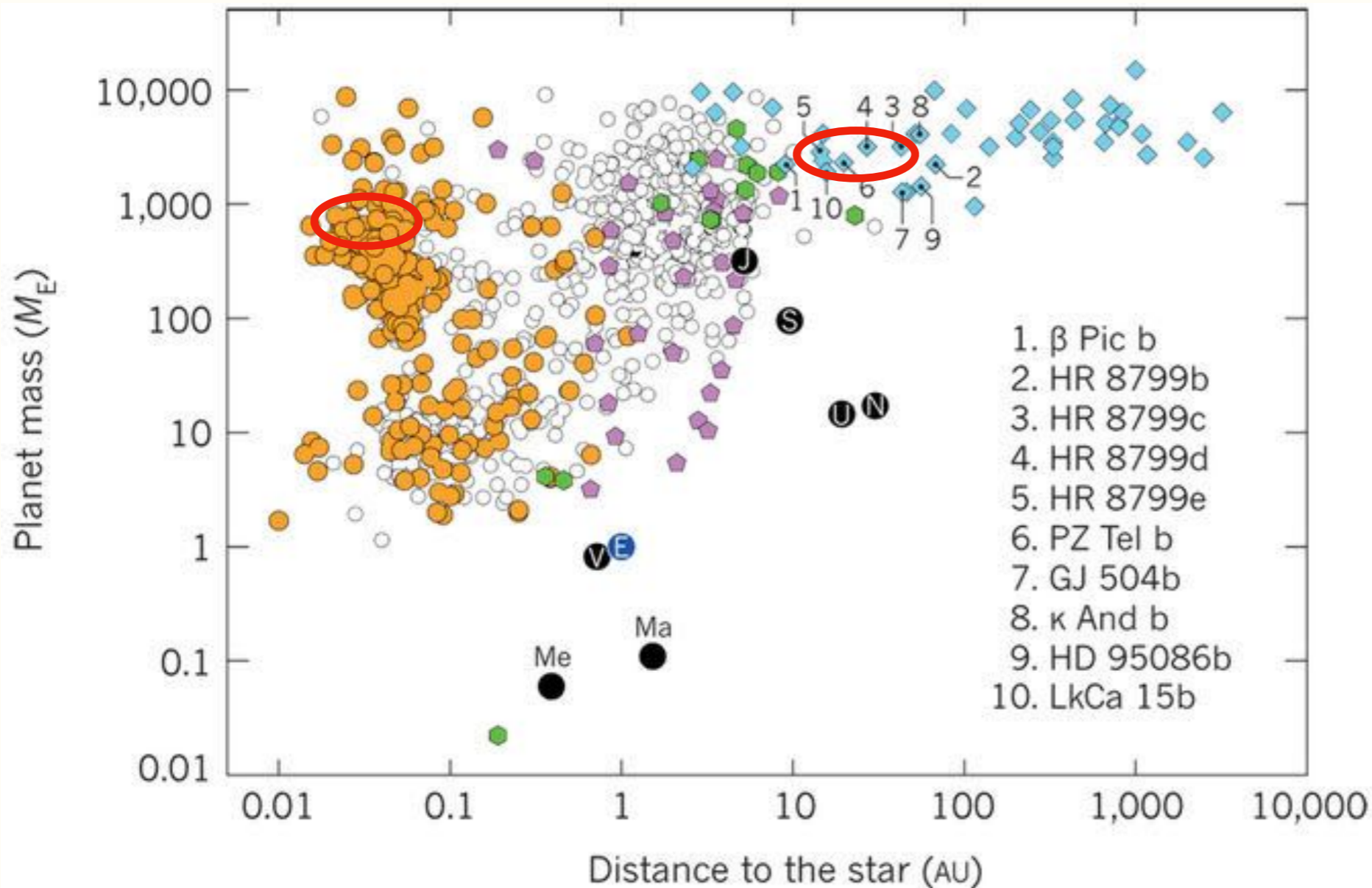
How do protoplanetary disks evolve to such diverse exoplanets?

- Look for disk structural change
- Look for signposts of planets



Credit: NRC/HIA, C. Marois, and Keck Observatory

Disk evolution and planet formation



Pepe+ 2014

Where are young planets on this plot?

Outline

- Disk Observations:

Optical/Near-IR:

Rings, Spirals, Disk shadowing

Submm:

Diverse features

Synergy between Near-IR and Submm

- Planet-disk interaction theory:

Gaps/rings

Spirals

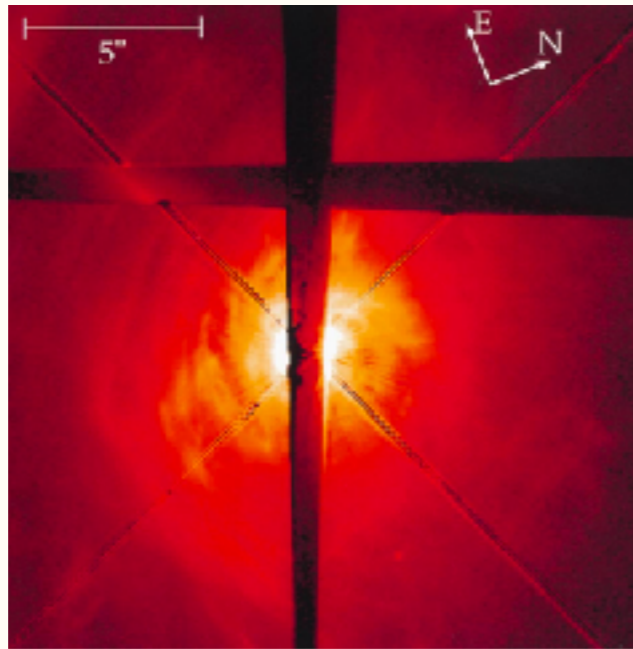
Lopsided structures

Shadows

CPDs

Optical/Near-IR: scattered and polarized light

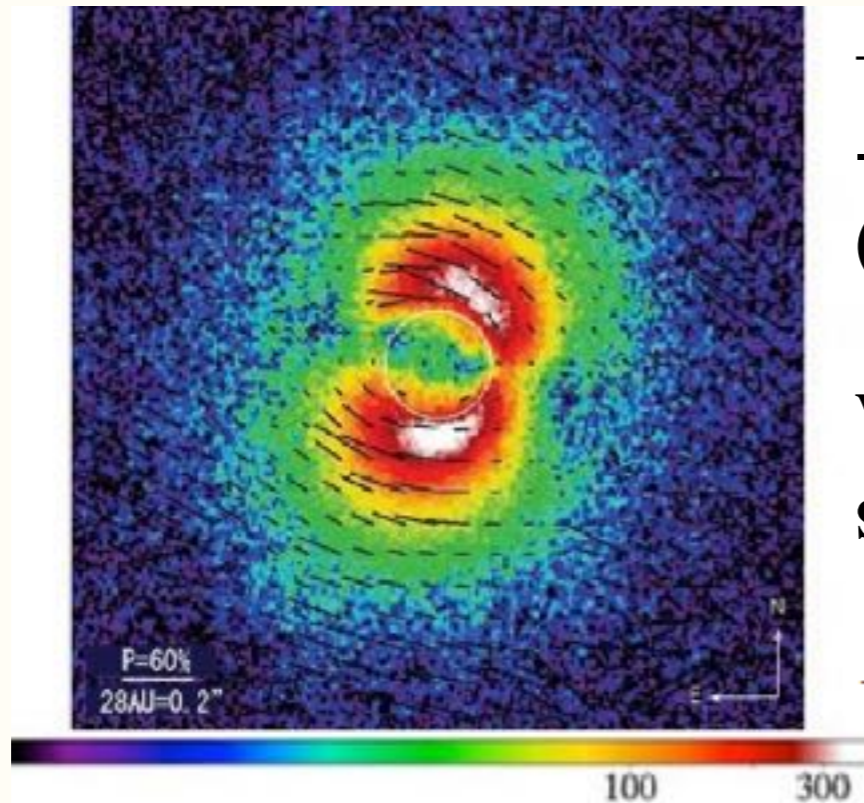
Full Intensity:



- + Full intensity
- But need a coronagraph
- the PSF halo of the star is hard to remove

AB Aur (Hubble)
Grady et al. 1999

Polarized light:



- + less contamination from the star
- Polarized light depends on lots of things (e.g. the scattering angle, inclination)

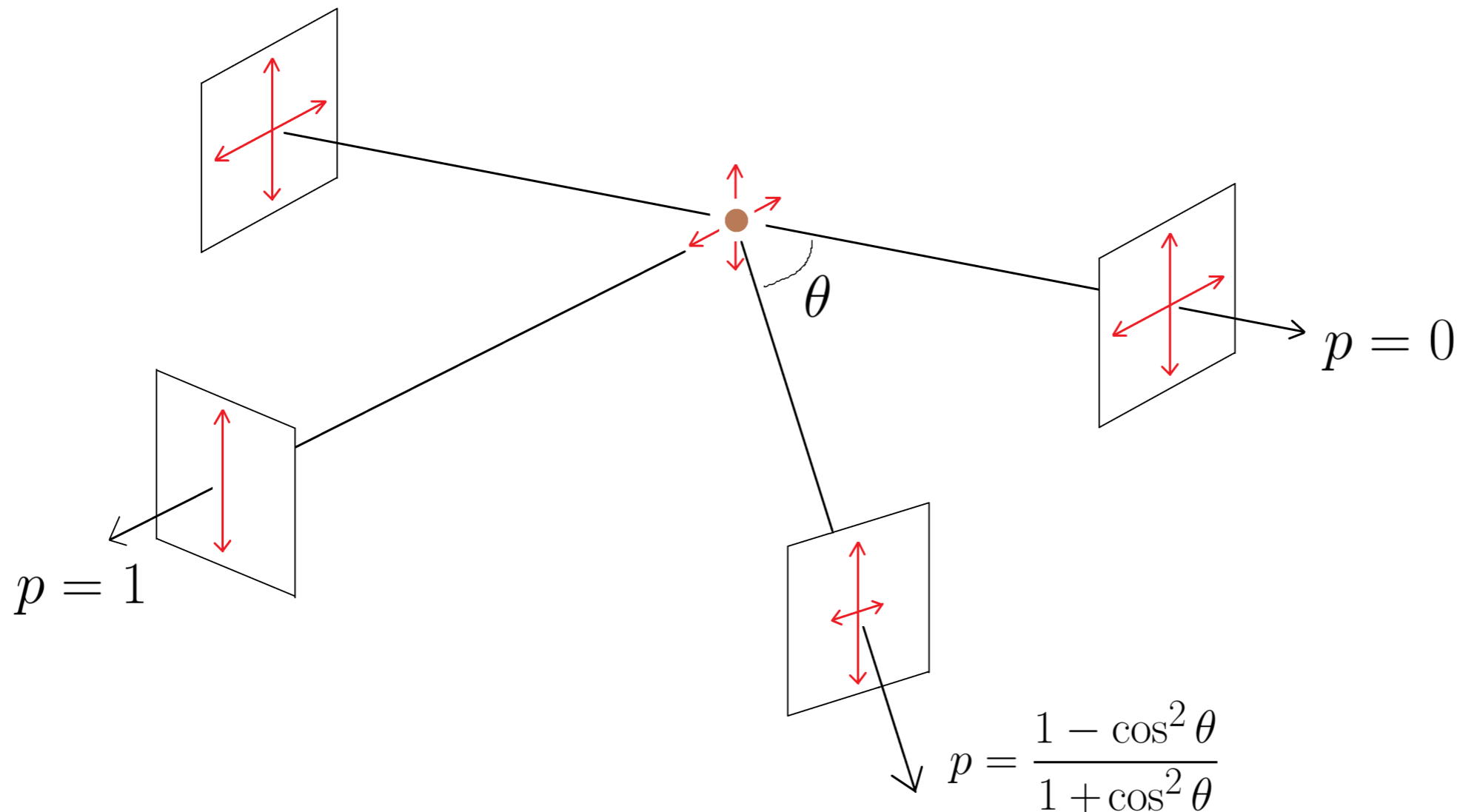
What we see is not what we think we are seeing!

$$PI = \sqrt{Q^2 + U^2}$$

UX Tau A (SEEDS)
Tanii et al. 2012

Polarization due to scattering

Scattering-induced polarization: simple illustration with oscillating dipoles



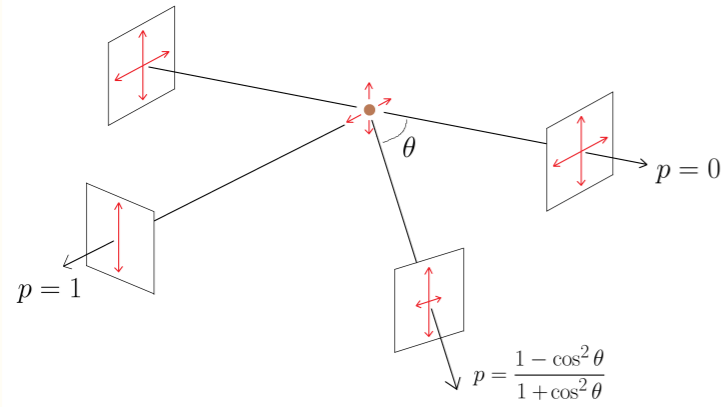
No light with E field along direction of propagation (transverse wave)

Maximum (full) polarization for 90° scattering

Polarization (E field) perpendicular to scattering plane (incident + scattered light)

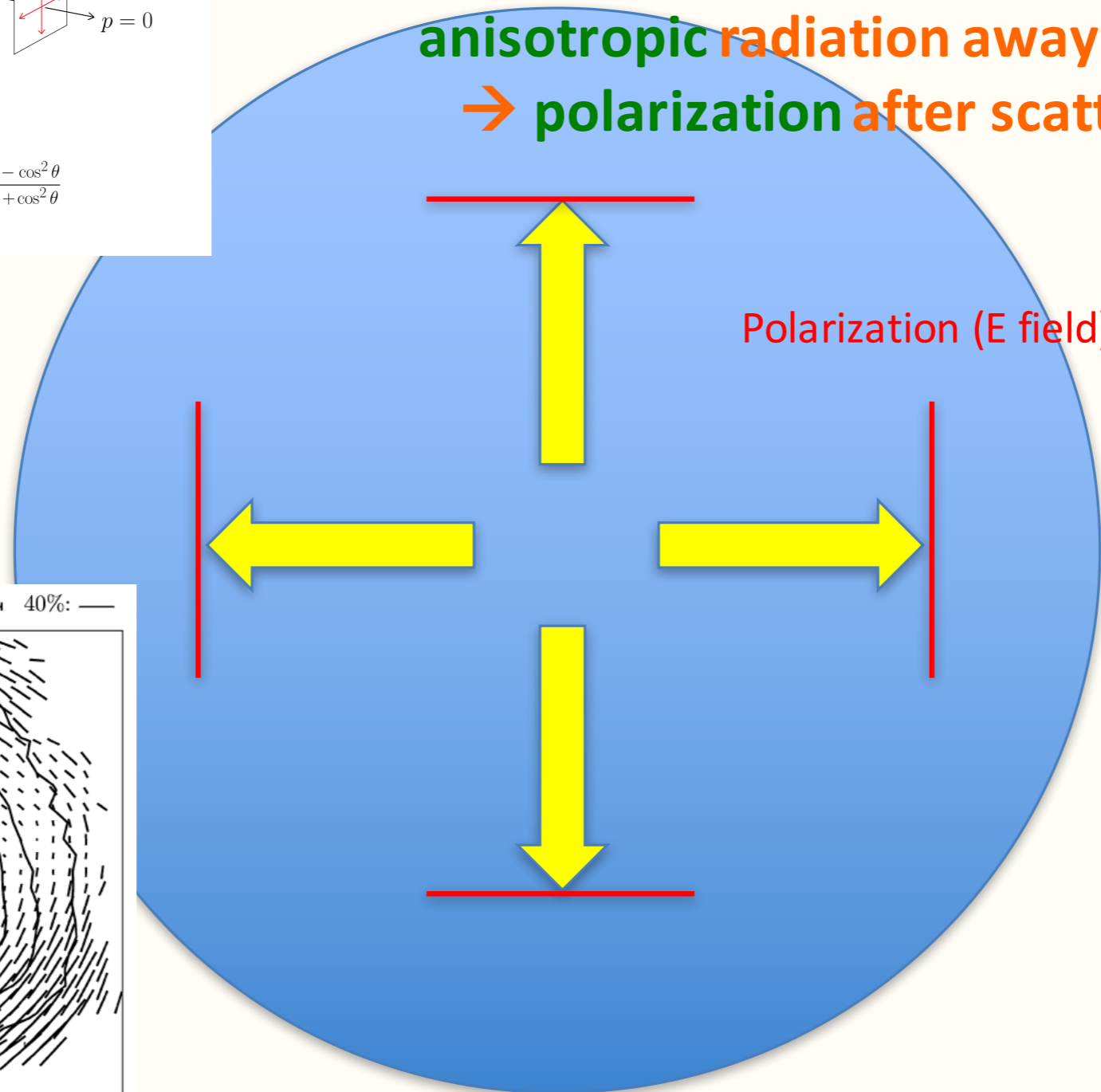
image: Zhi-Yun Li

Polarization due to scattering



Simplest case: face-on disk

anisotropic radiation away from center
→ polarization after scattering



(a) Subaru - K band

1": 40%:

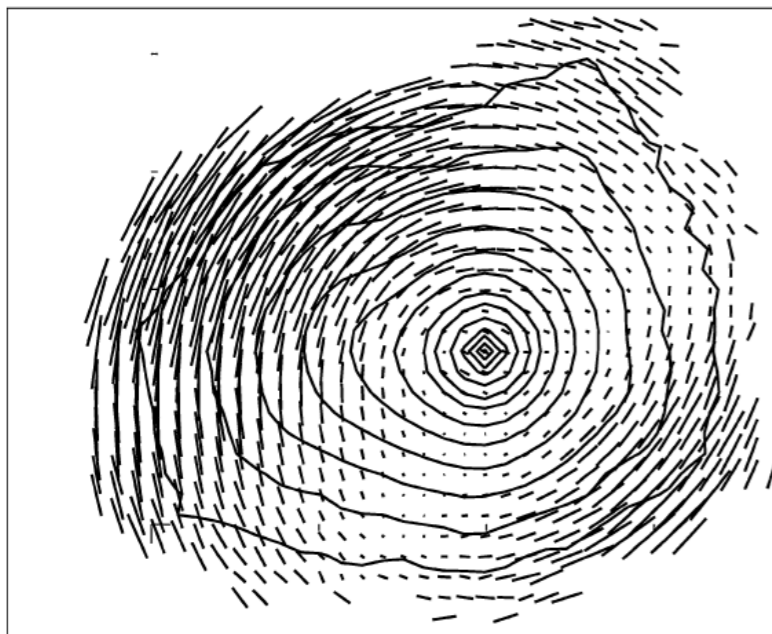
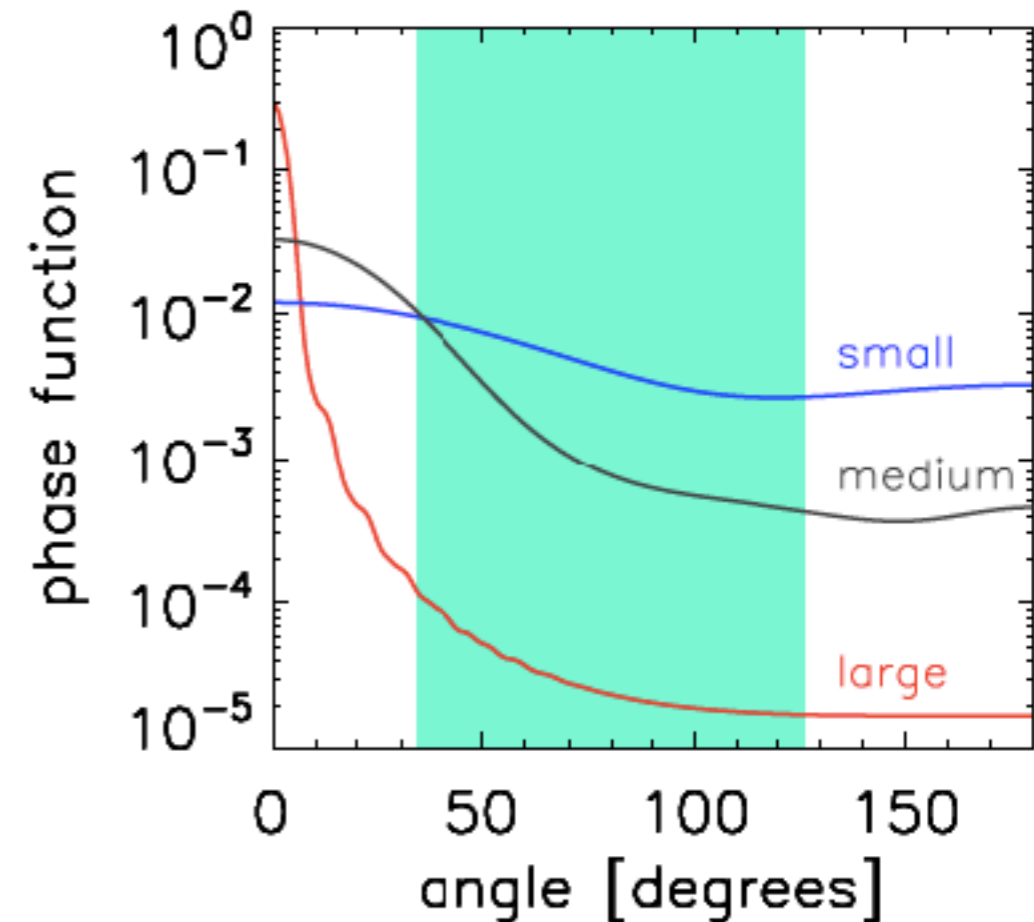
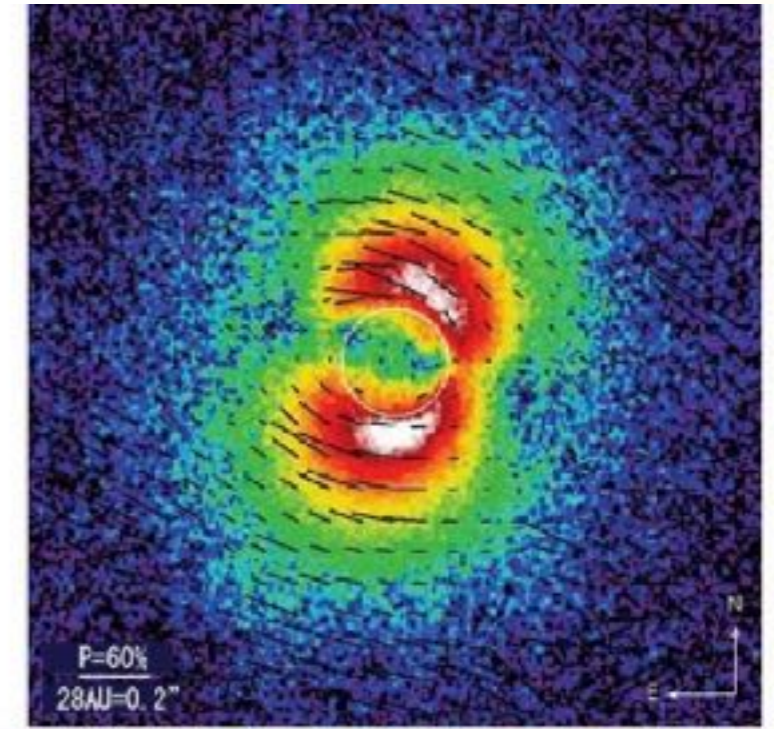
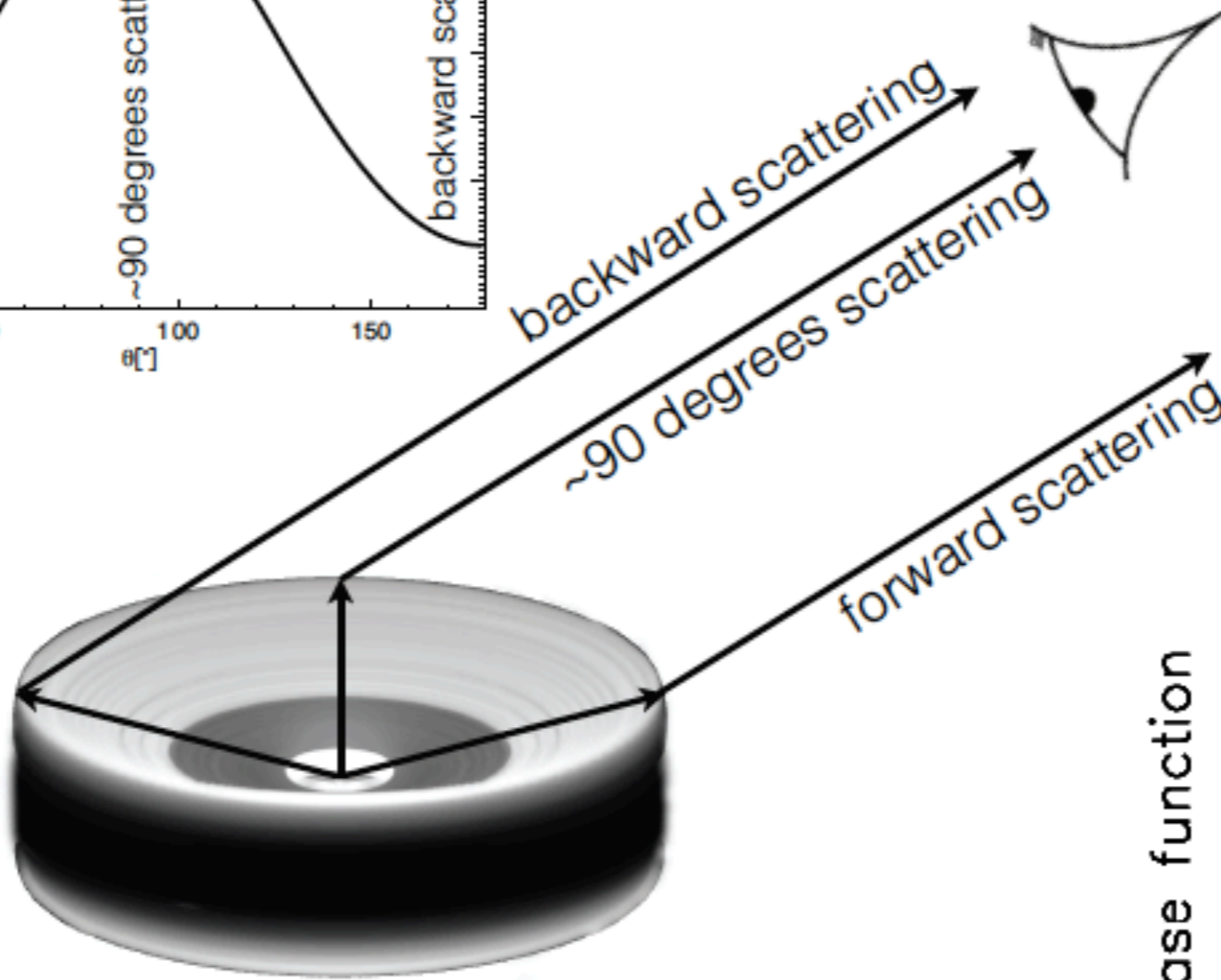
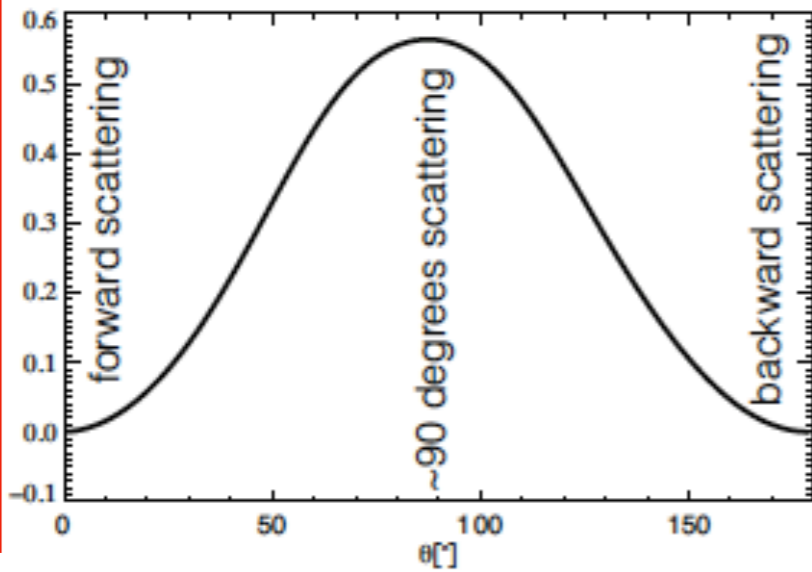


image: Zhi-Yun Li

→ Azimuthal polarization pattern

Polarization due to scattering: Inclination

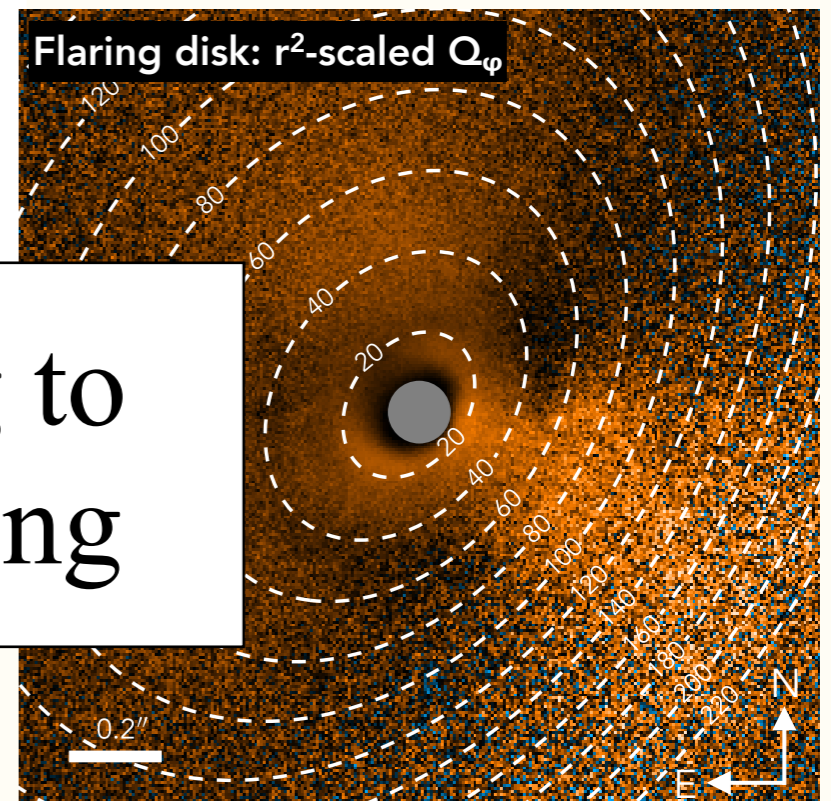
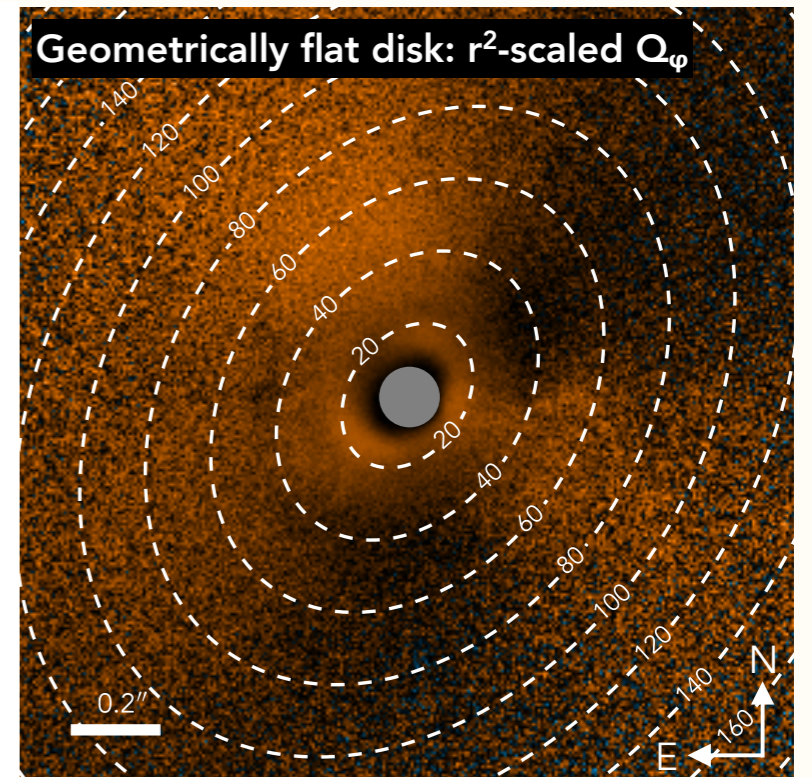
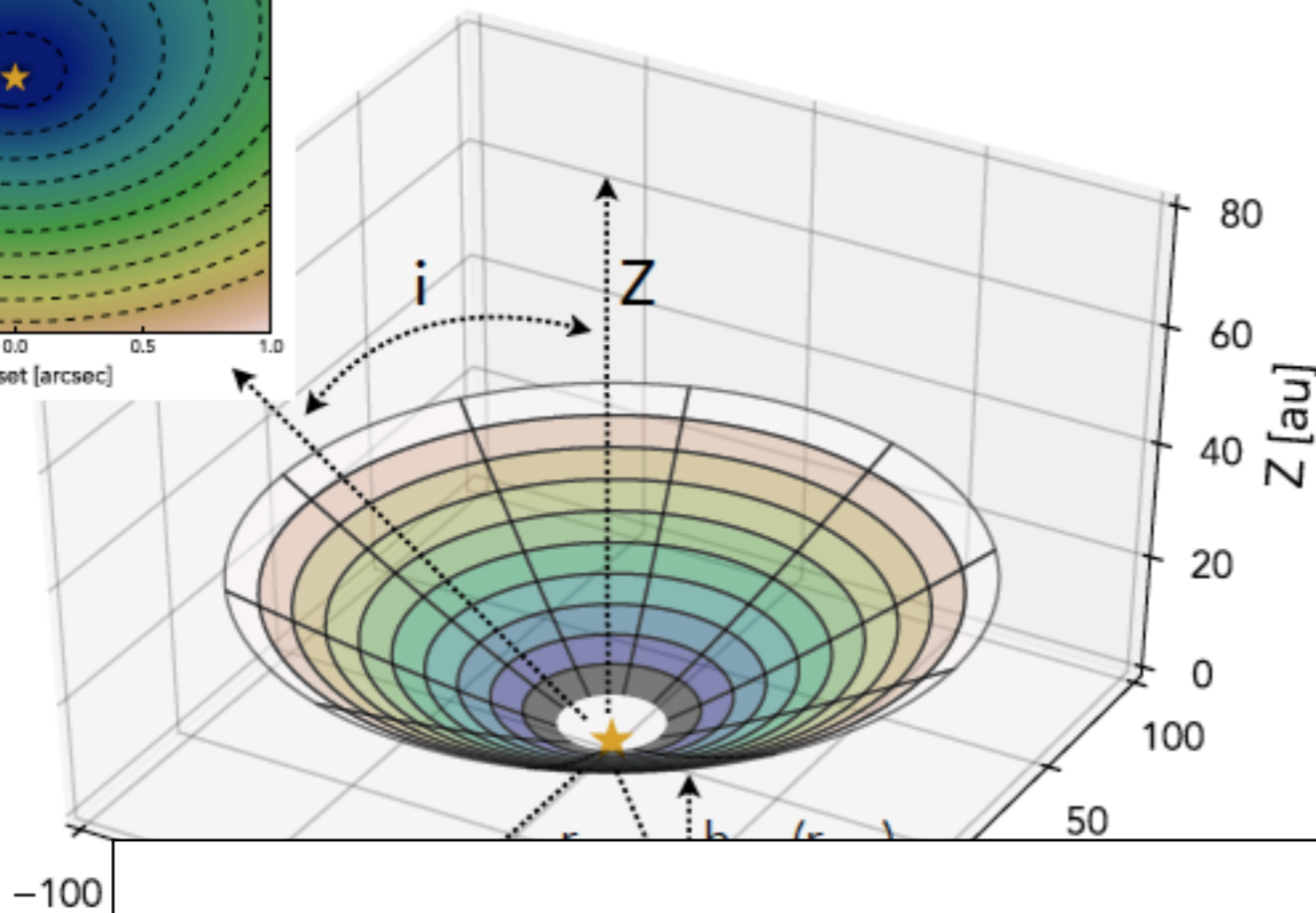
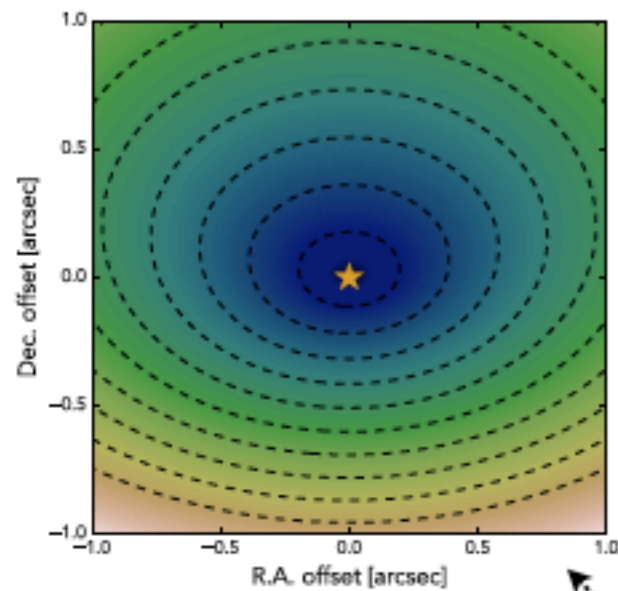
degree of polarization



Min et al. 2015

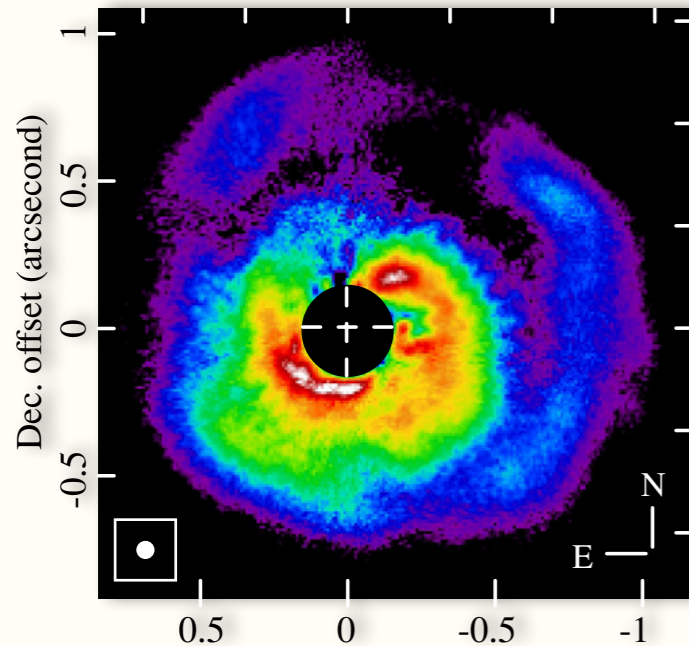
... depends on grain size, composition, porosity...

Polarization due to scattering: Projection



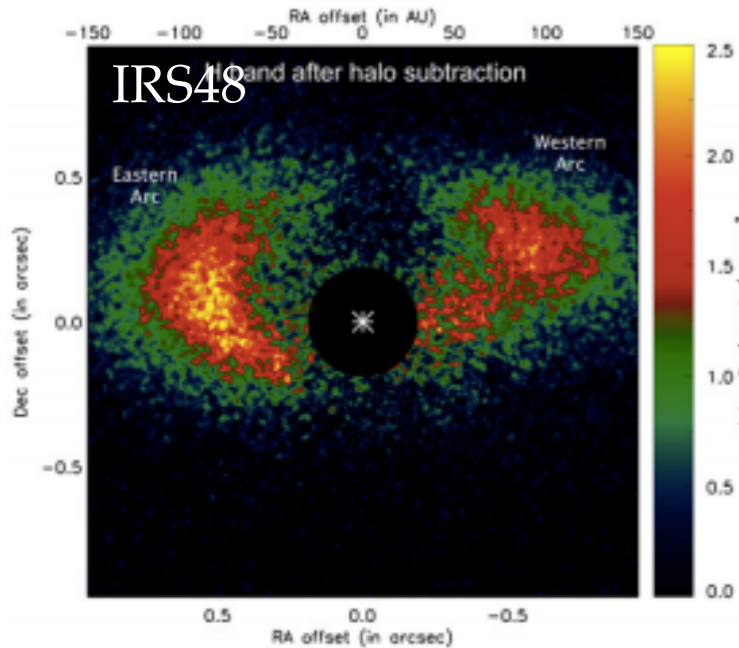
Need careful modeling to know what we are seeing

First PDI surveys

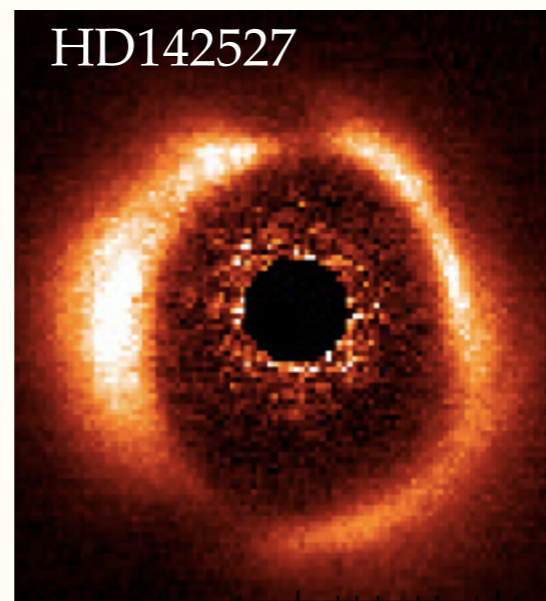


Hashimoto et al. 2011

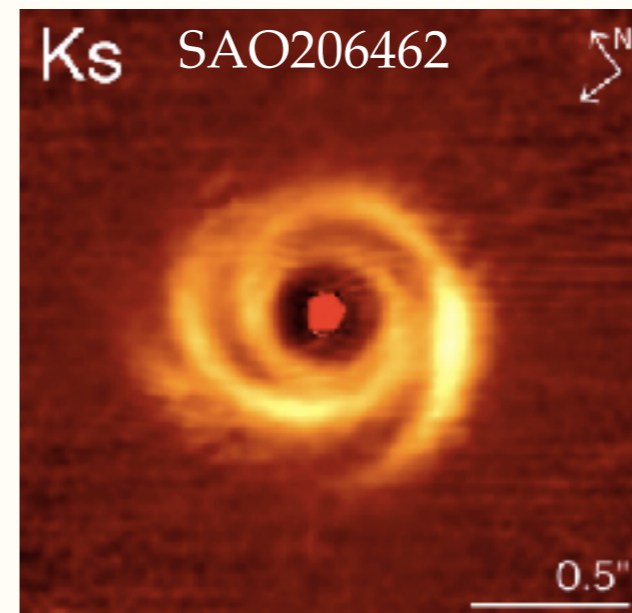
Observations of Herbig AeBe and TD with Naco/VLT and HiCIAO/Subaru at high resolution have shown more complex features.



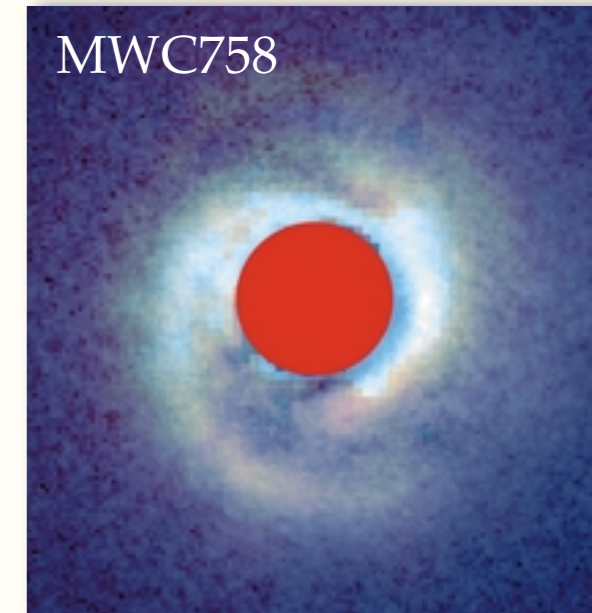
Folette et al. 2015



Canovas et al 2013



Garufi et al 2013



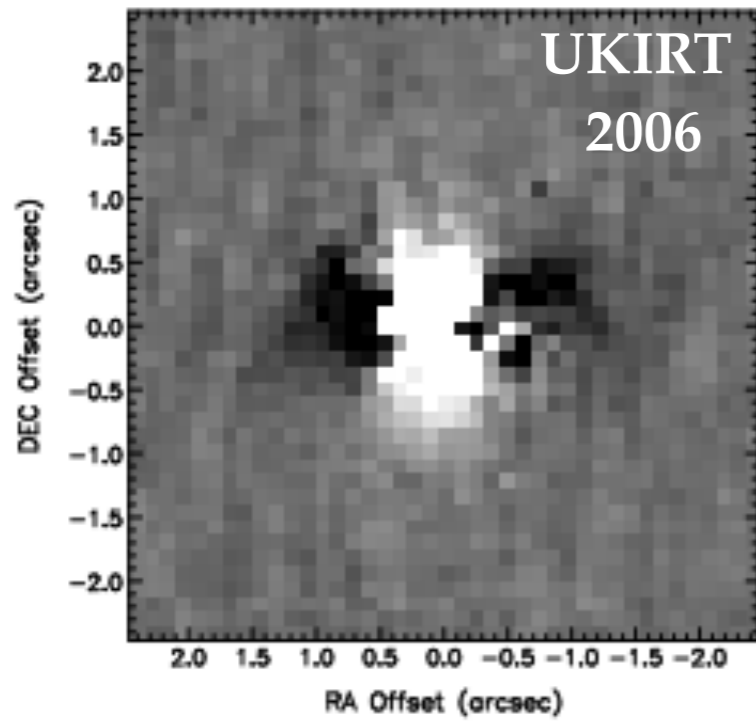
Grady et al 2013

Also Fukagawa et al. 2006; Hashimoto et al. 2011; Quanz et al. 2011,2012; Muto et al. 2012; Kusakabe et al 2012; Folette et al. 2013; Avenhaus et al. 2014; Garufi et al. 2014, and more.

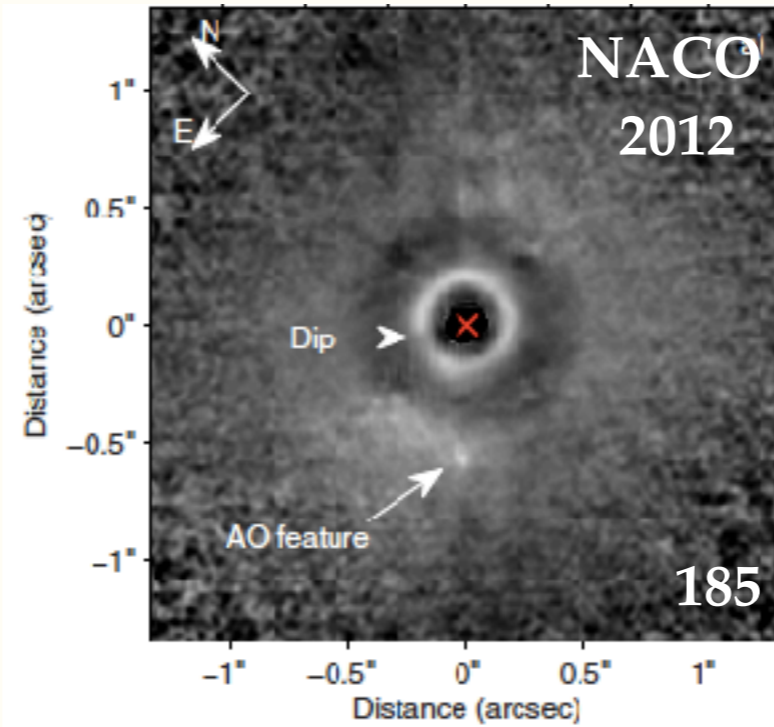
Evolution of AO

HD169142

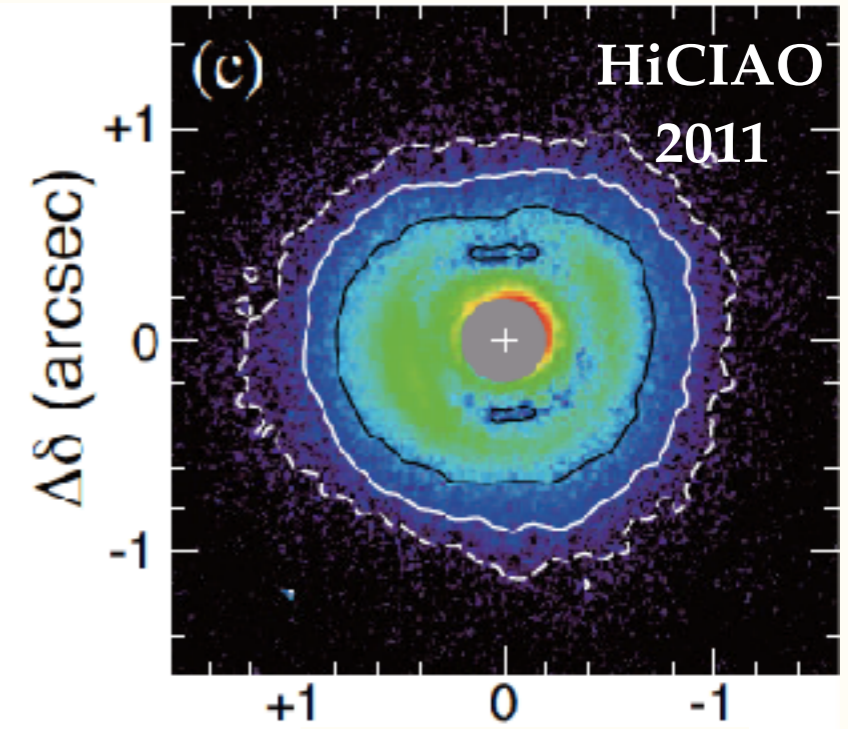
Hales et al. 2006



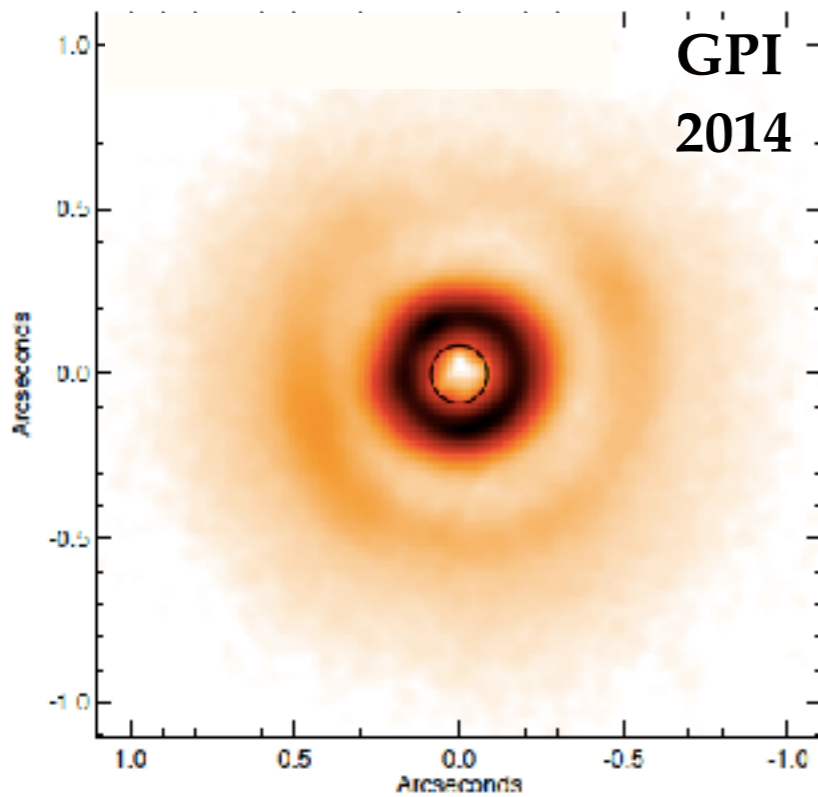
Quanz et al. 2013



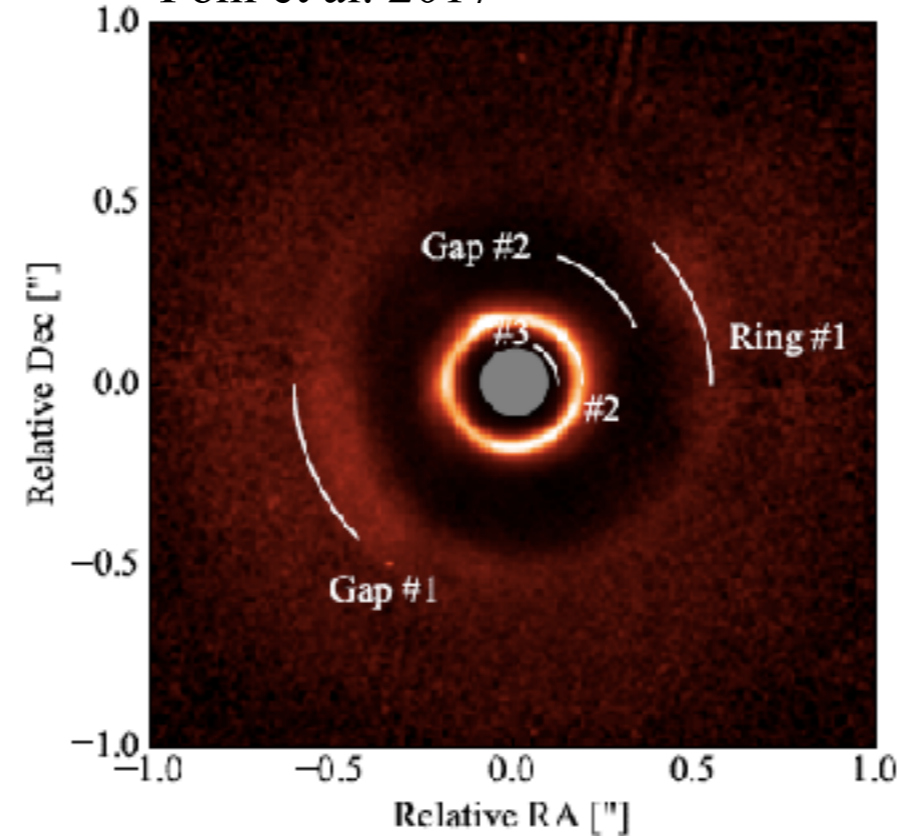
Momose et al.



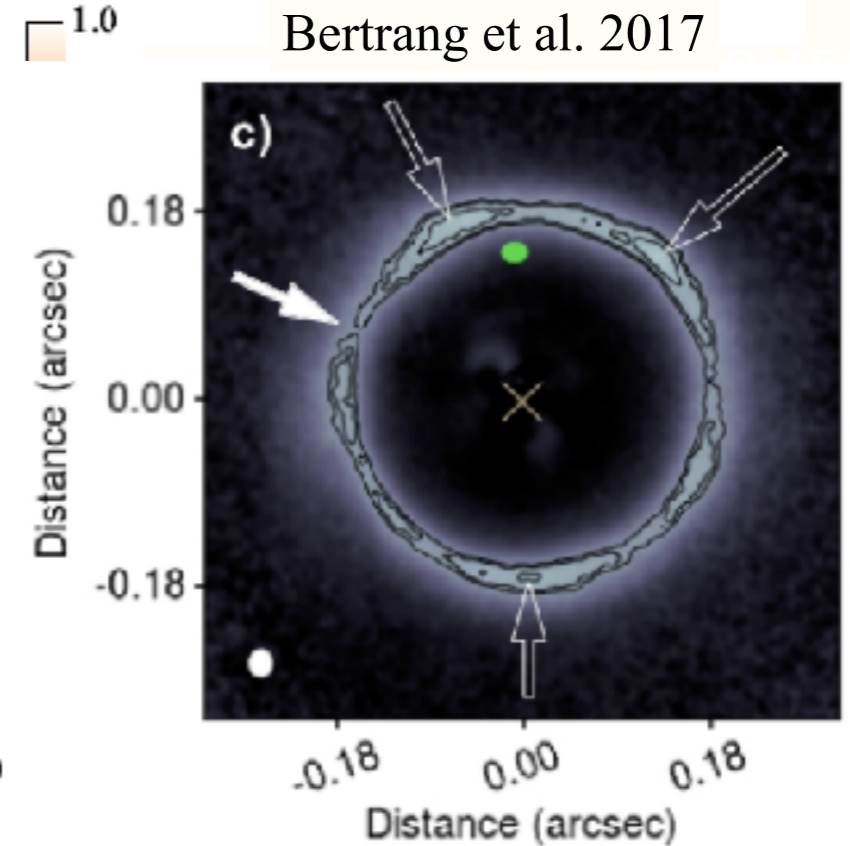
Monnier et al. 2017



Pohl et al. 2017



Bertrang et al. 2017



Outline

- Disk Observations:

Optical/Near-IR:

Rings, Spirals, Disk shadowing

Submm:

Diverse features

Synergy between Near-IR and Submm

- Planet-disk interaction theory:

Gaps/rings

Spirals

Lopsided structures

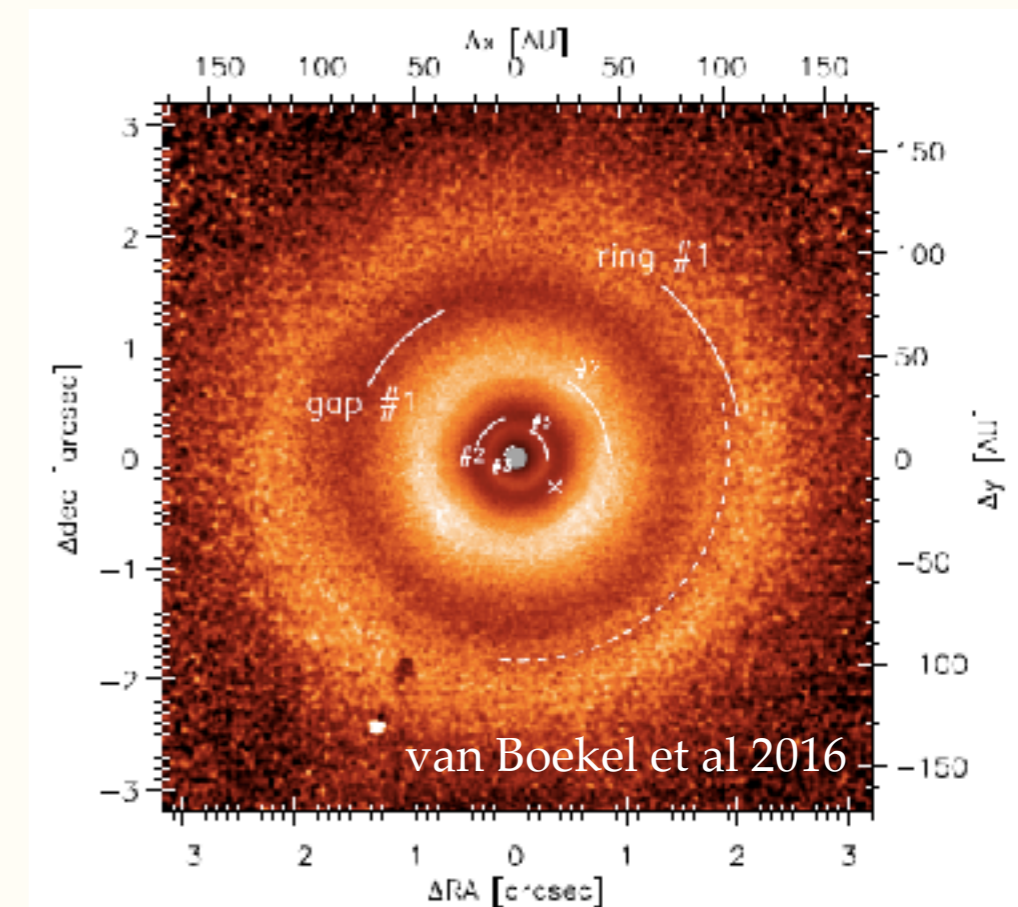
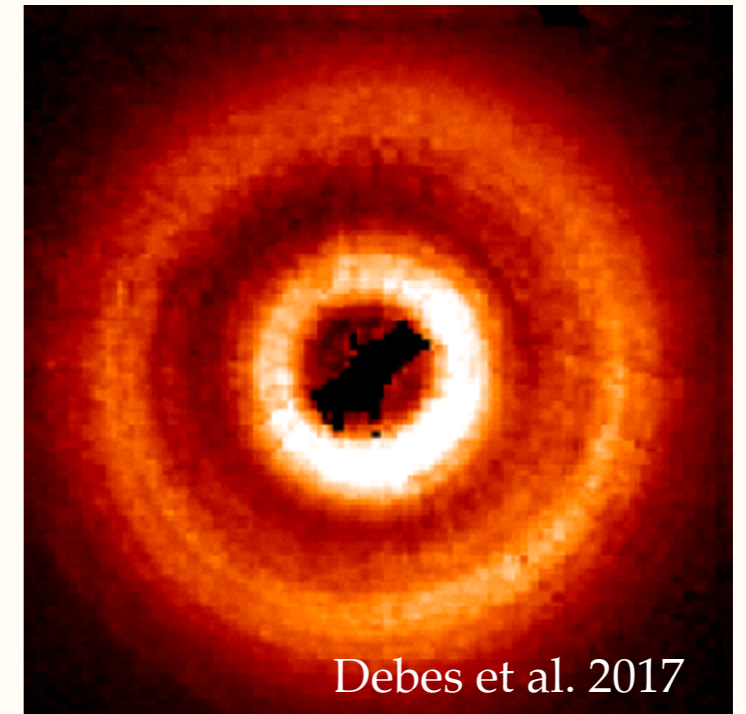
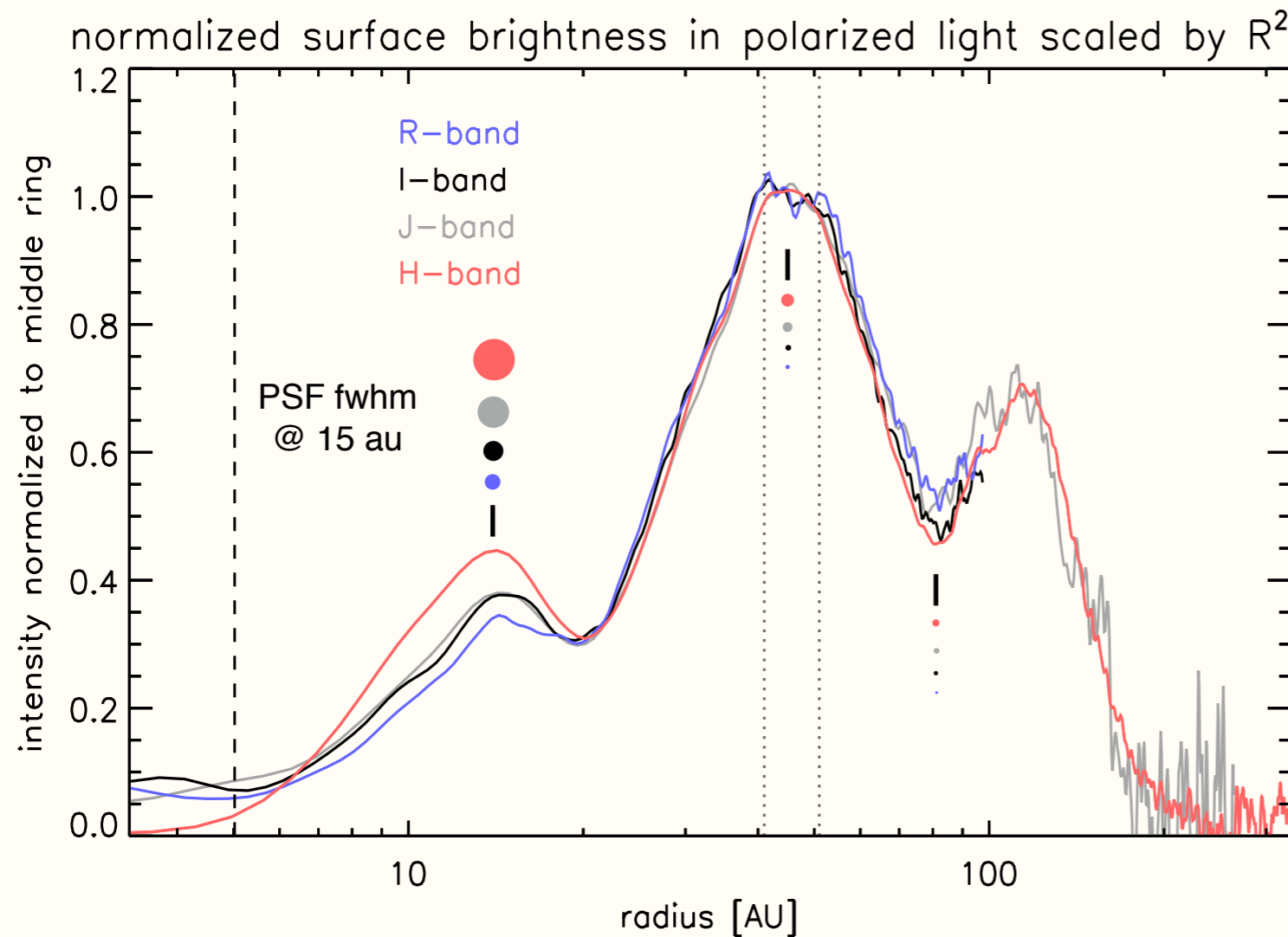
Shadows

CPDs

Rings

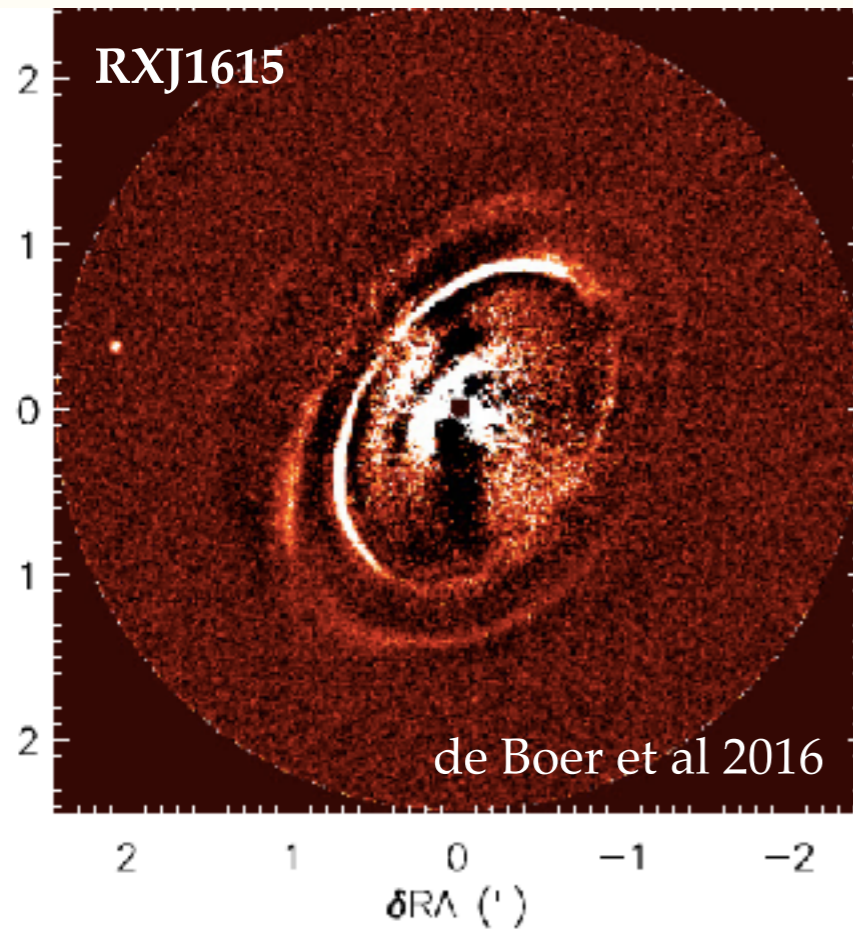
TW Hya

Gap @ 6 au, 20 au, 80 au

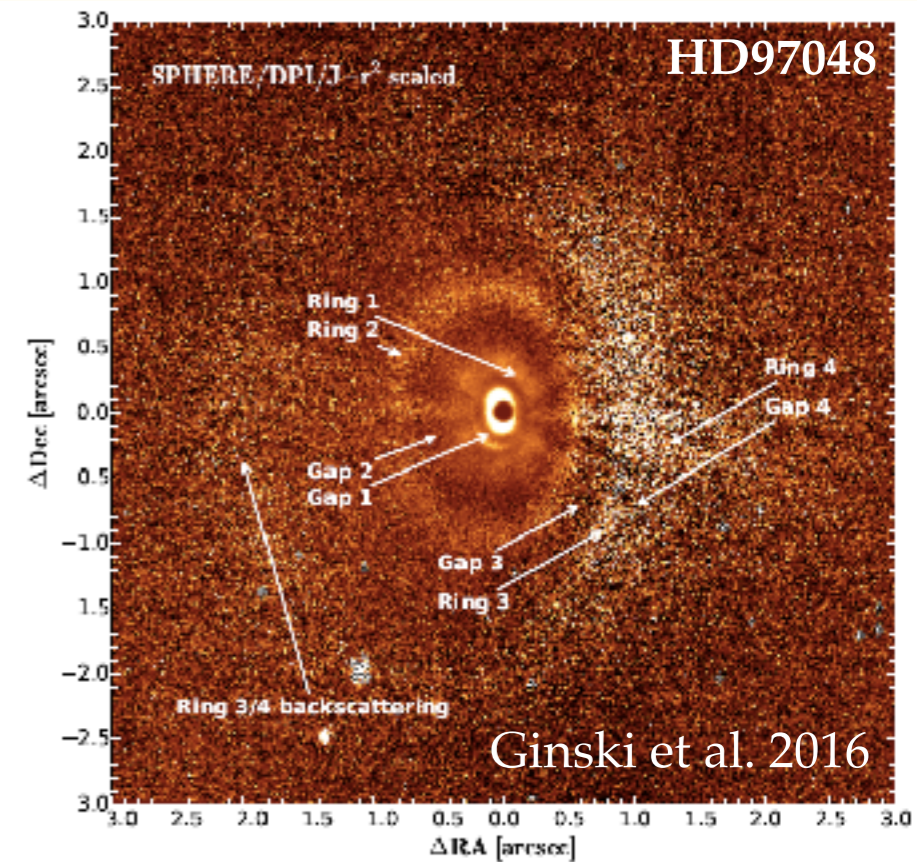


Also Debes et al. 2013, Akiyama et al. 2015, Rapson et al. 2015a,b.

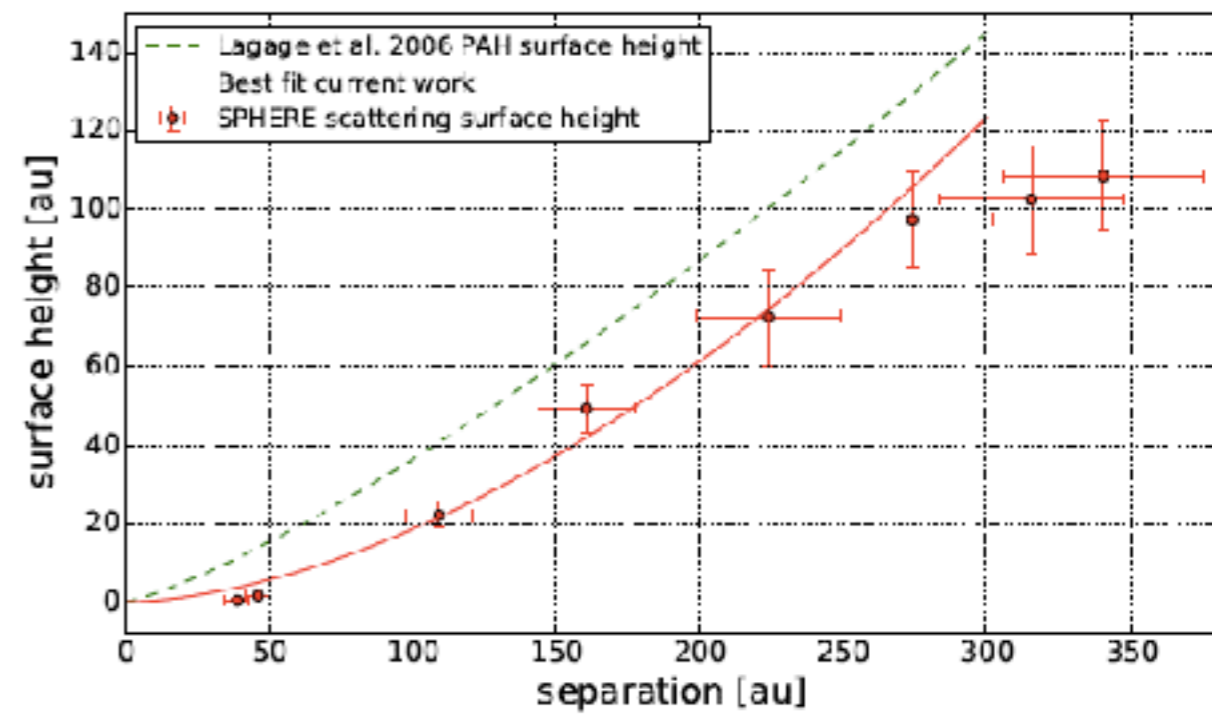
Using rings to constrain the disk surface



- An inner disk (up to ~56 au) and two rings (196 au; 278 au).
- Apparent offset provides the height of the scattering surface ($H/R \sim 0.15, 0.16$)

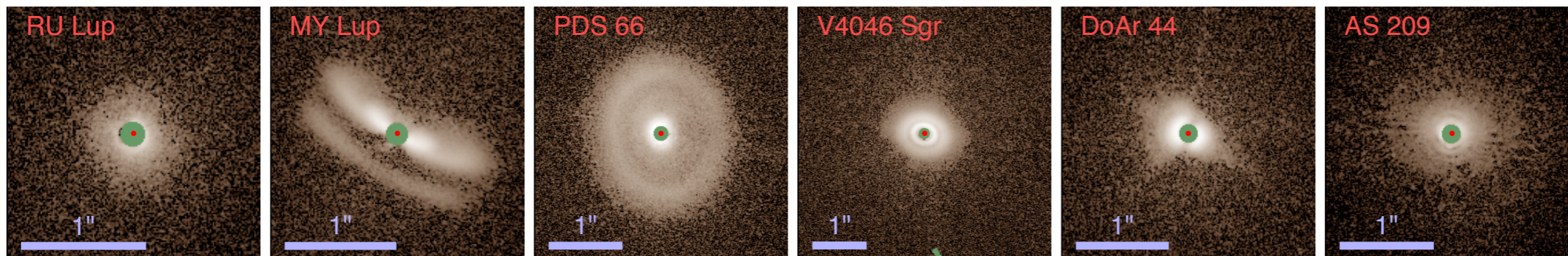
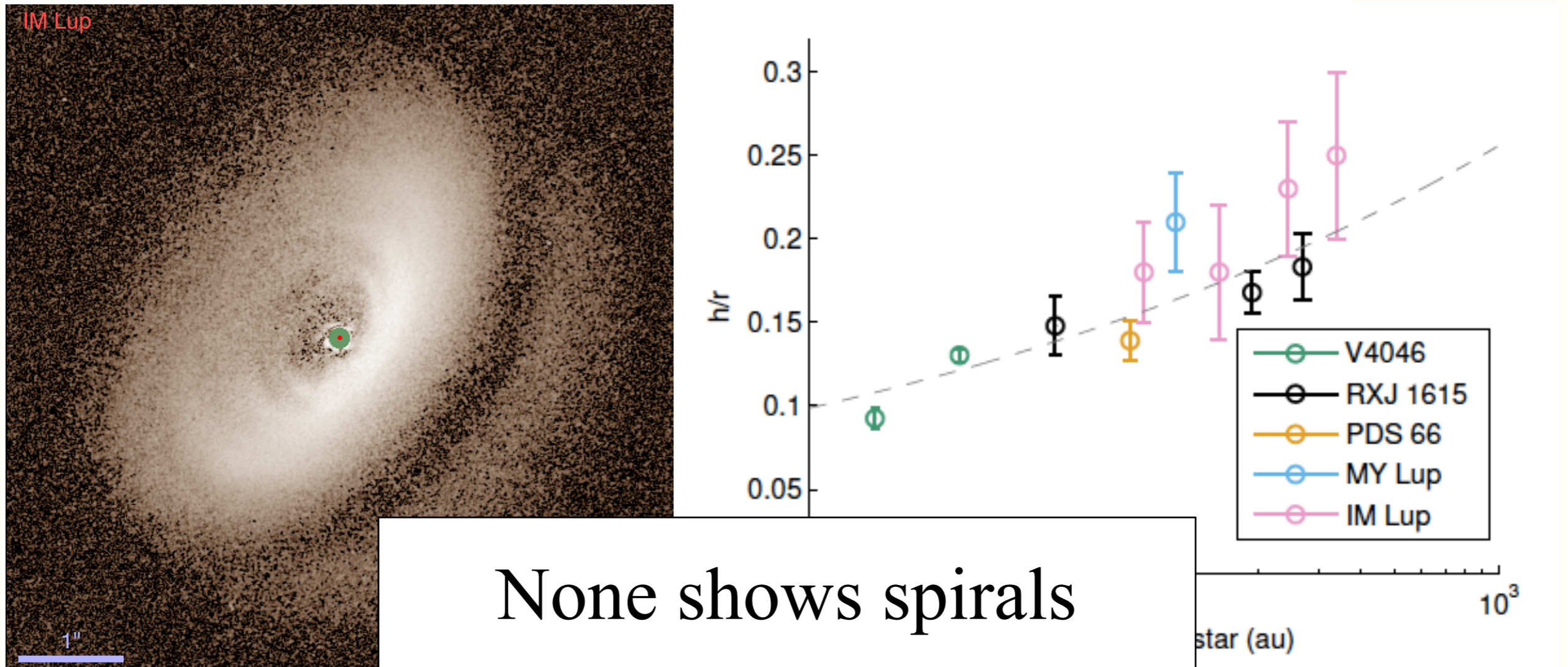


An inner disk (up to ~39 au) and 4 rings (46, 160, 274, 340 au)



Using rings to constrain the disk surface

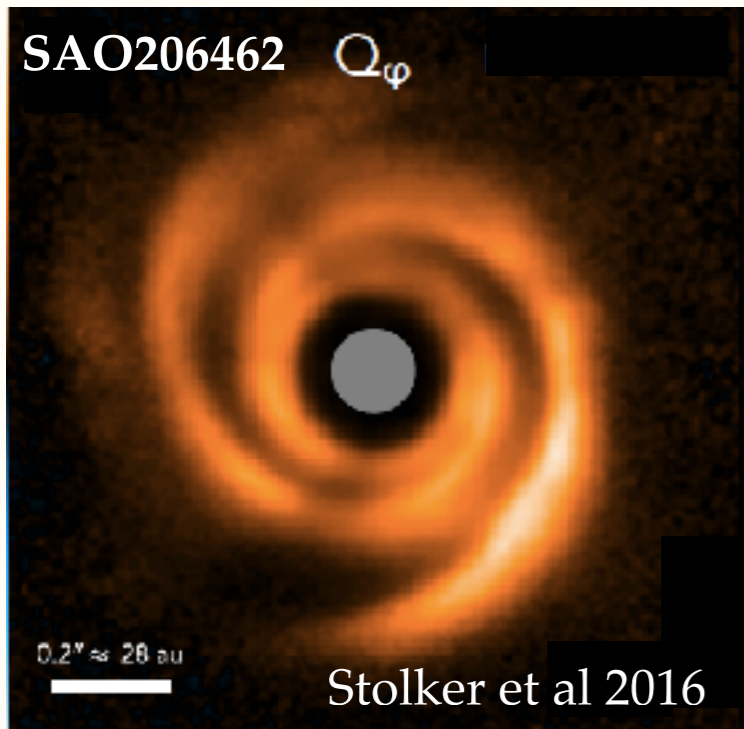
Recent survey of T Tauri stars



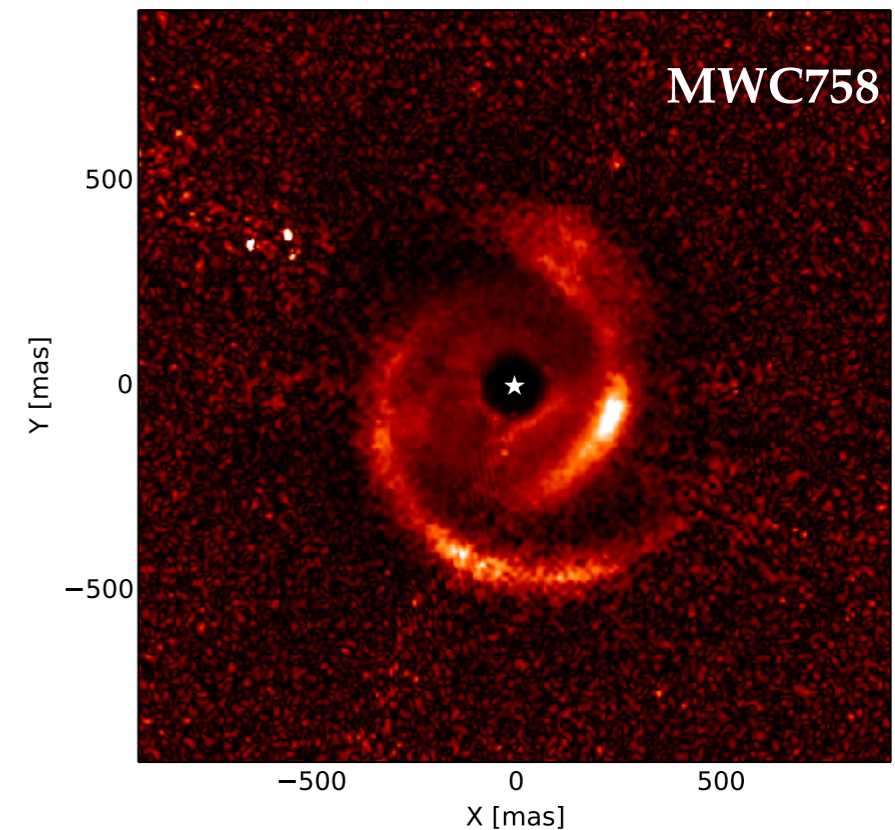
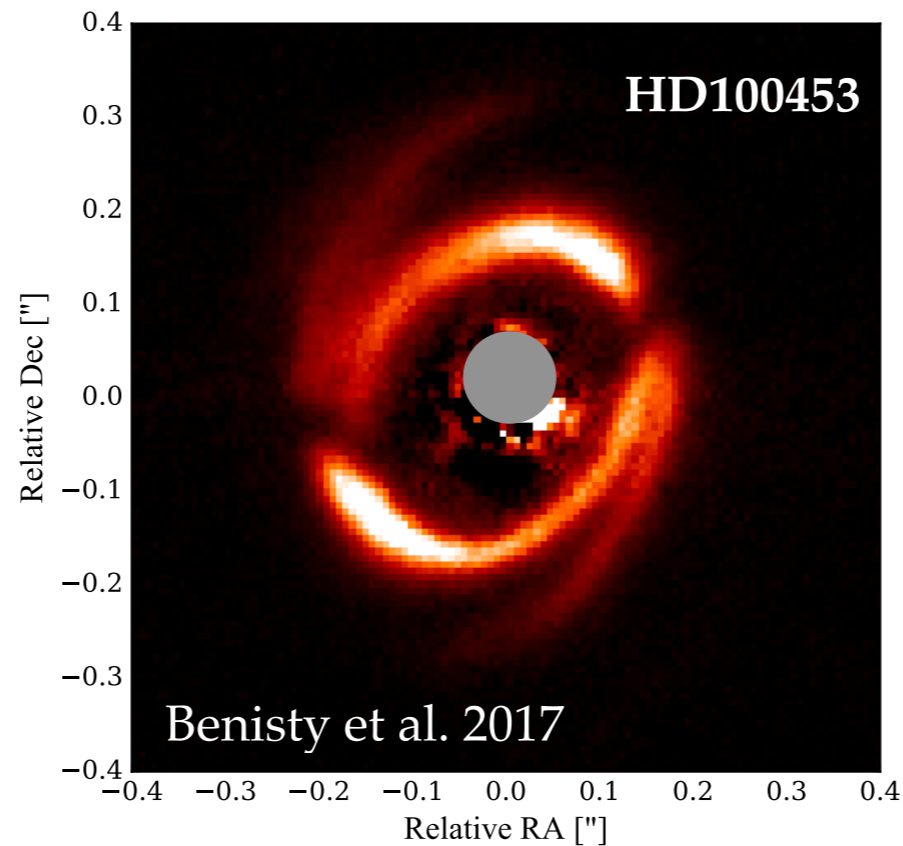
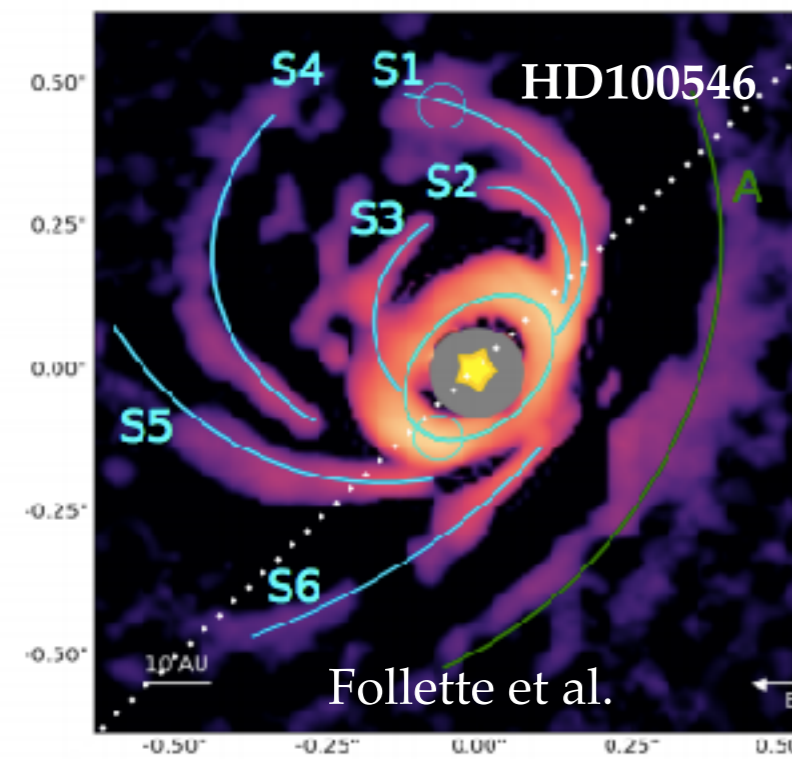
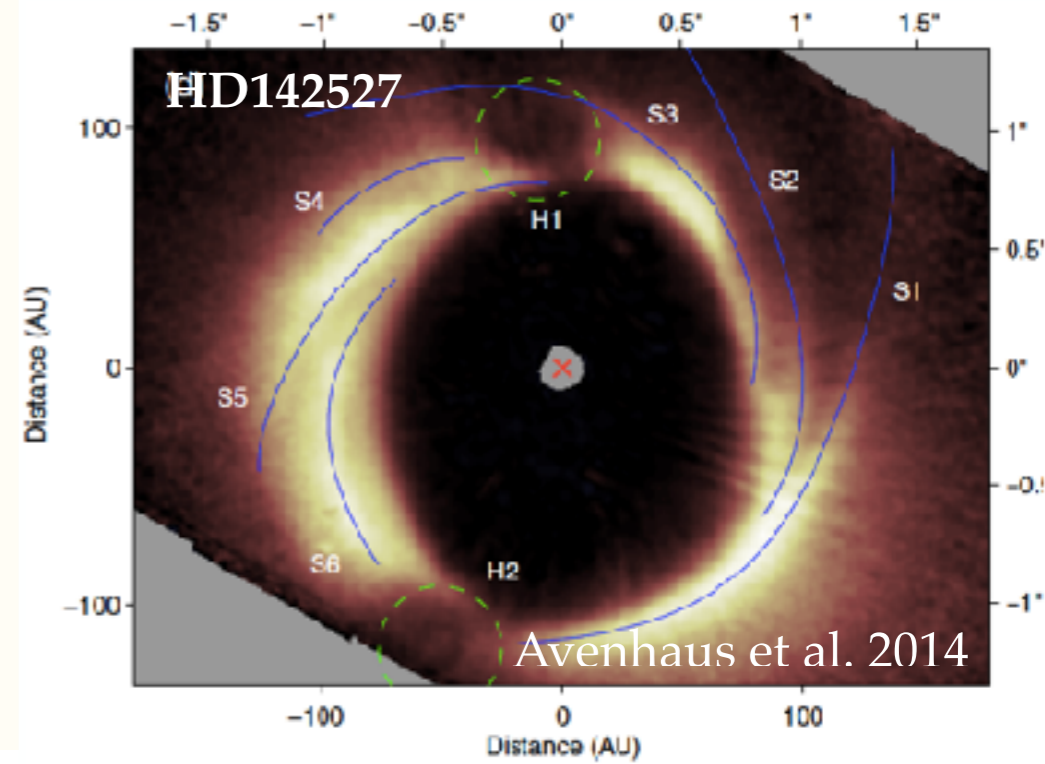
Survey of 8 T Tauri stars.

Avenhaus et al. 2018

Multiple spiral arms

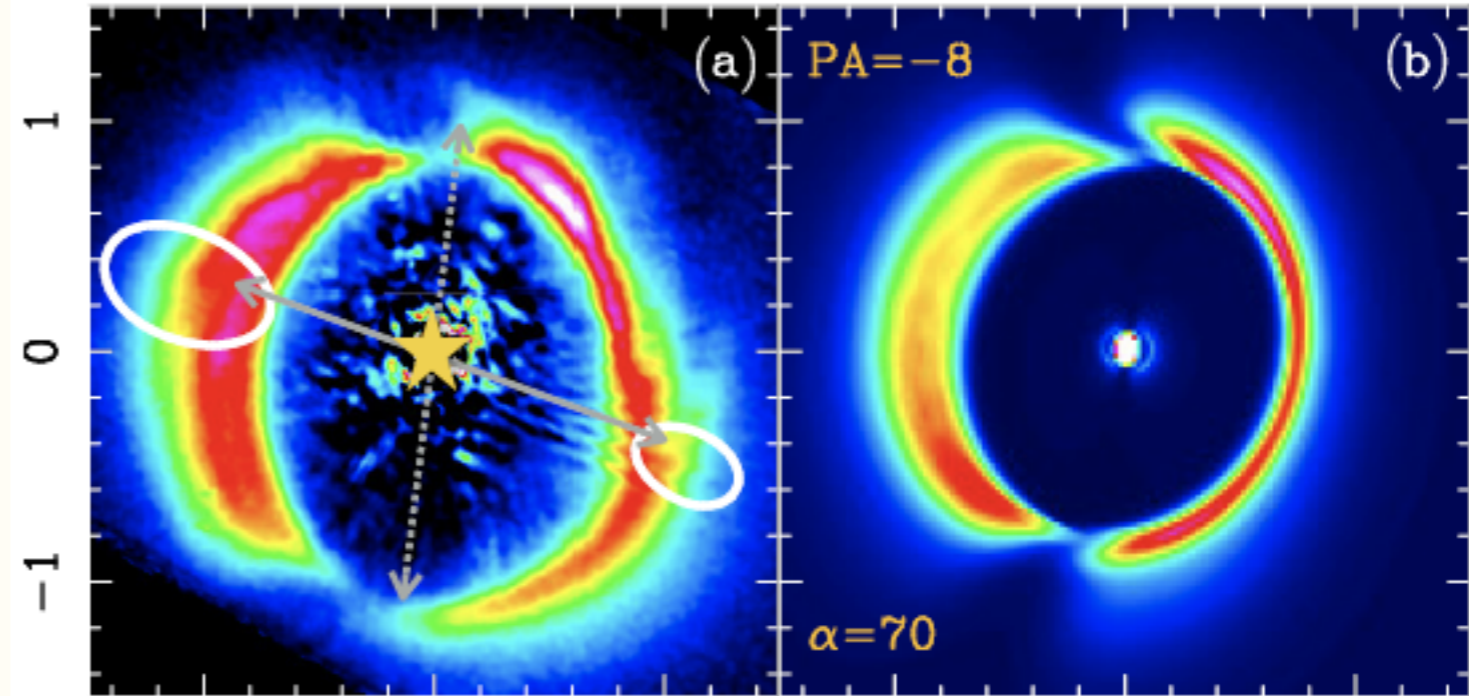
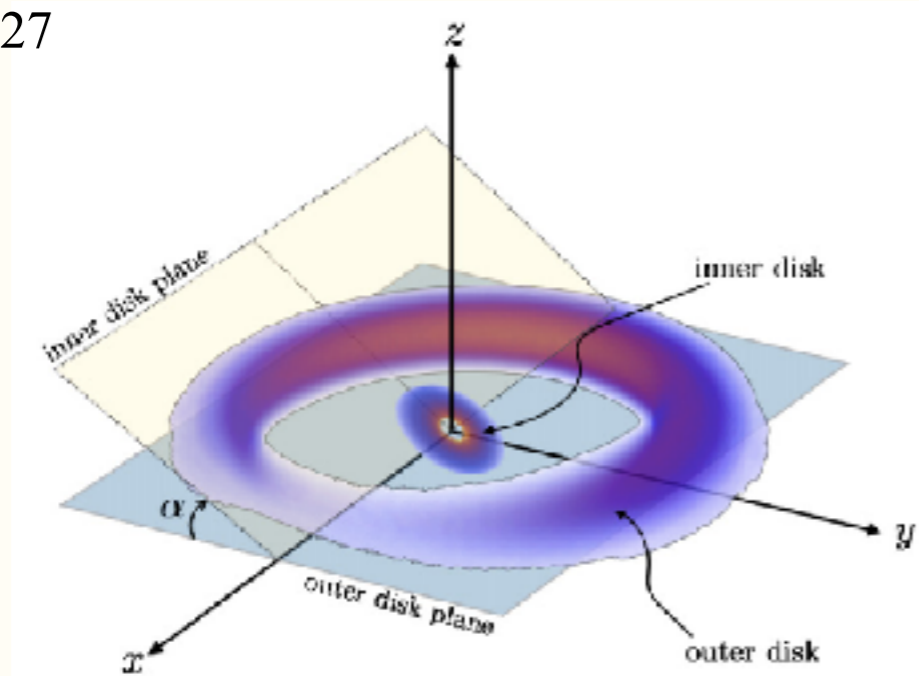


- 2 or more arms
- All Herbig transition disks
- Often with “shadows”



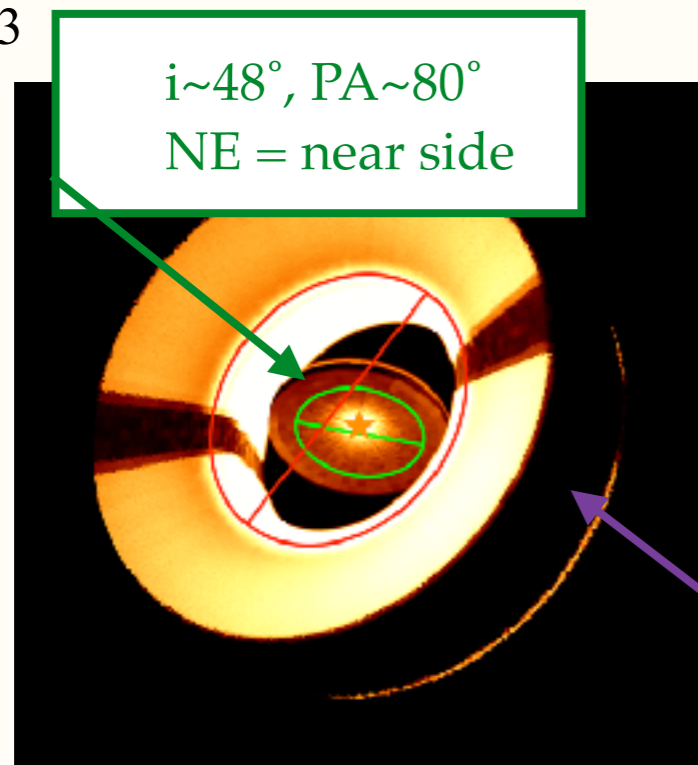
Disk shadows

HD 142527

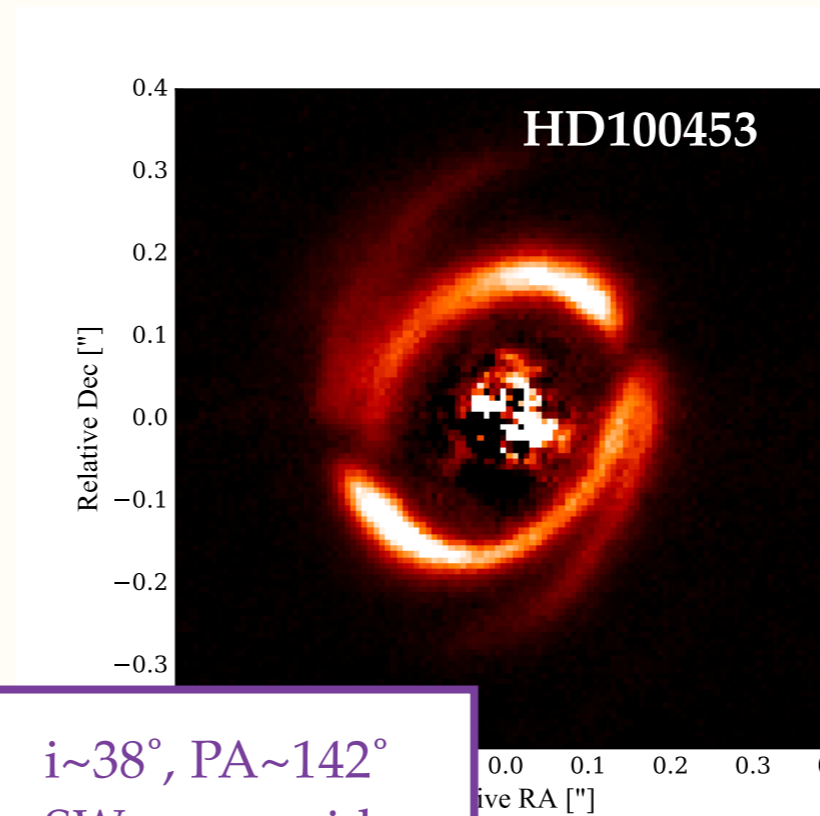


Marino et al. 2015

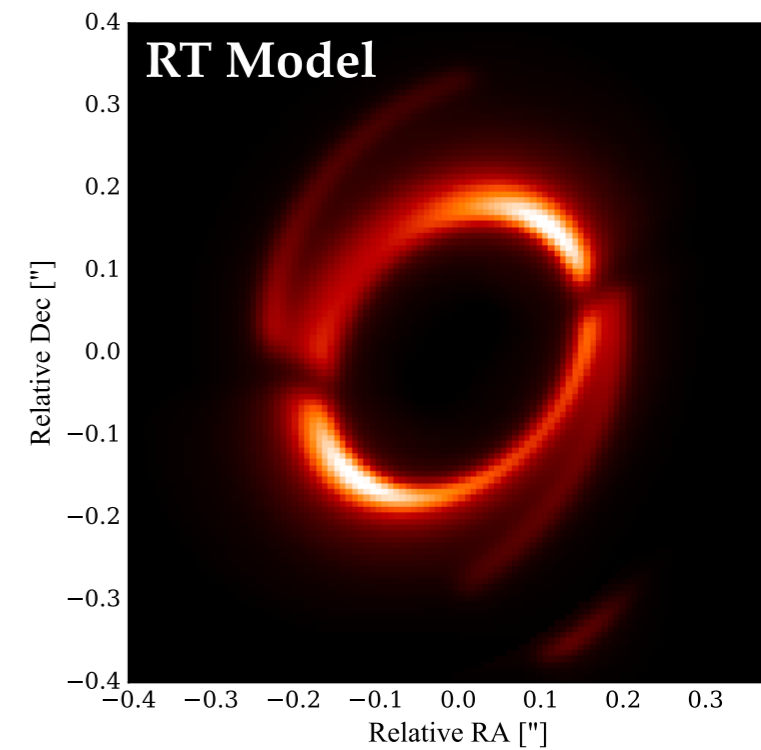
HD 100453



$i \sim 48^\circ$, $PA \sim 80^\circ$
NE = near side

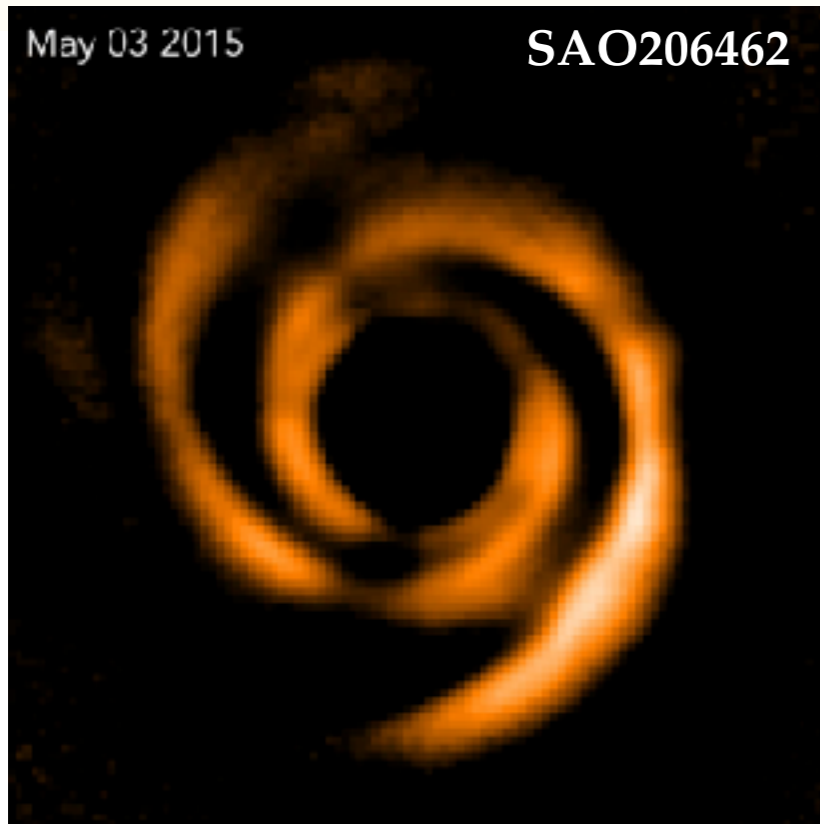


$i \sim 38^\circ$, $PA \sim 142^\circ$
SW = near side

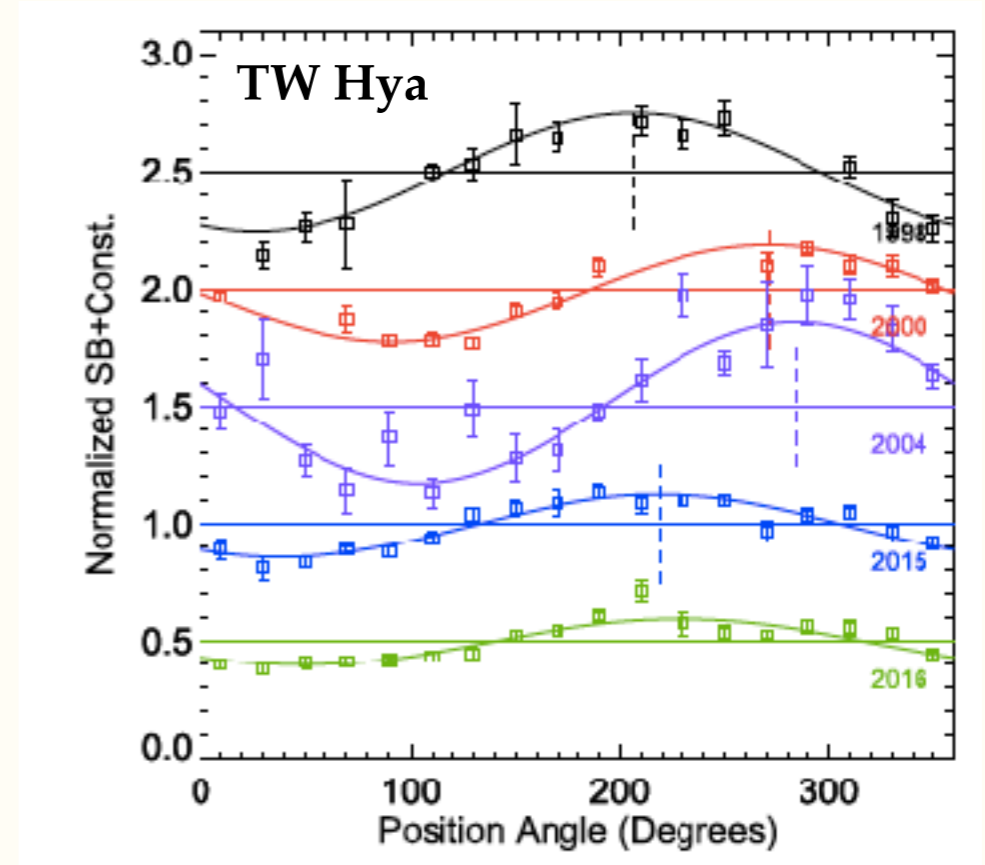


Min et al. 2017, Long et al. 2017

Variable disk shadows



Stolker et al. 2017b



Debes et al. 2017

- Strongly dynamic inner regions
- Significantly misaligned and optically thick dust in the inner(-most?) regions

An inclined inner disk < 1 au precessing with a period of ~ 16 yrs

Also Schneider et al. 2014, Wolff et al. 2016

Outline

- Disk Observations:

Optical/Near-IR:

Rings, Spirals, Disk shadowing

Submm:

Diverse features

Synergy between Near-IR and Submm

- Planet-disk interaction theory:

Gaps/rings

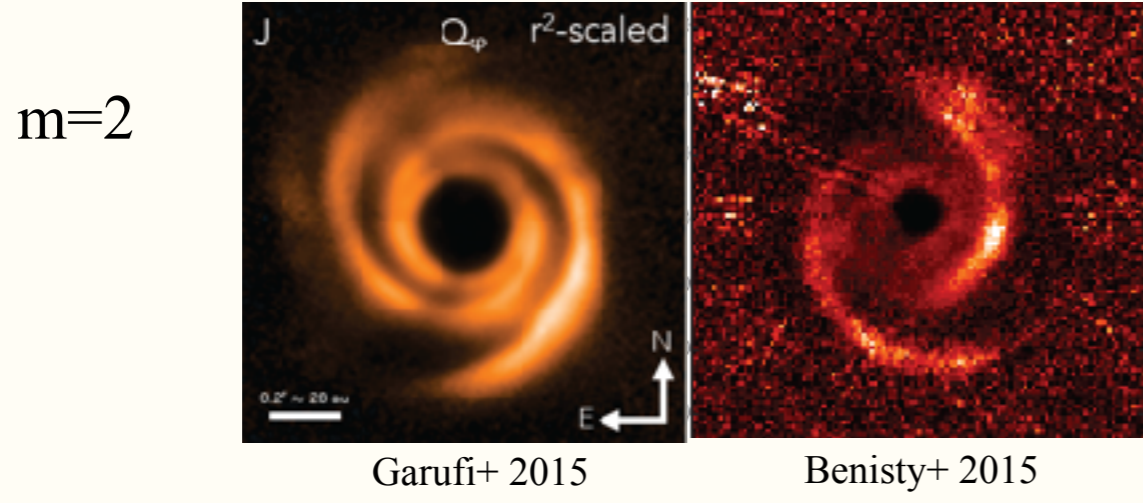
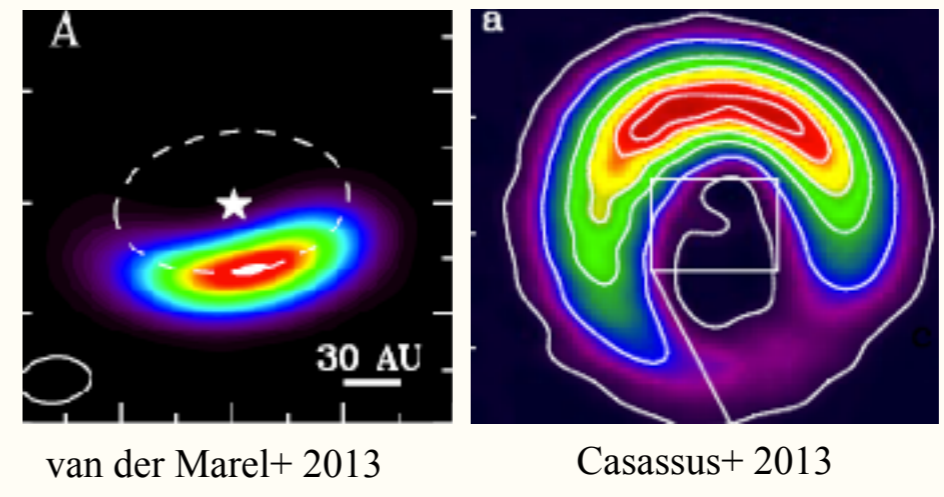
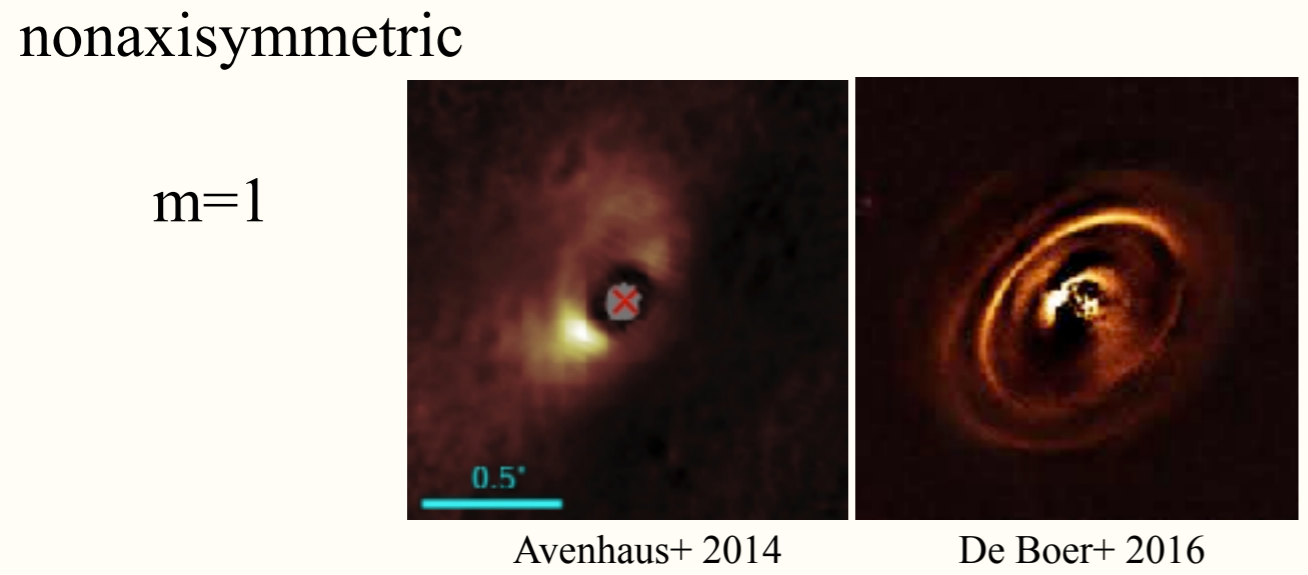
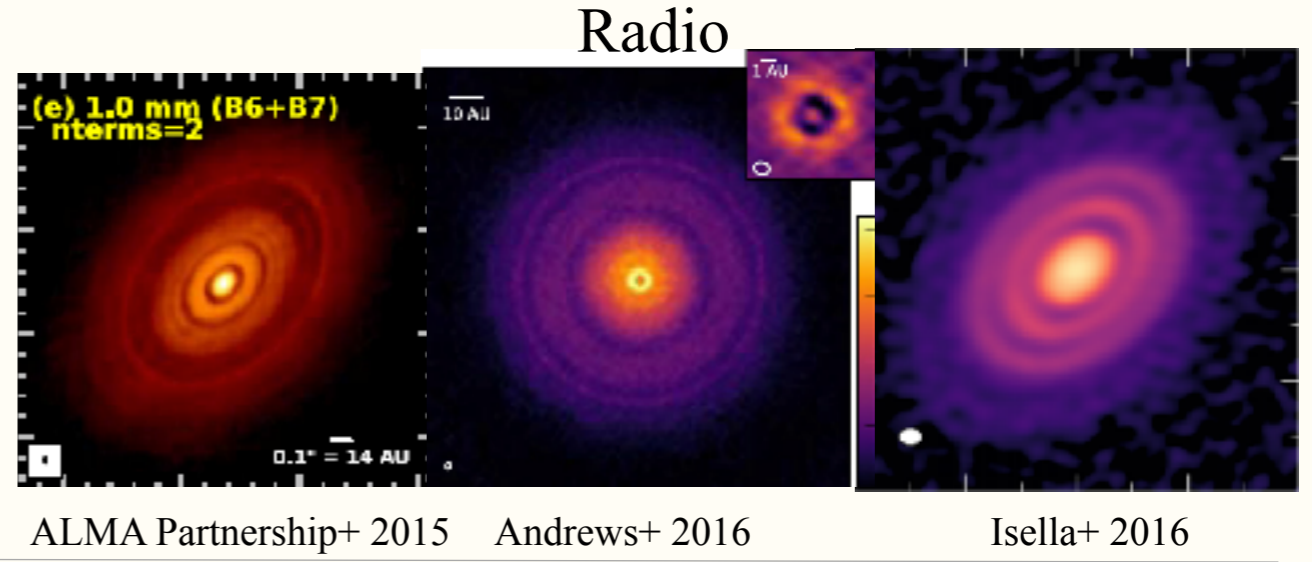
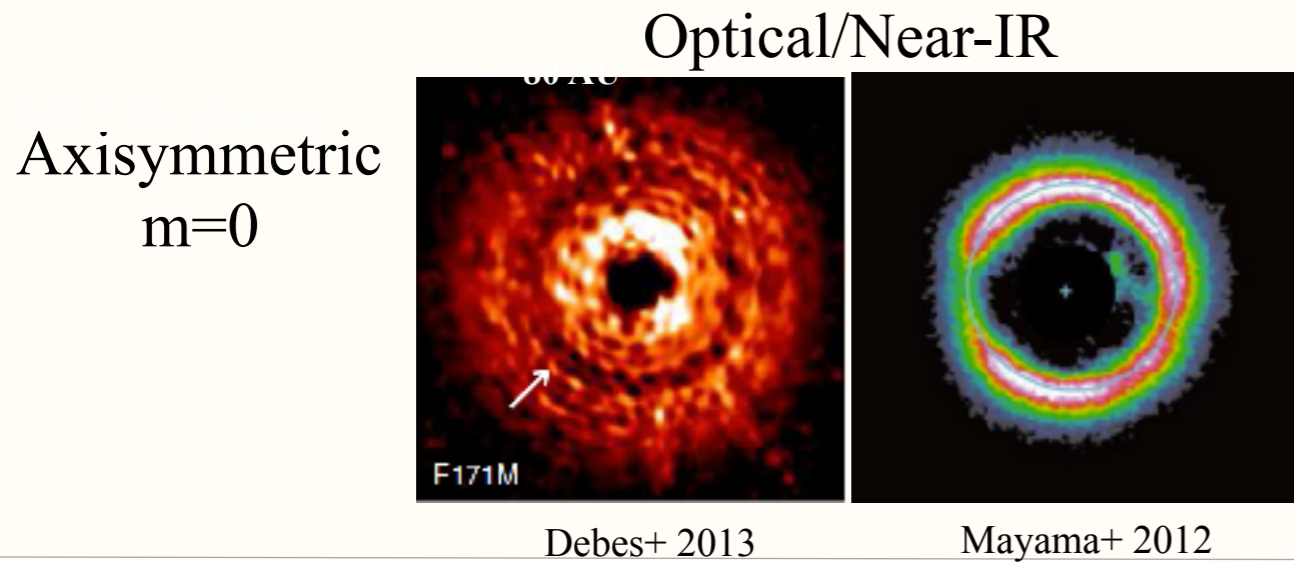
Spirals

Lopsided structures

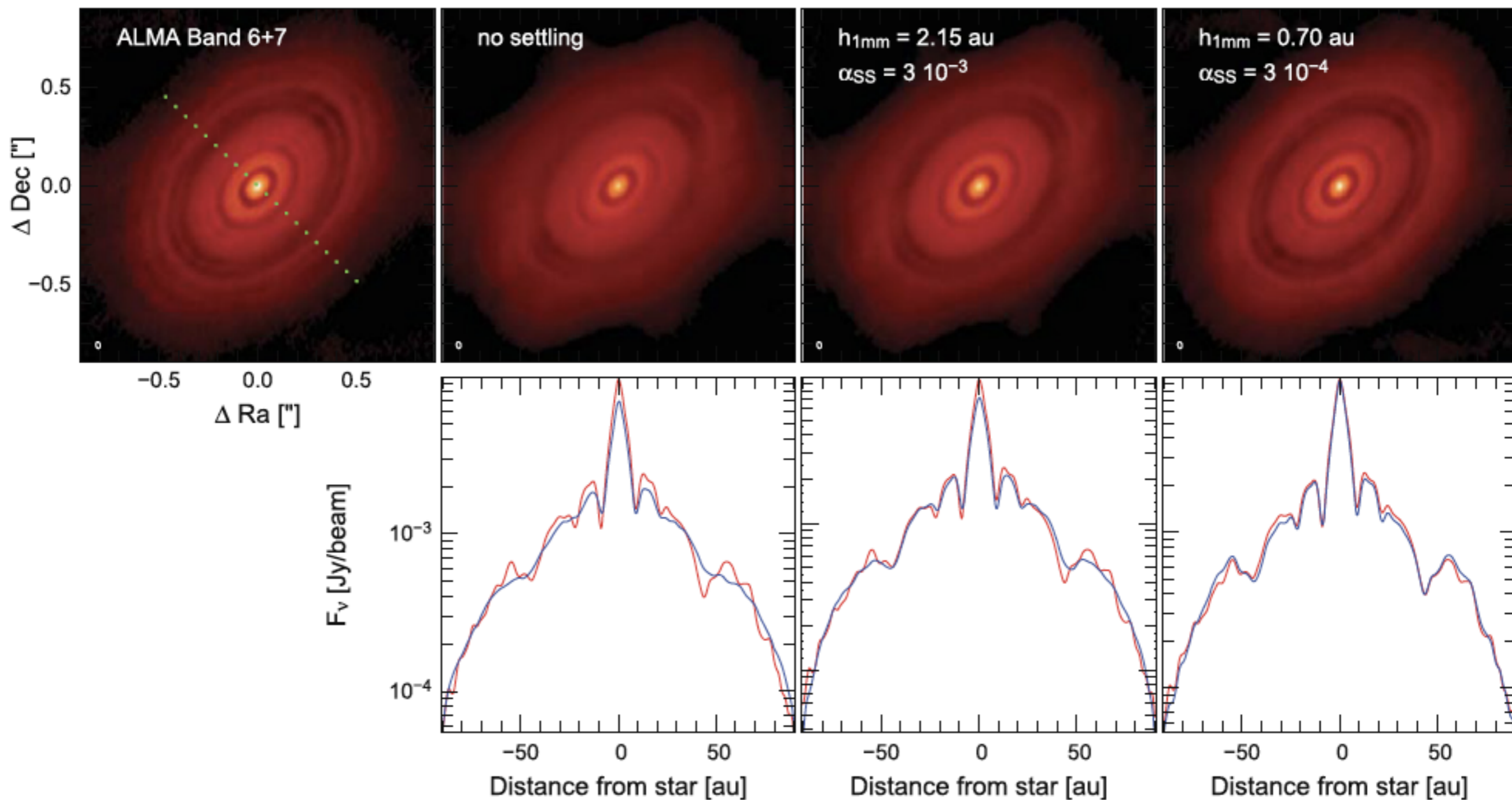
Shadows

CPDs

Diverse disk features too



Constraints for disk surface and disk turbulence:

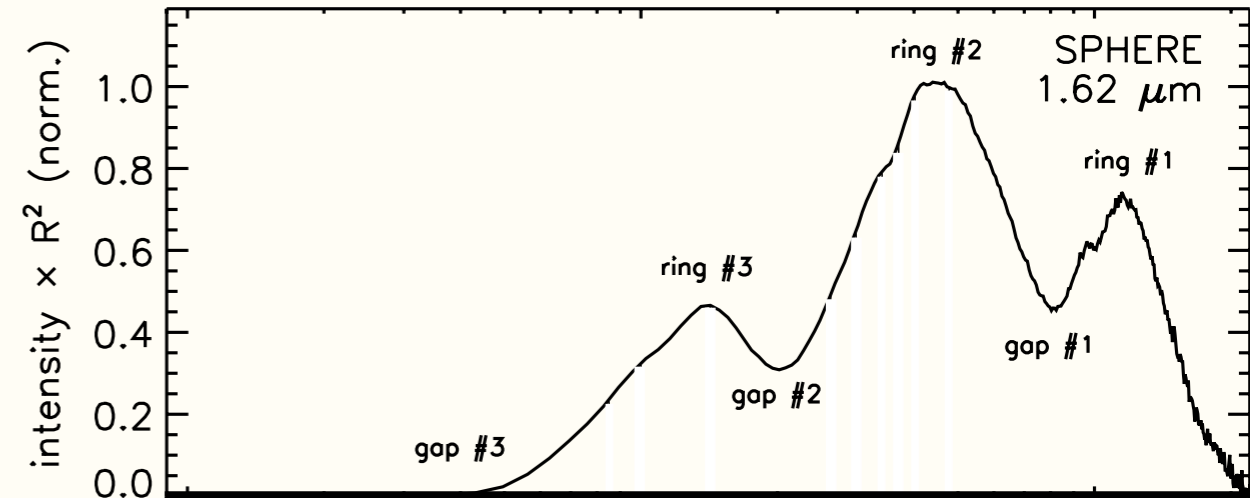
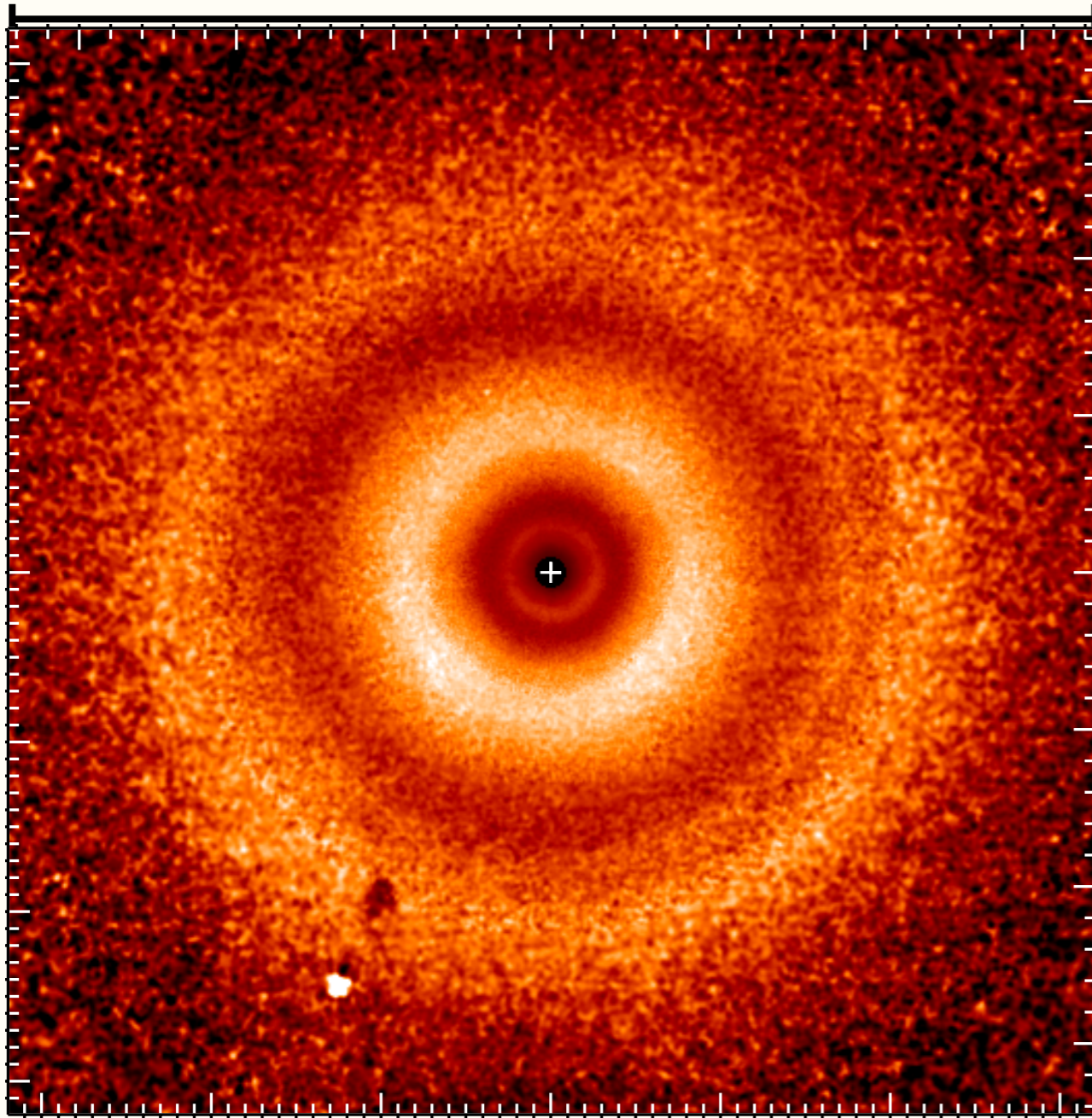


Pinte et al. 2016

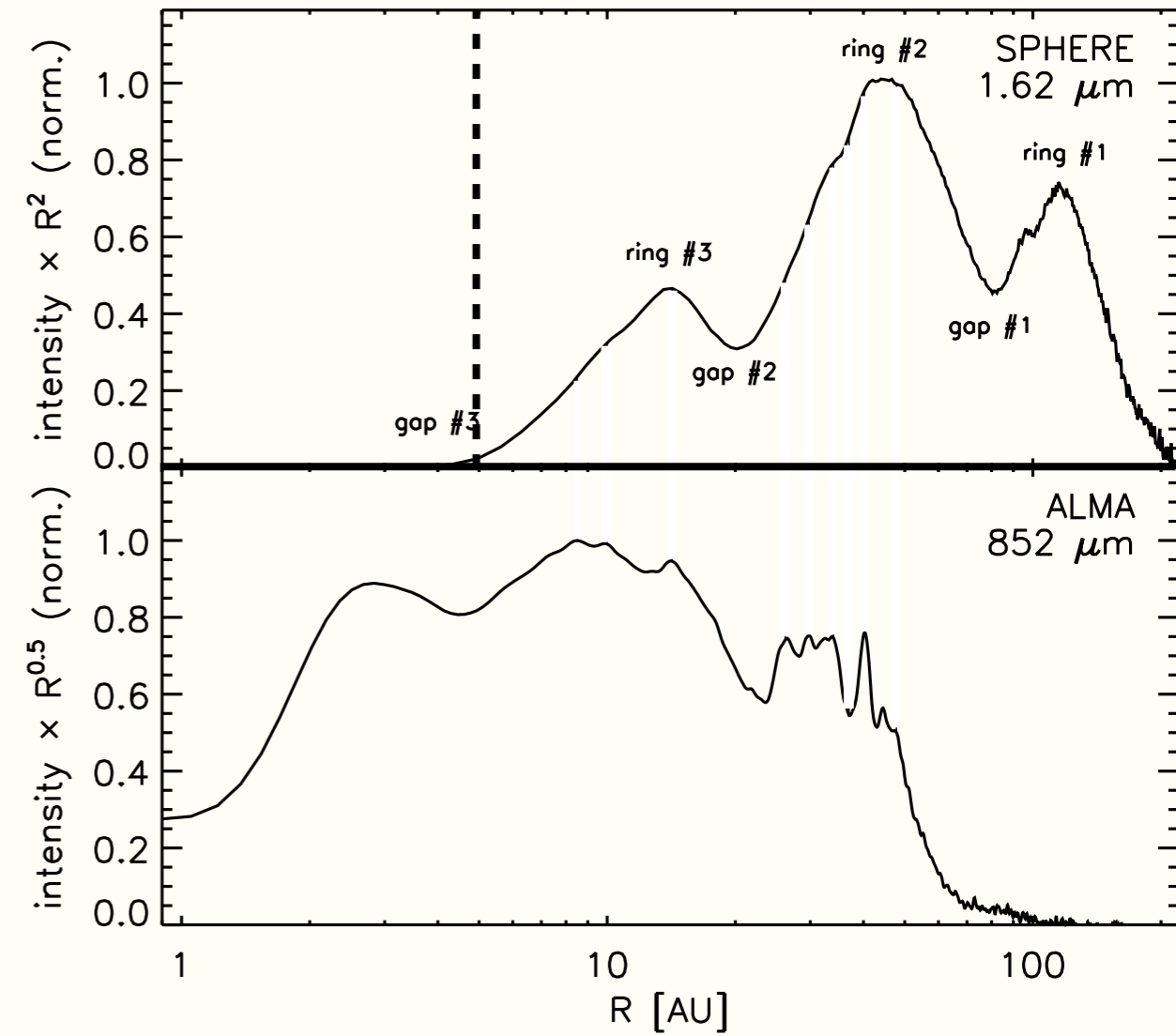
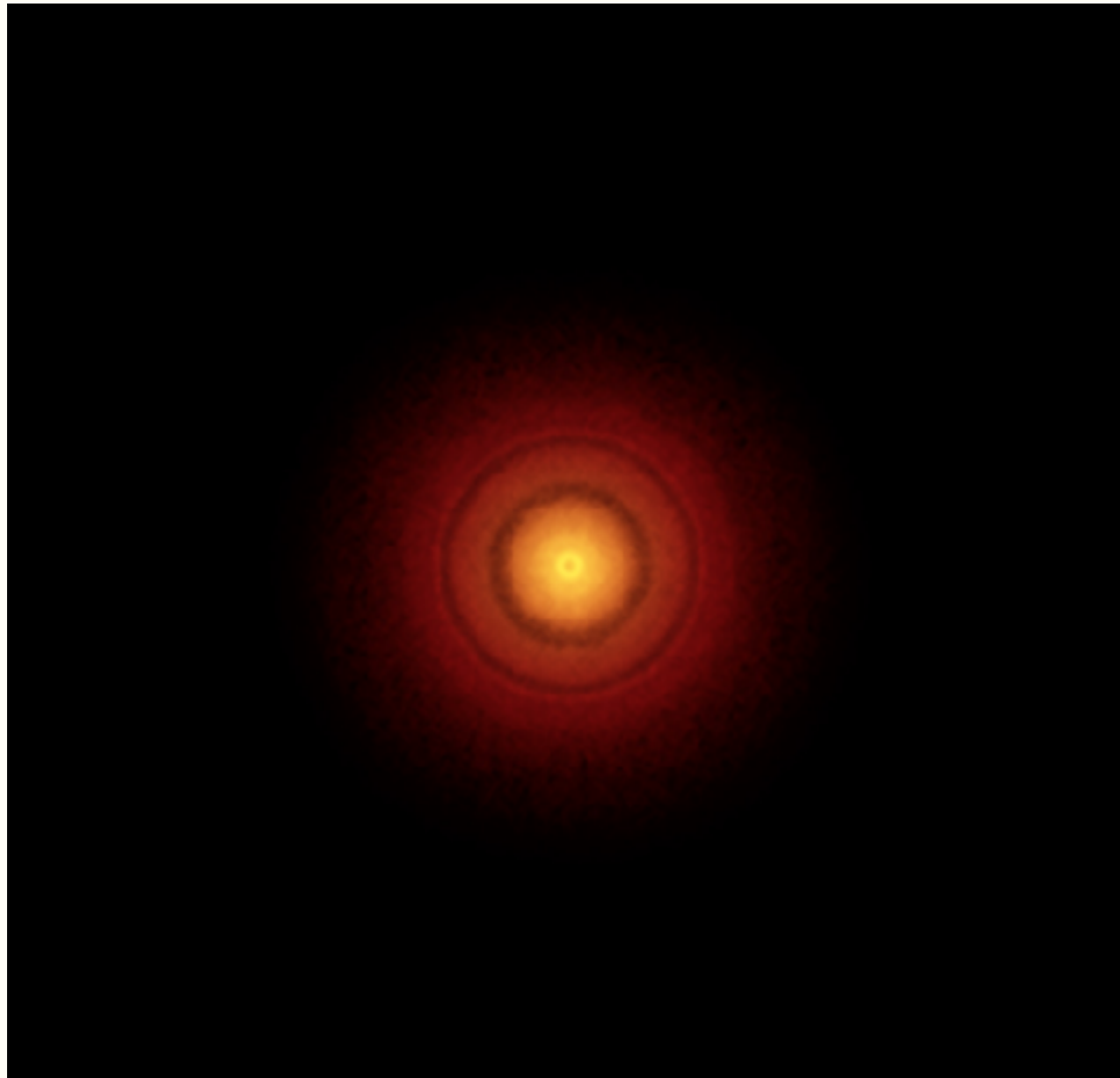
$$H_d \sim \sqrt{\frac{\alpha}{T_s}} H$$

Synergy between Near-IR and Sub-mm

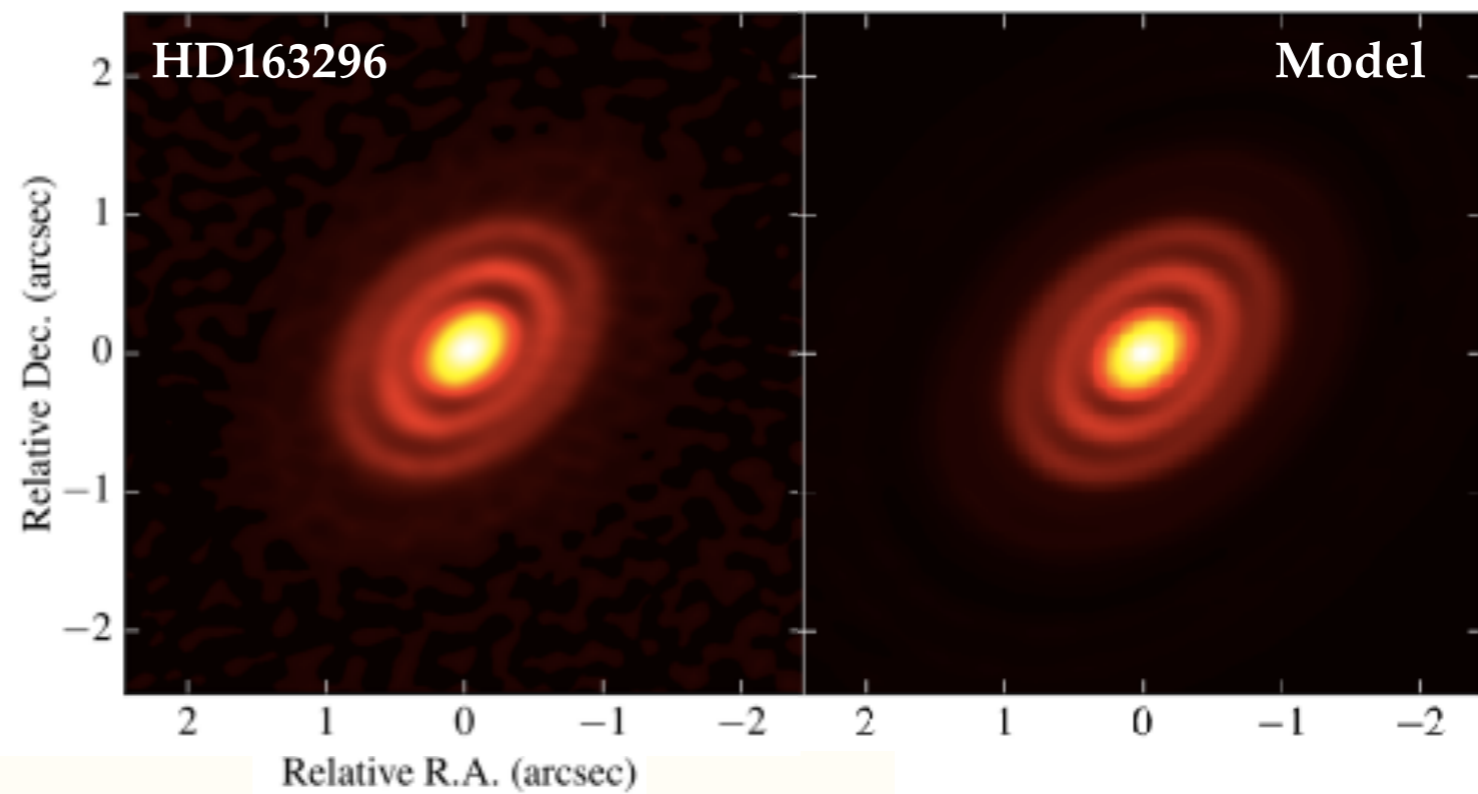
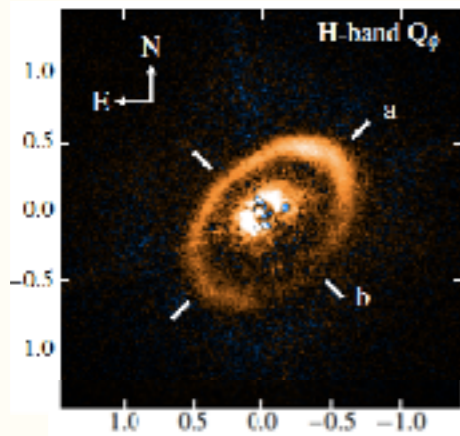
6.4'' = 380 au



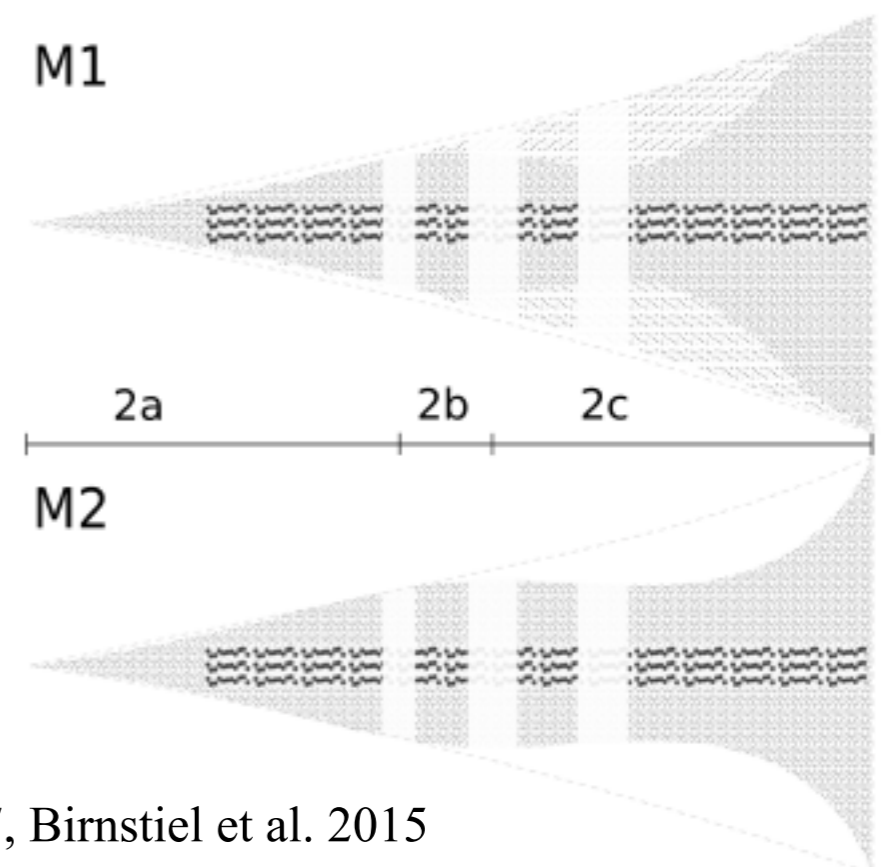
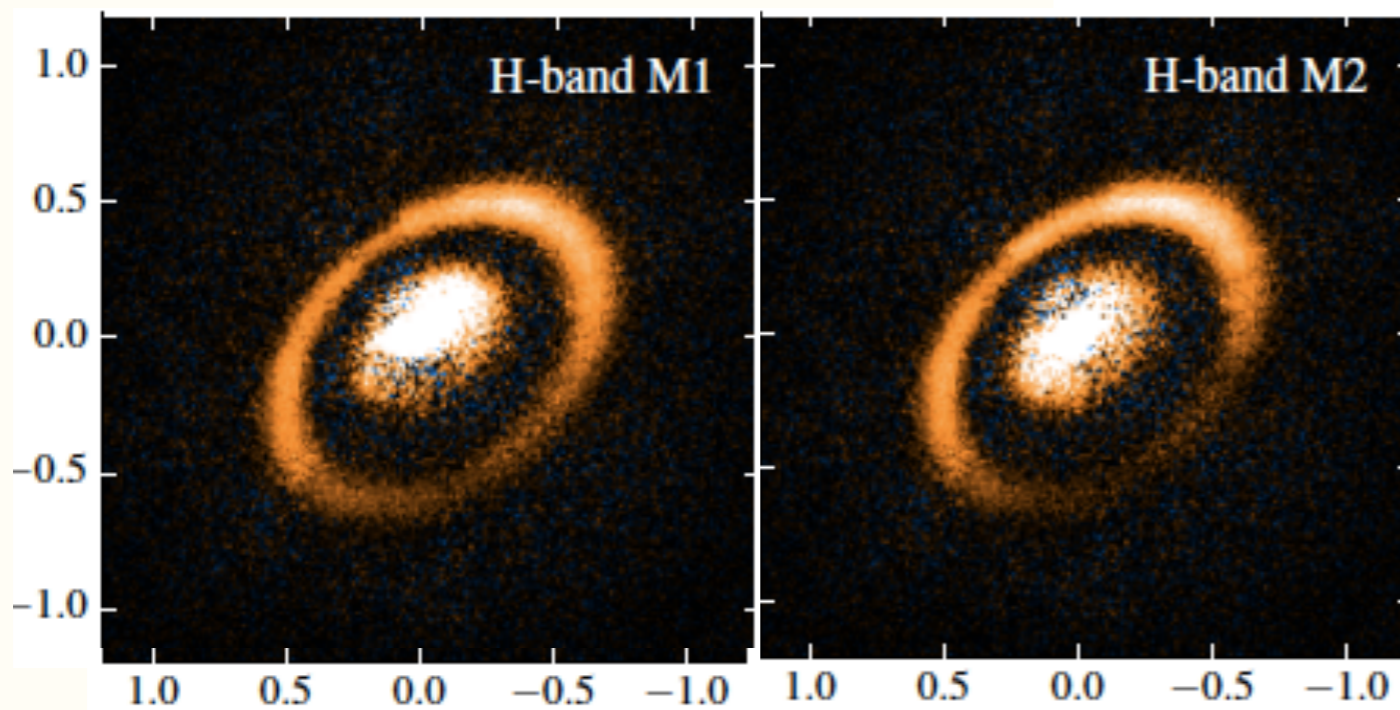
Near-IR and ALMA



Vertical distribution of grains



Rings @ 80,
124, 200 au



Outline

- Disk Observations:

1. Know the disk => Use disk features to probe the planets
Disk features => Know the disk (e.g. turbulence, dust properties)

2. Can we model the disk with all constraints from different methods (imaging, SED), different wavelengths (near-IR, submm), techniques (ADI, PDI, sub-mm thermal/polarization), etc to build a complete disk picture?

3. Large sample now. Any trend with different samples?

Spirals

Lopsided structures

Shadows

CPDs

Outline

- Disk Observations:

Optical/Near-IR:

Rings, Spirals, Disk shadowing

Submm:

Diverse features

Synergy between Near-IR and Submm

- Planet-disk interaction theory:

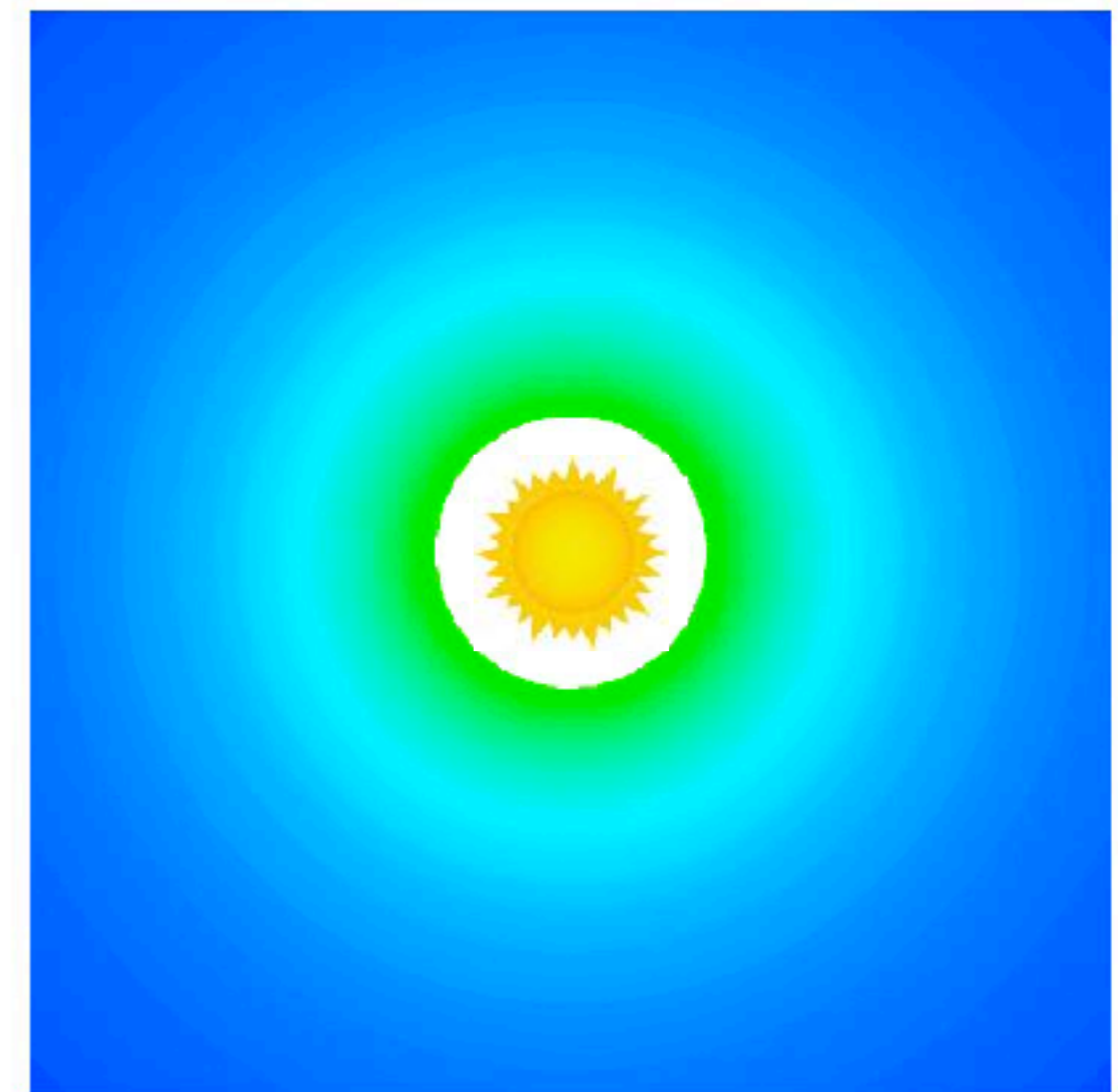
Gaps/rings (basics, dust dynamics, gas dynamics)

Spirals

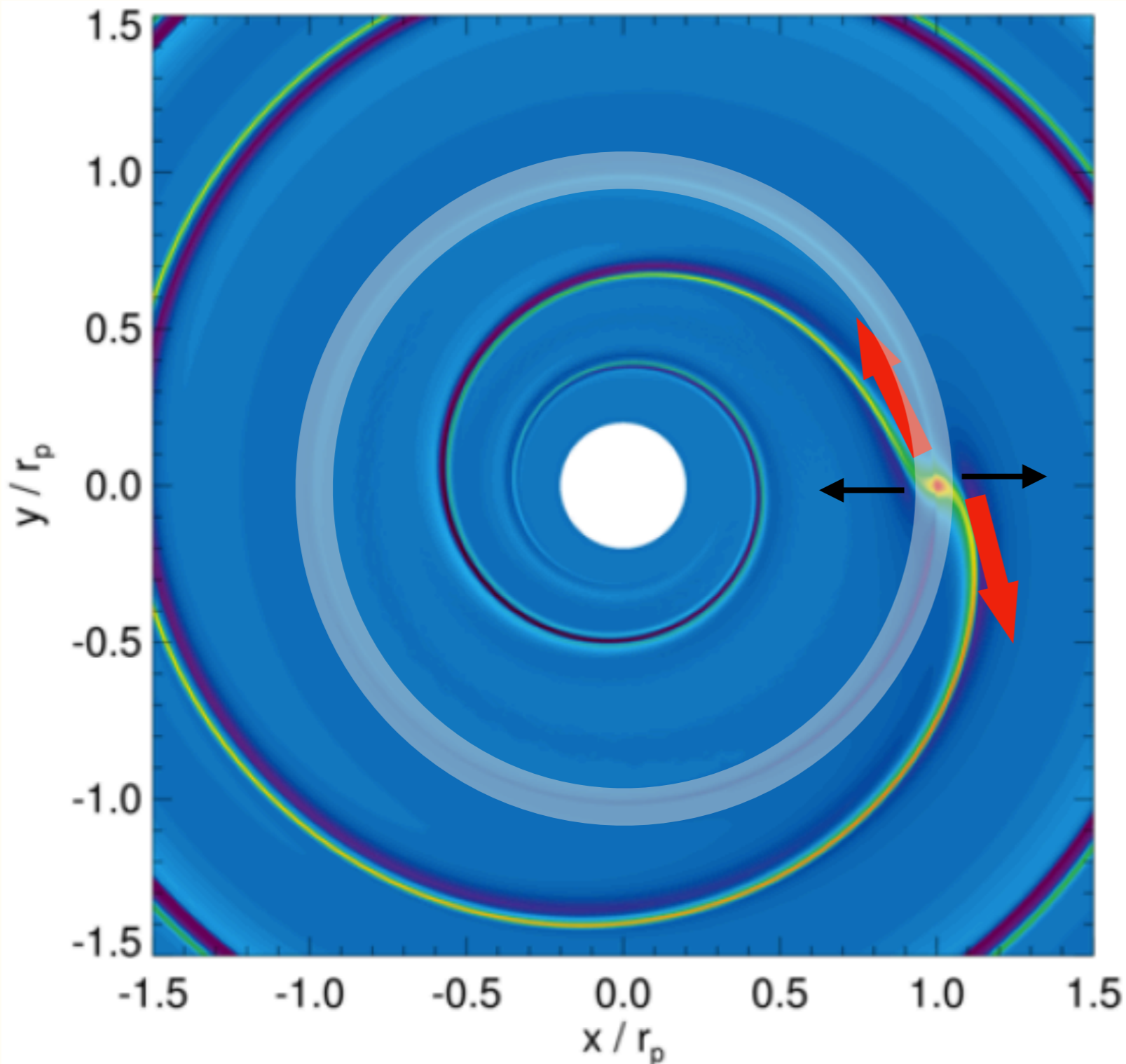
Lopsided structures

Shadows

CPDs



Planet-disk interaction: migration



Wave torque (Lindblad Resonances)

(Goldreich & Tremaine 1979, Ward 1997,
Tanaka et al. 2002)

migration timescale for both
Earth and Neptune $\sim 10^5$ years

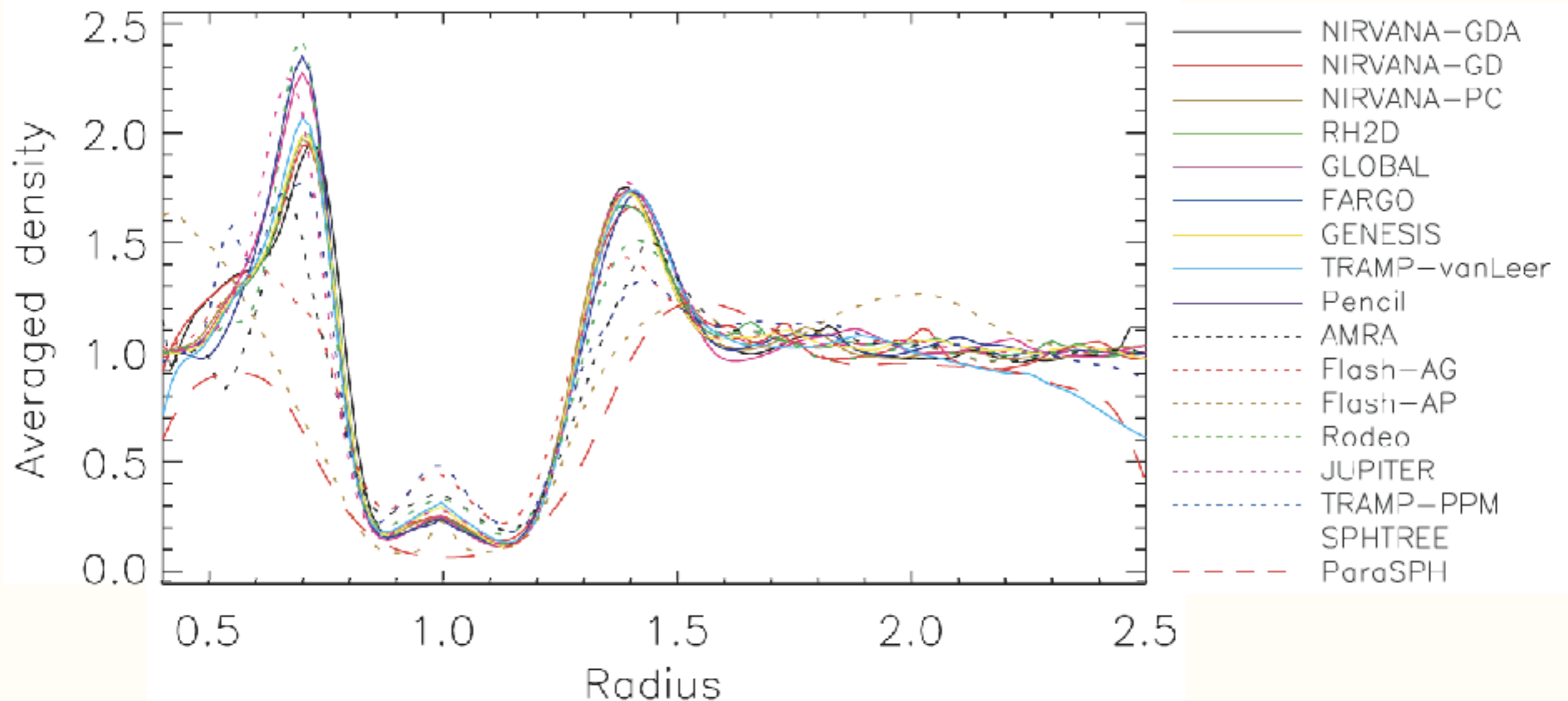
Corotation torque (horseshoe drag or corotation resonances)

Planet-disk interaction: gap opening

When planetary torque $>$ viscous torque, a gap is opened

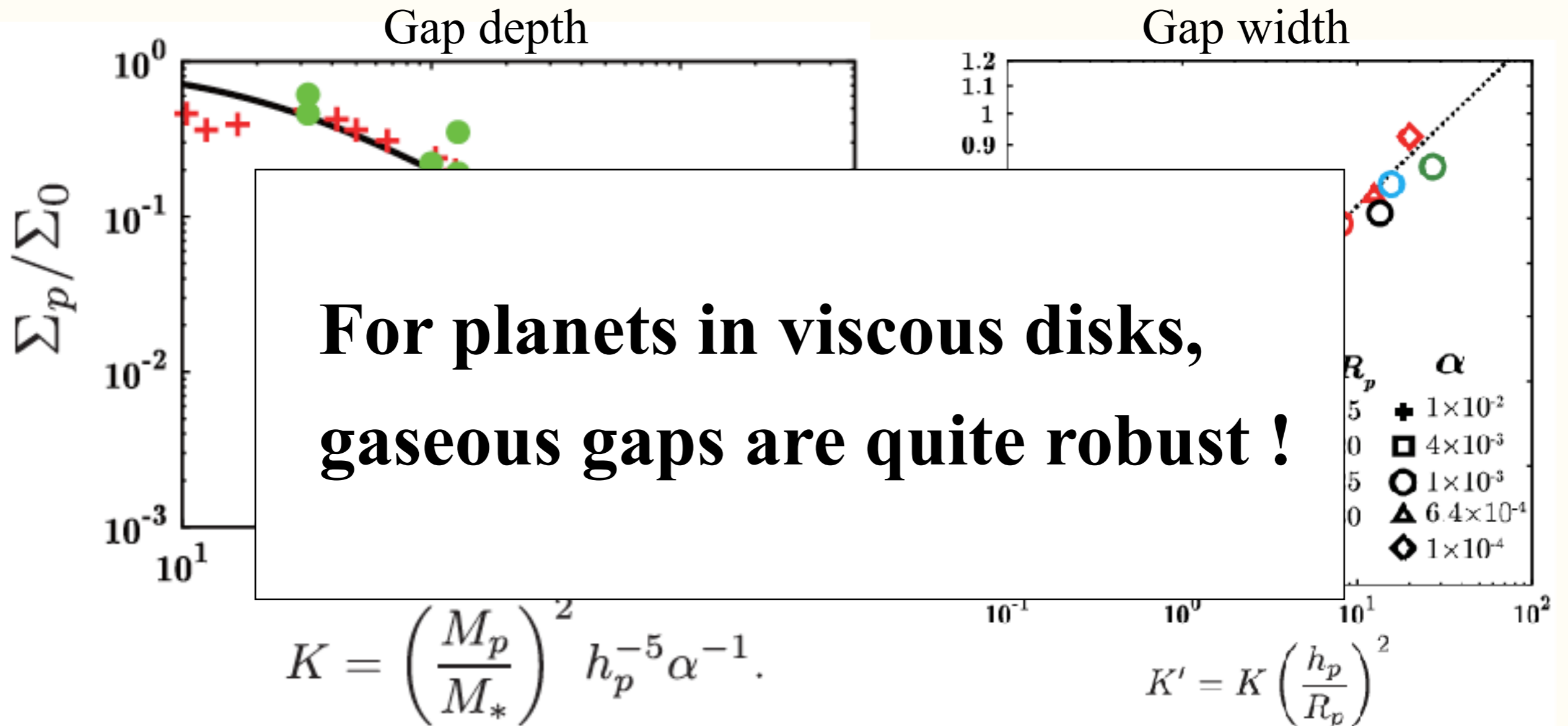
$0.1 M_J$ in $\alpha=0.01$, $H/R=0.05$ disks

Goldreich & Tremaine 1979, Lin & Papaloizou 1986, Crida et al. 2006



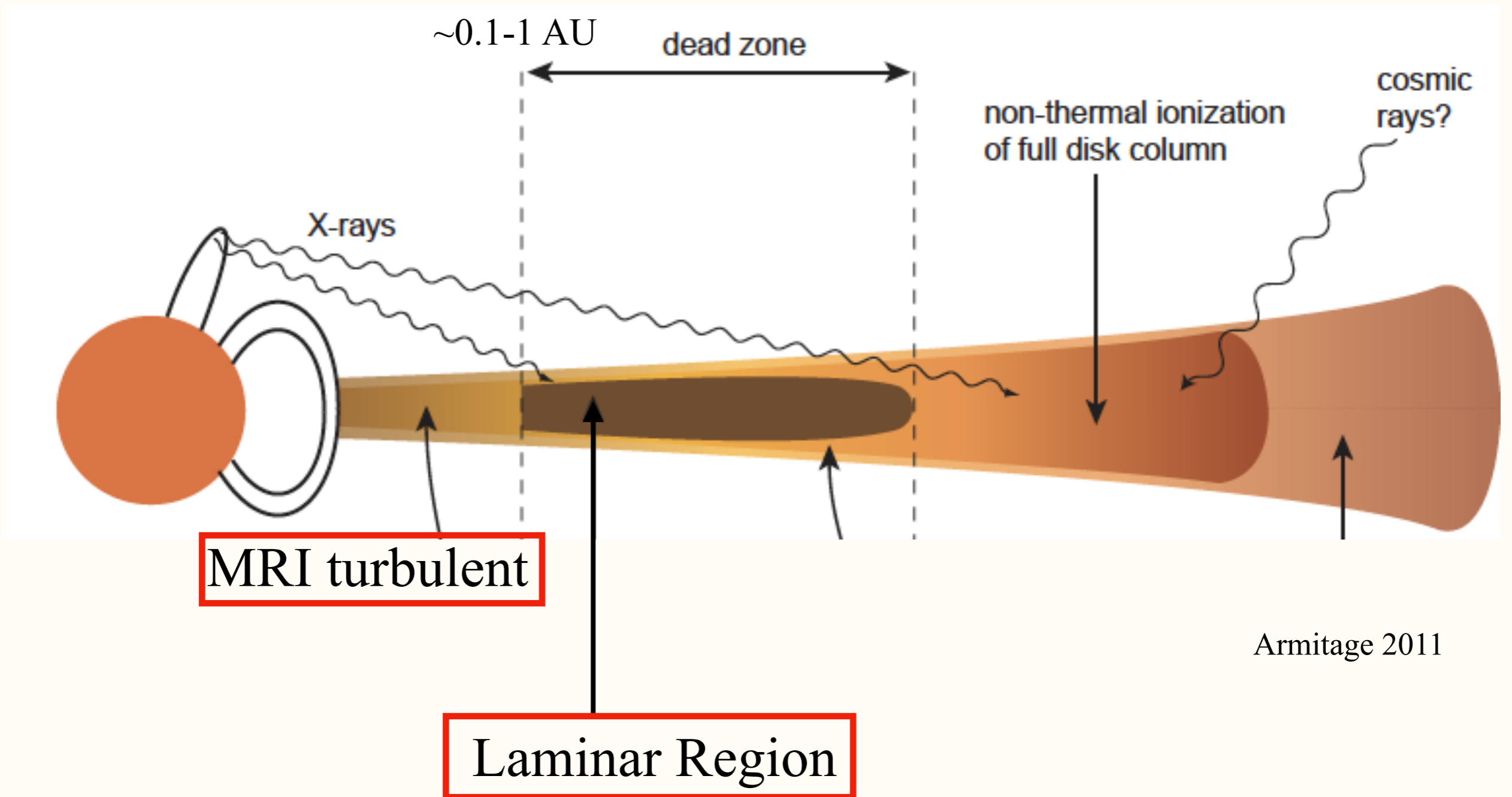
de Val-Borro et al. 2006

Gap opening in viscous disks



Kanagawa+2015, 2016
Ginzburg & Sari 2018

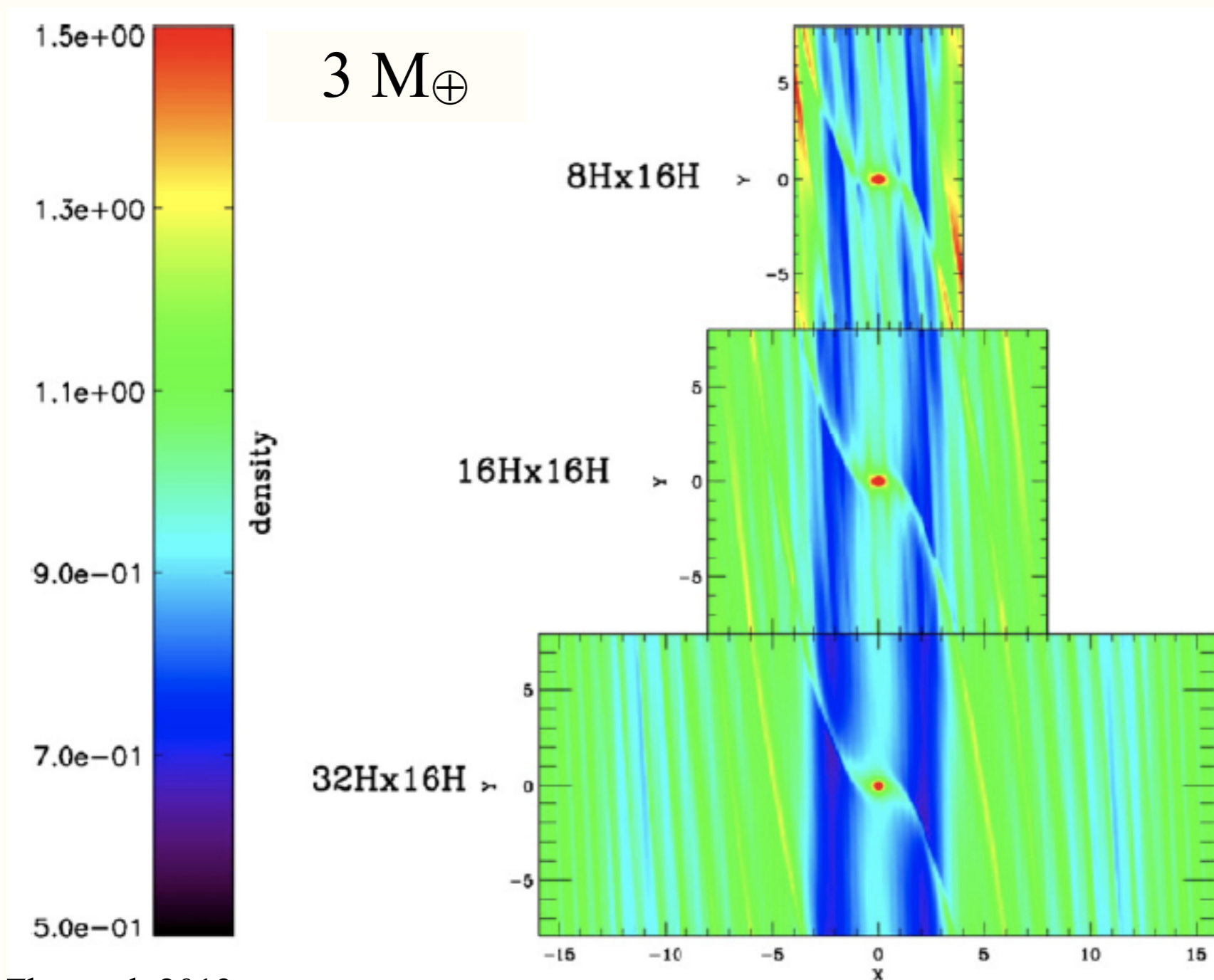
Gap opening in more realistic disks



Gap opening in inviscid disks (“dead zone”)

Gaps can be opened by any mass planets

Goodman & Rafikov 2001, Dong et al. 2009, Muto et al. 2010,
Duffell & MacFadyen 2012, Dong et al. 2017, Bae et al. 2017

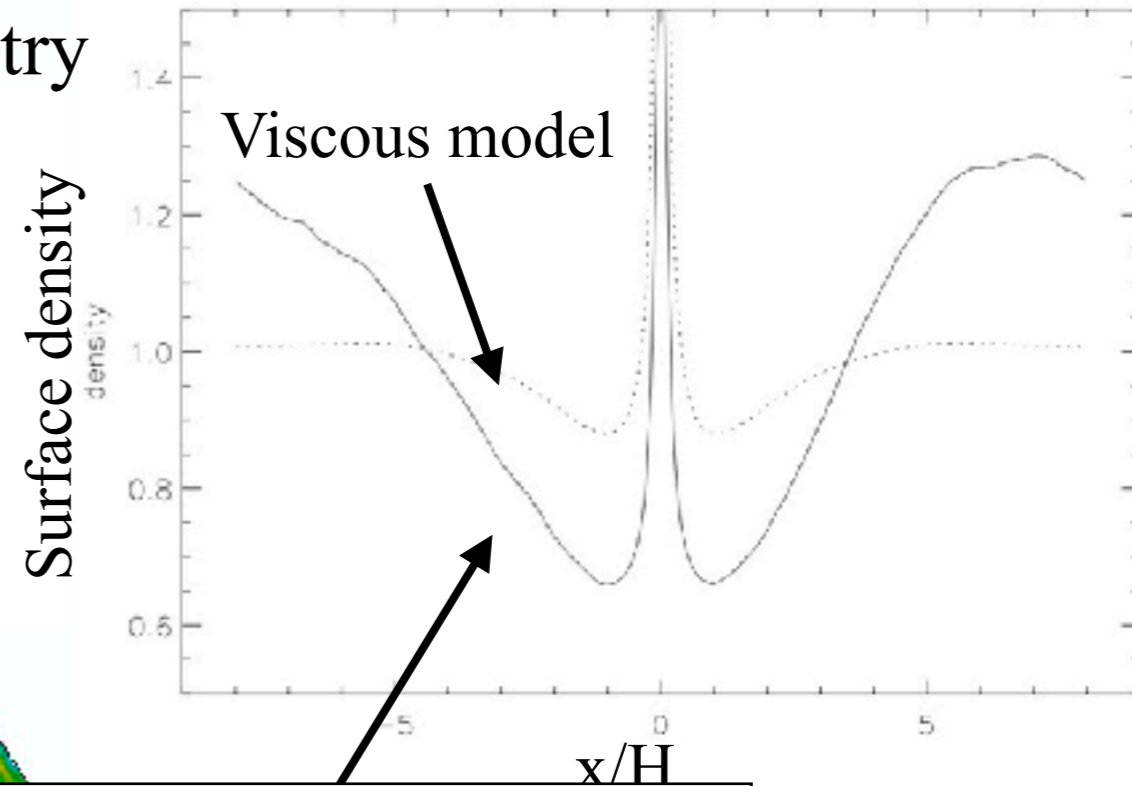
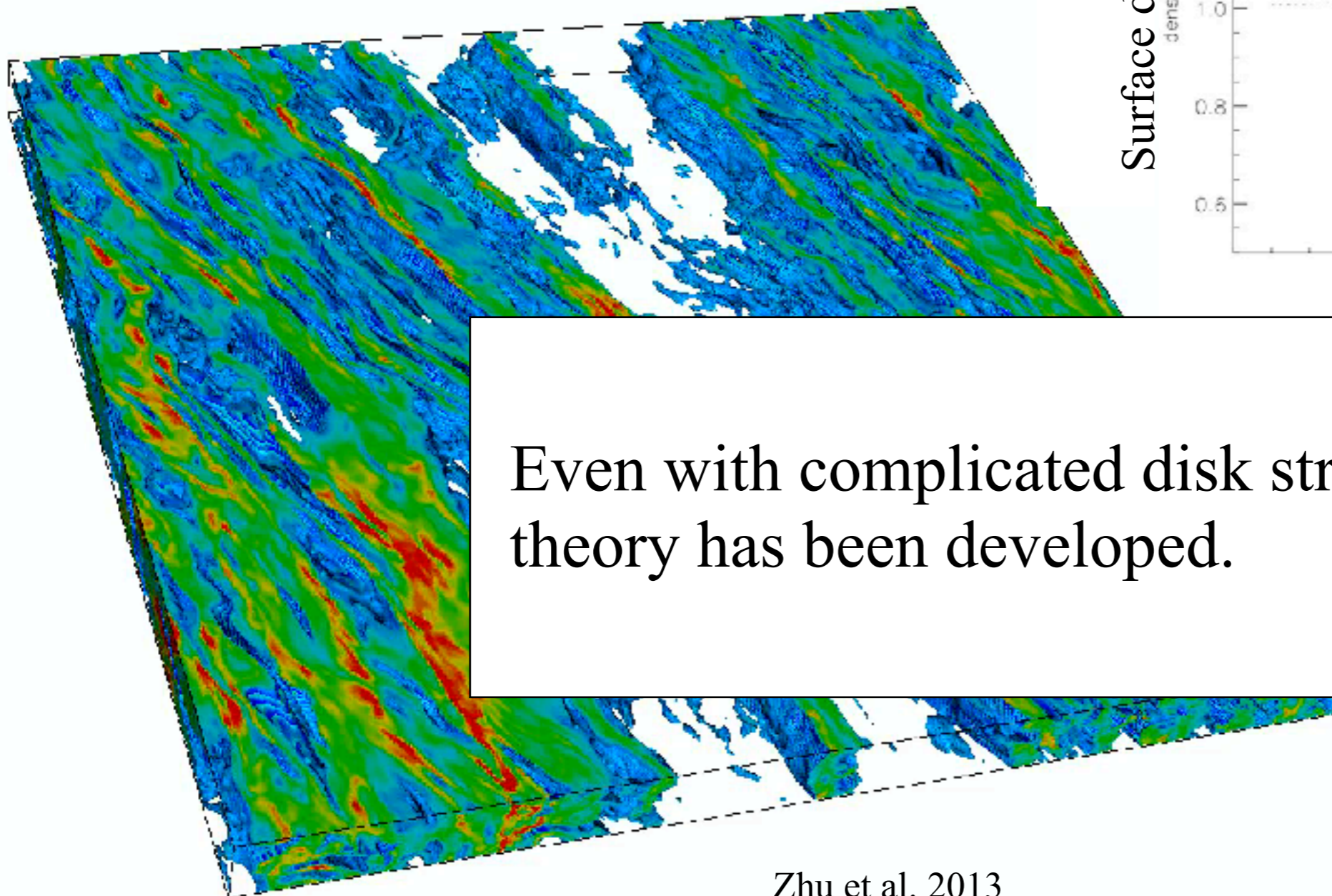


Zhu et al. 2013

Gap opening in turbulent disks

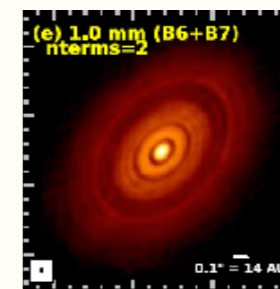
Gap depth depends on magnetic field geometry

Nelson & Papaloizou 2004, Nelson & Gressel 2010



Even with complicated disk structure, theory has been developed.

Gaps/Rings: dust dynamics



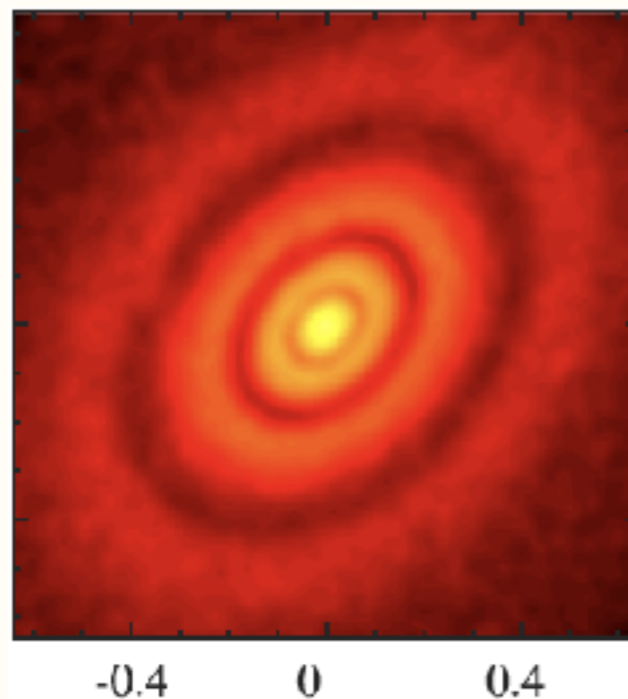
Theory: dust particles drift to gas pressure maximum due to aerodynamic drag

Paardekooper & Mellema 2004, 2006, Rice et al. 2006, Fouchet et al. 2007, Arzuffo et al. 2012, Zhu et al. 2012, 2012, Dipierro & Laibe et al. 2018

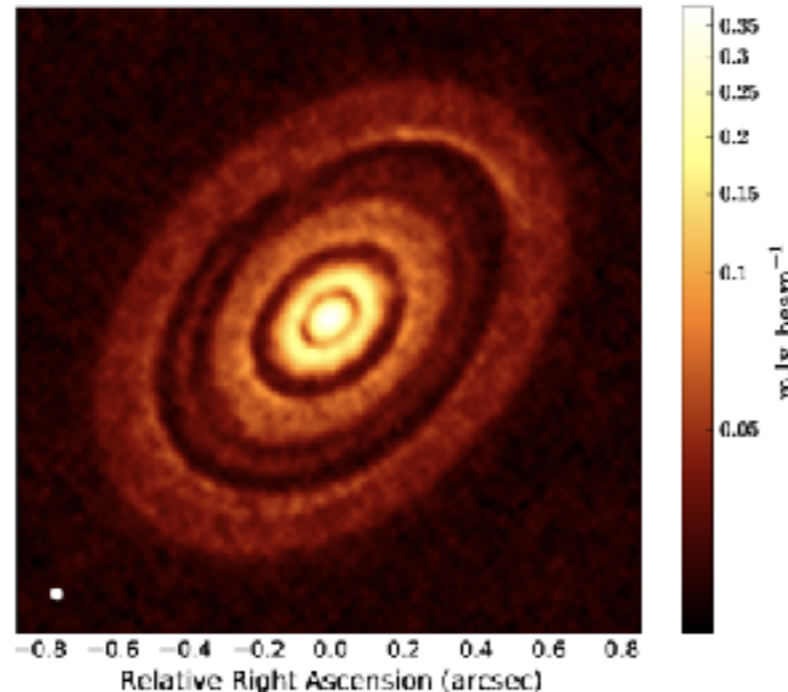
- + Most sensitive indirect method (M_{\oplus})
- Other ways to make gaps/rings
- Even it is by planets, huge degeneracy

Observations

with MCRT:



Dong et al. 2015



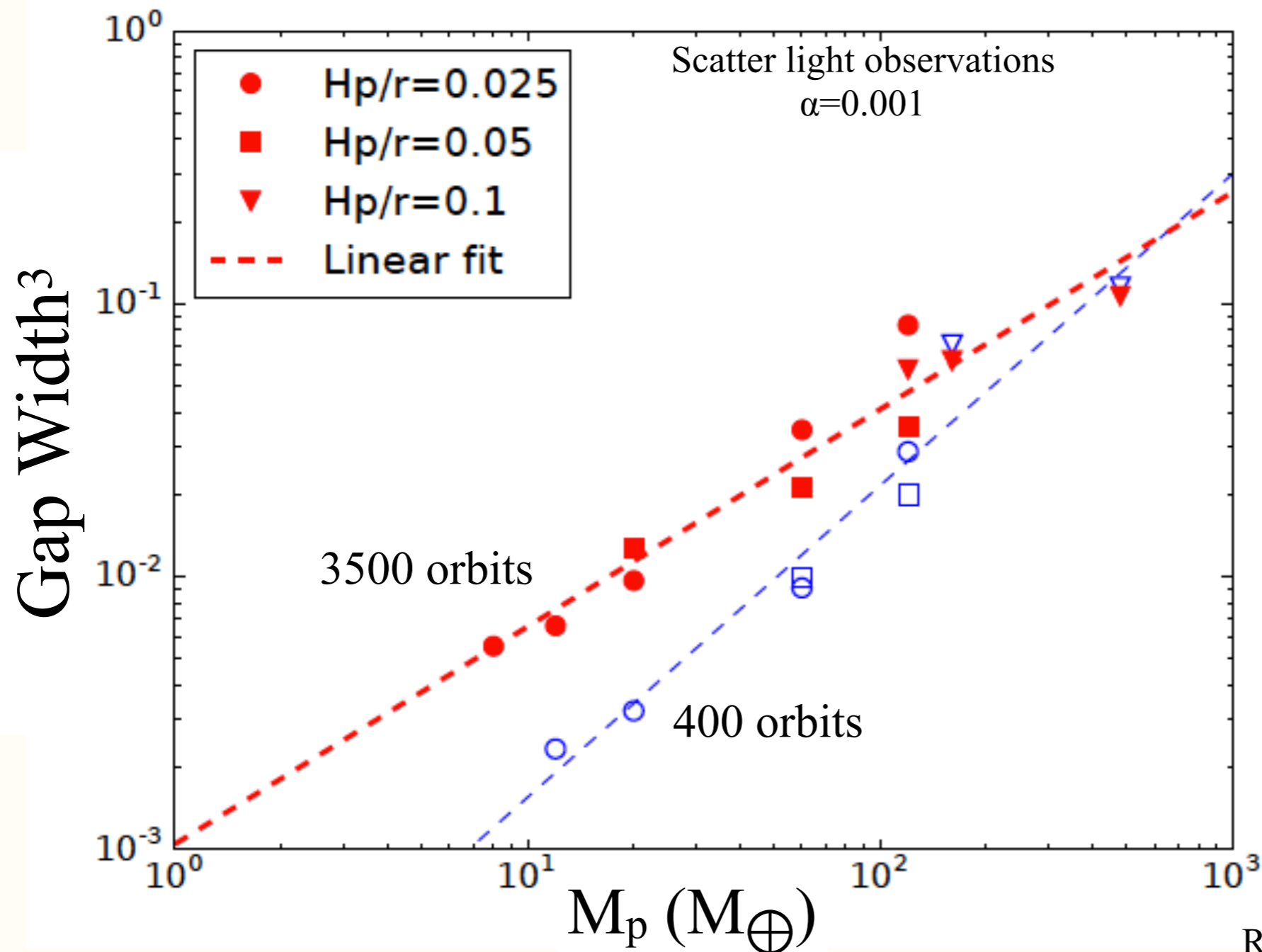
Dipierro et al. 2016

De Juan Ovelar et al. 2013, Garufi et al. 2013, Dong et al. 2013, Benisty et al. 2015, Picogna & Kley 2015, Dipierro et al. 2016, Dong & Fung 2017, Hornbeck et al. 2018, Boehler et al. 2018

0.2, 0.27, 0.55 M_J

Gaps/Rings: degeneracy

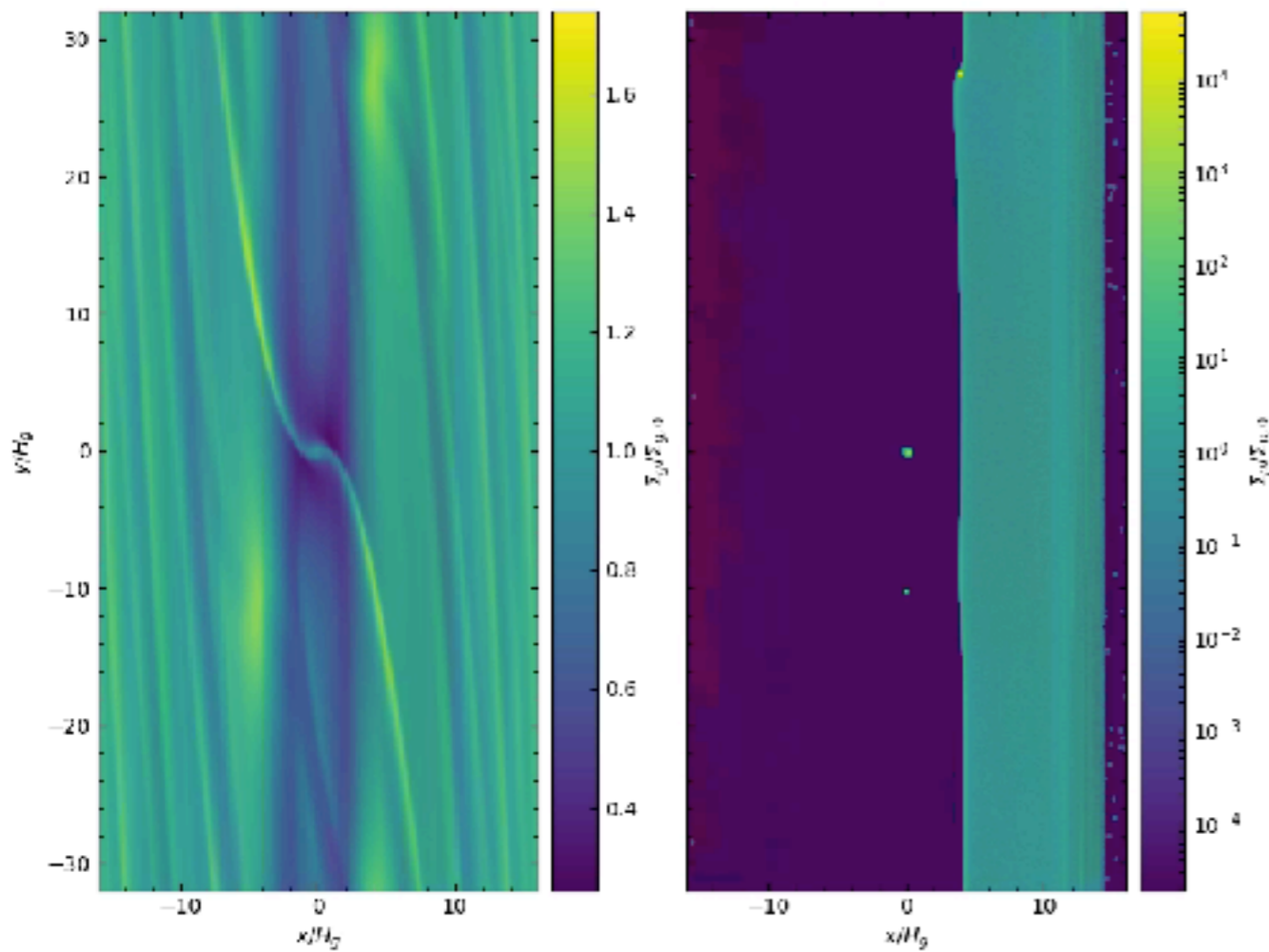
- Uncertain particle size distribution
- Time dependent



Gaps/Rings: including dust's back reaction to gas

No back-reaction

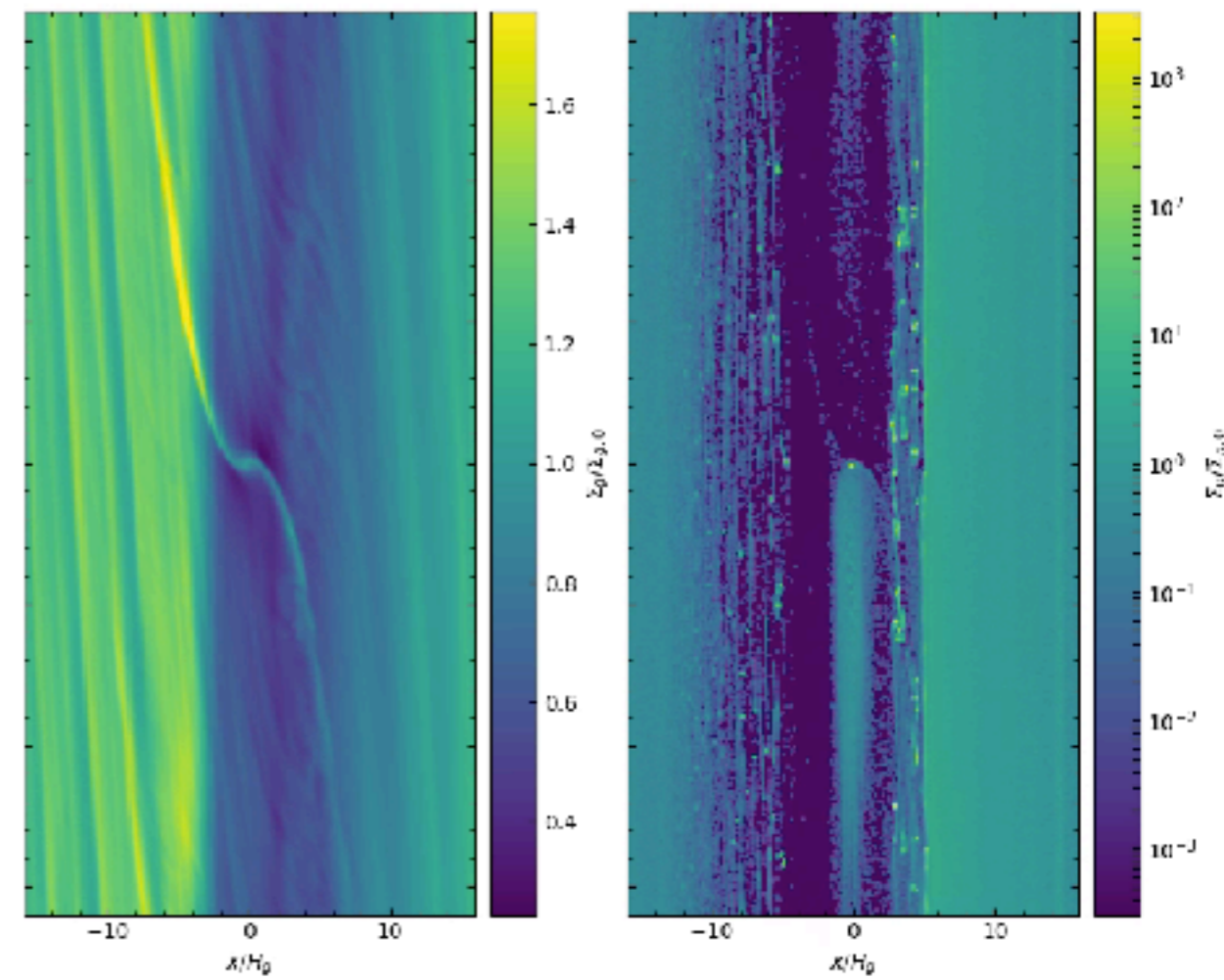
$\Pi = 0.05$ --- $M_p = 1M_{\text{Jup}}$ --- $\tau_s = 10^0$ (no back reaction) --- $8\lambda_g H_g^{-1}$



$t/P = 72.00$

Z=0.3 back-reaction

$\Pi = 0.05$ --- $M_p = 1M_{\text{Jup}}$ --- $\tau_s = 10^0$ --- $Z = 0.3$ --- $8\lambda_g H_g^{-1}$

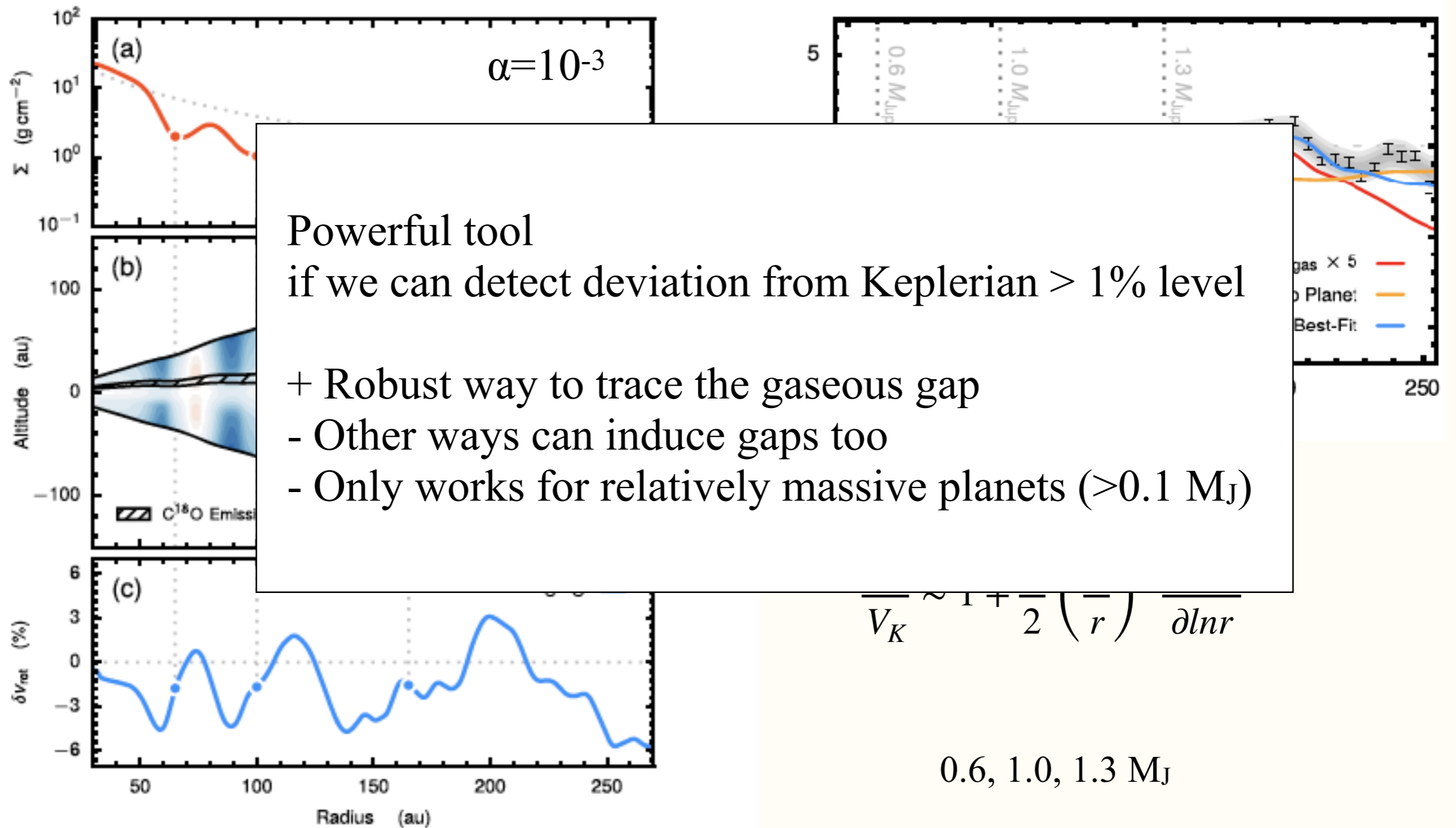


$t/P = 72.40$

- Particle filtration efficiency is significantly reduced.
- Gas is accumulated at the inner gap edge.

Yang & Zhu in prep.

Gaps/Rings: gas dynamics



Outline

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Synergy between Near-IR and Submm

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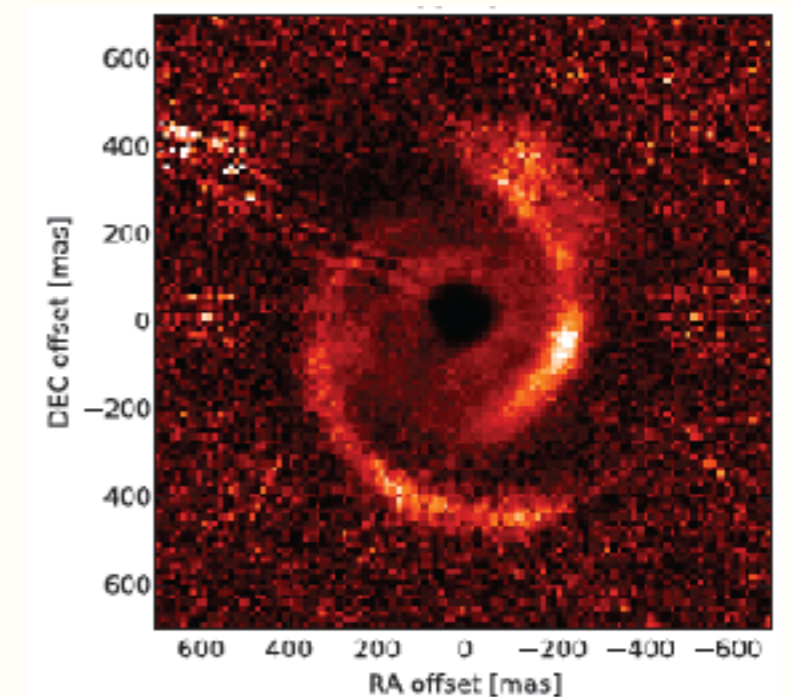
Gaps/rings

Spirals (theory, test theory, spirals lead to gaps)

Lopsided structures

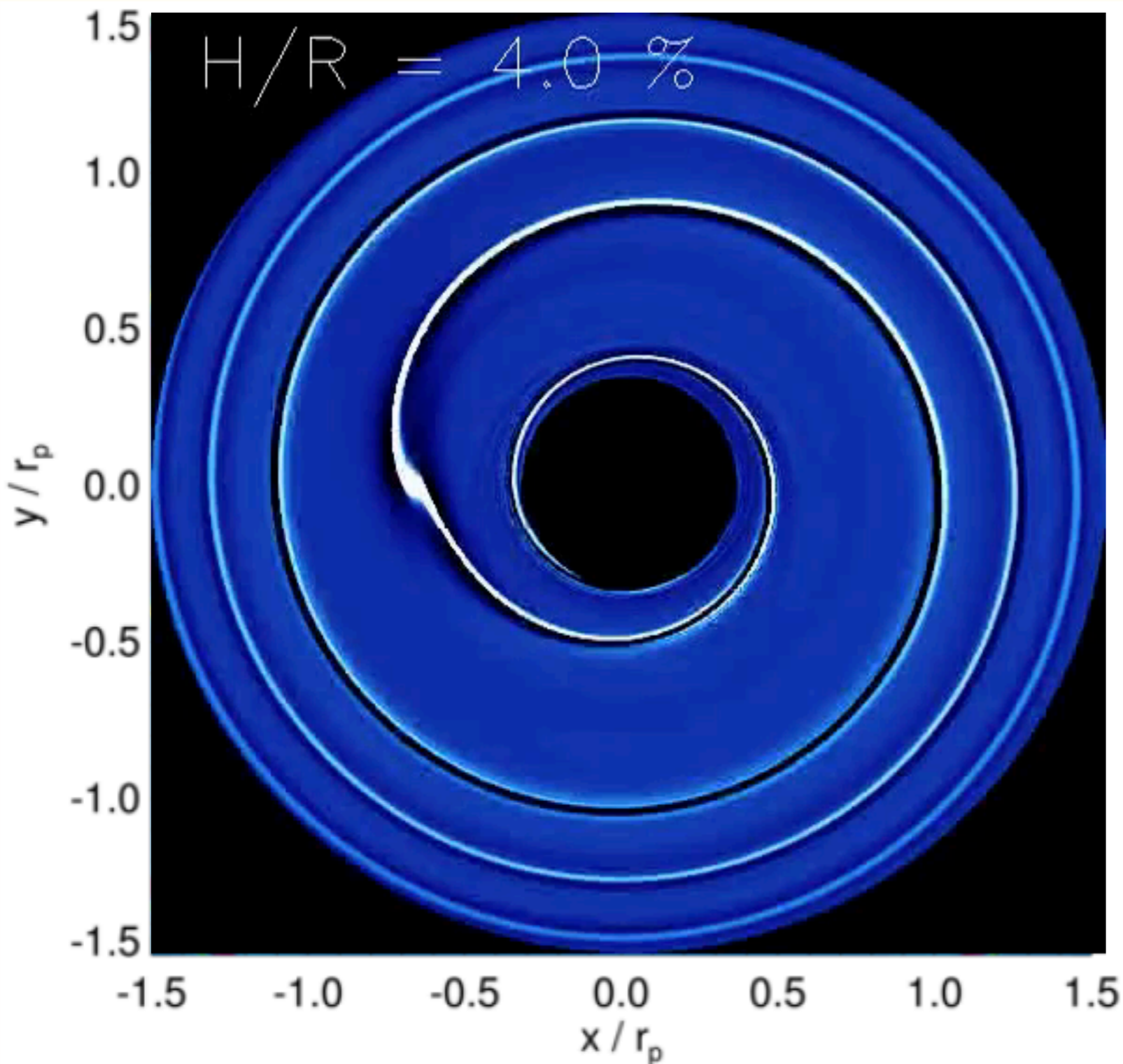
Shadows

CPDs



Benisty+ 2015

Sound waves in disks



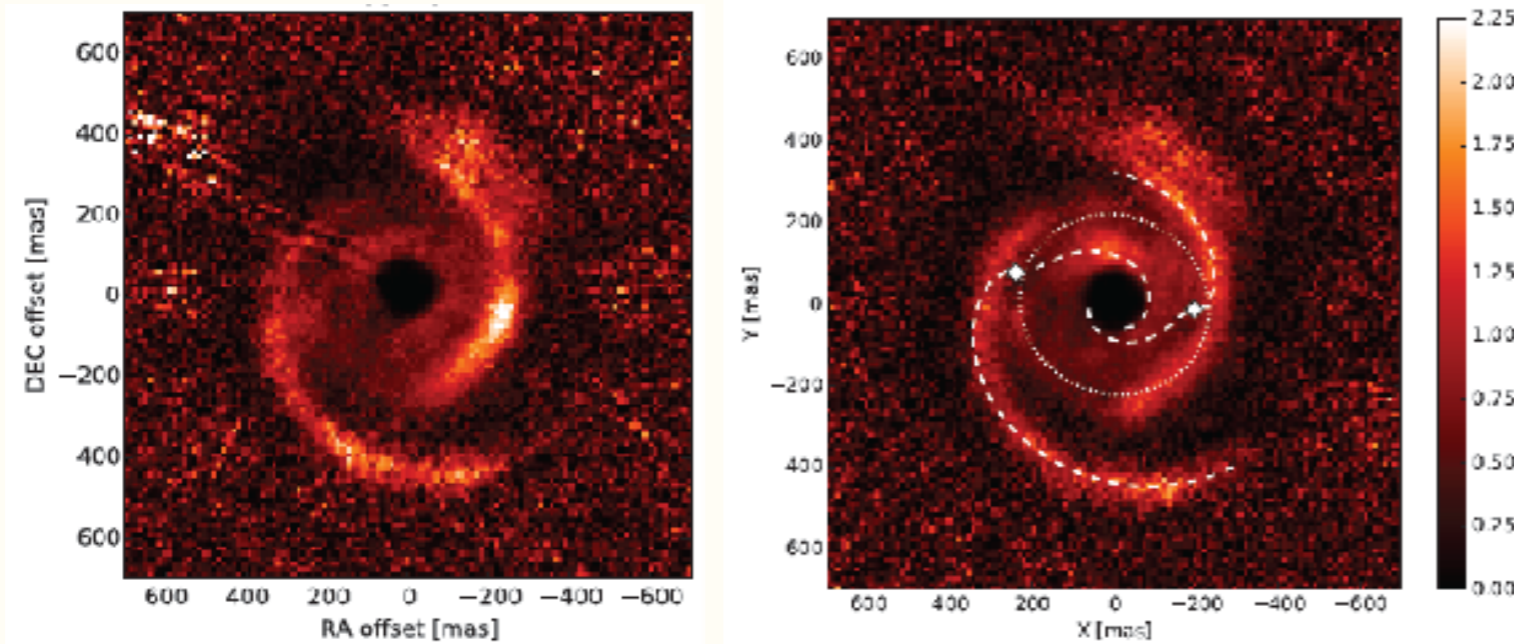
The pitch angle β

$$\tan \beta = \frac{c_s}{R |\Omega - \Omega_p|}$$

Explaining observations is difficult

1. Fitting the pitch angle suggests a too hot disk

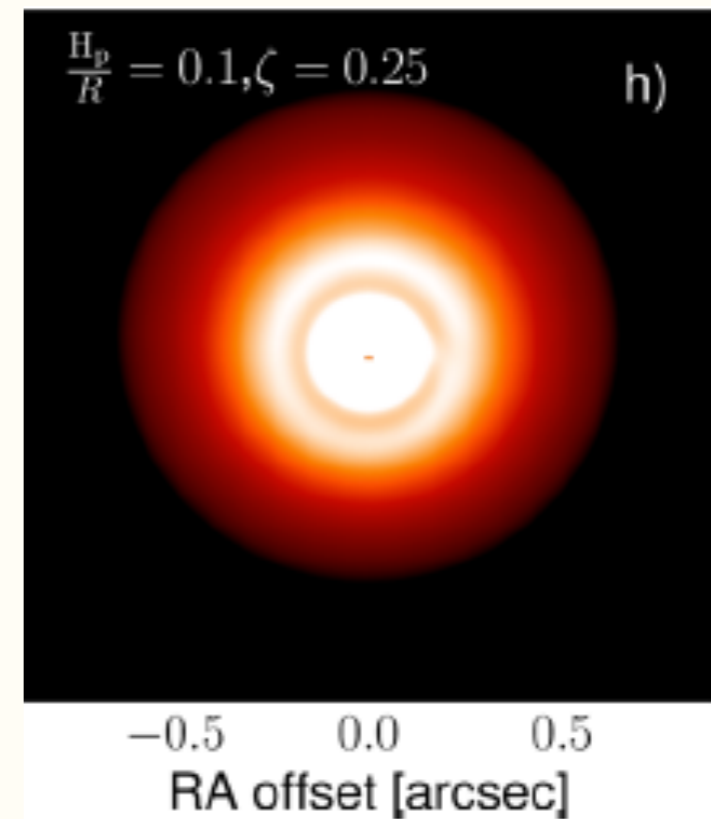
MWC 758



At 50 AU, $T \sim 300$ K

Benisty et al. 2015

2. Planet-induced spiral arms are too weak



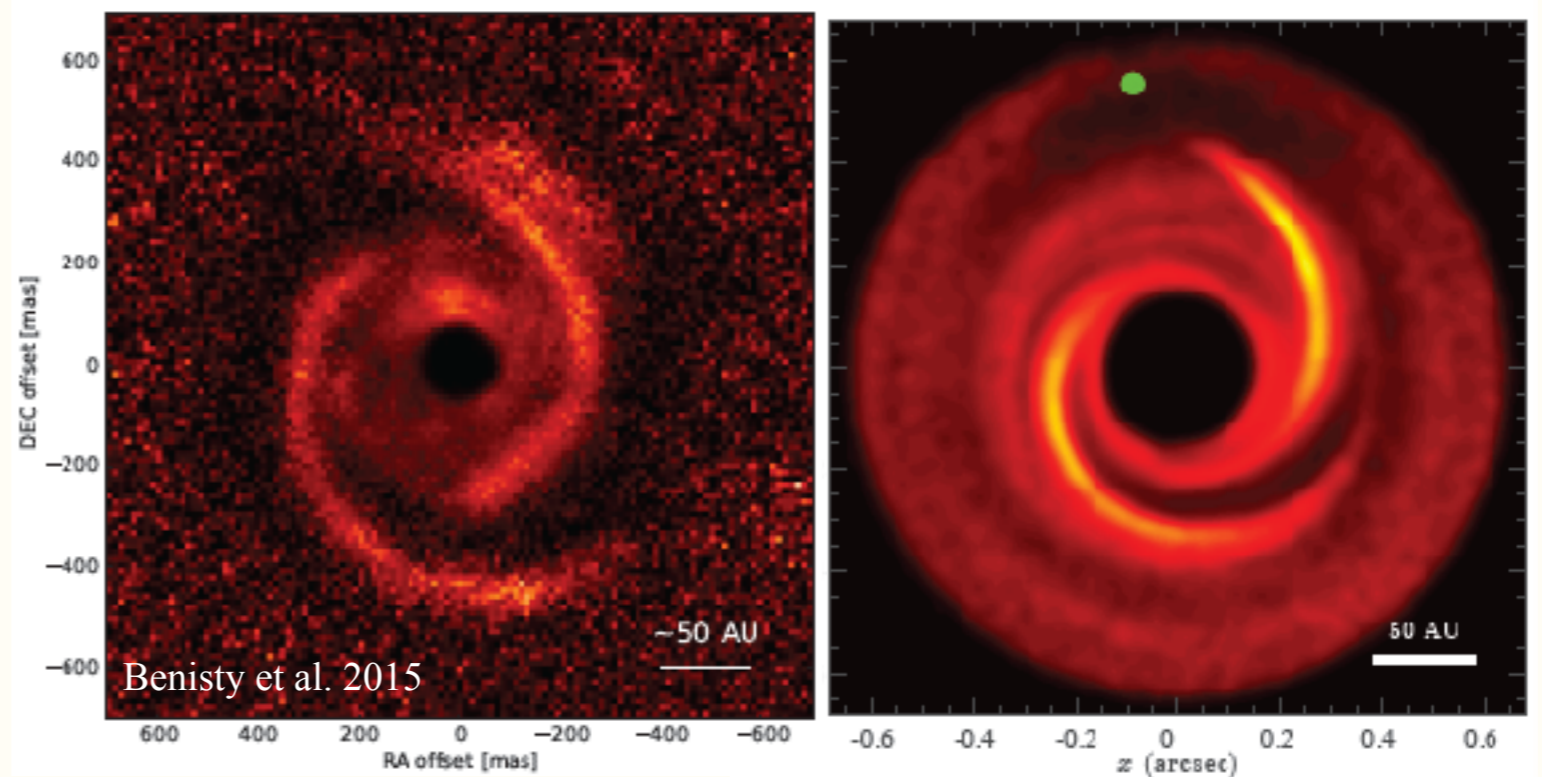
Juhász et al. 2015

Spirals: Grand design

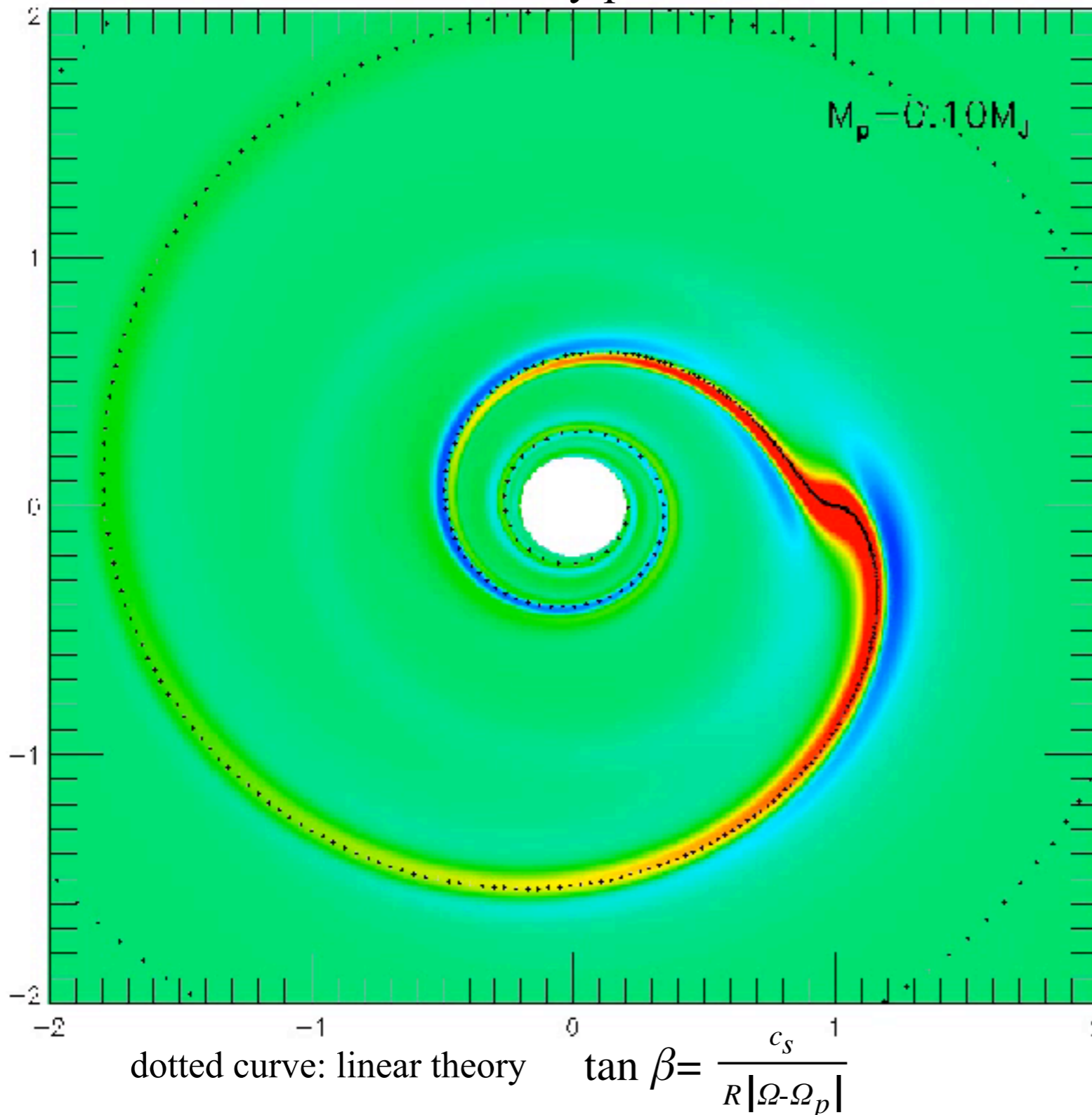


M51

What if the planet is outside the spirals?
(Dong et al. 2015, Zhu et al. 2015)



Surface density perturbation



When the planet mass increases:

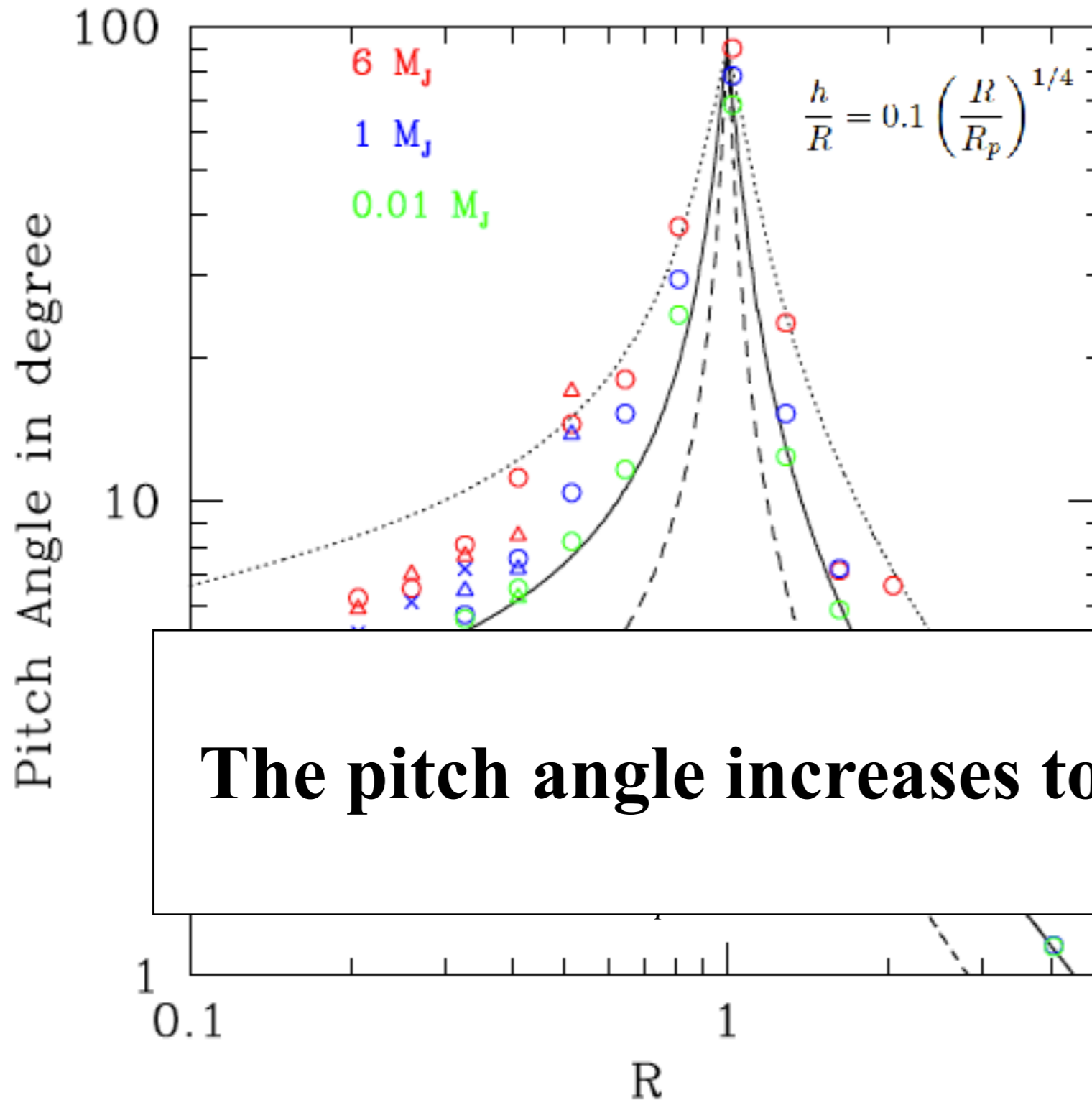
- The **pitch angle** increases
- The secondary arm becomes apparent and the **separation** between two arms increases
- **Amplitude** of shocks becomes larger



Use spiral arms to estimate planet mass

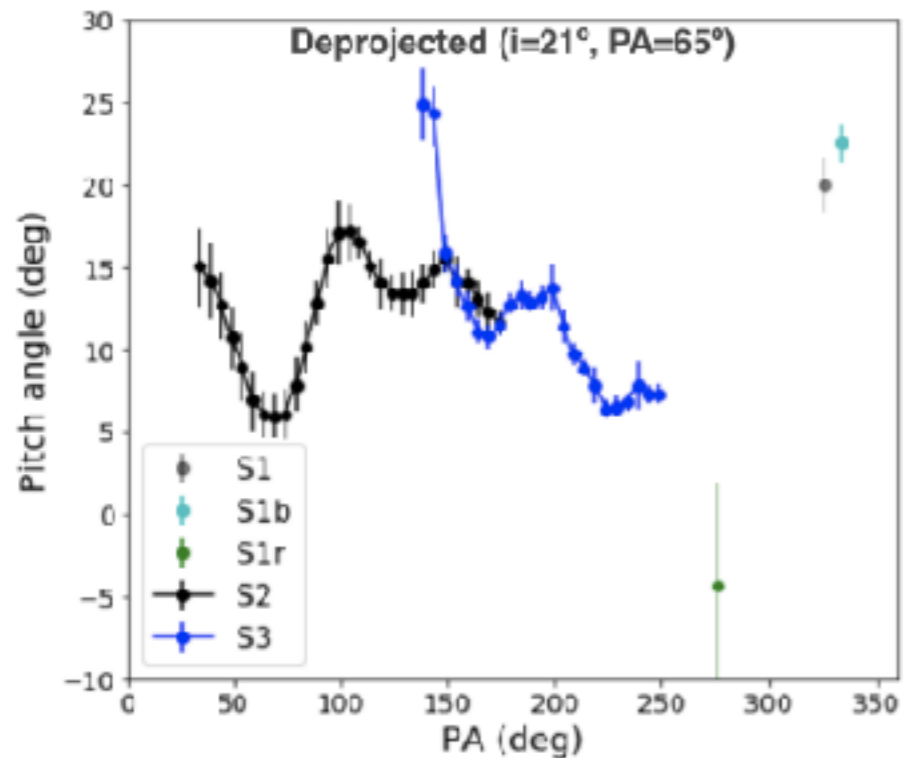
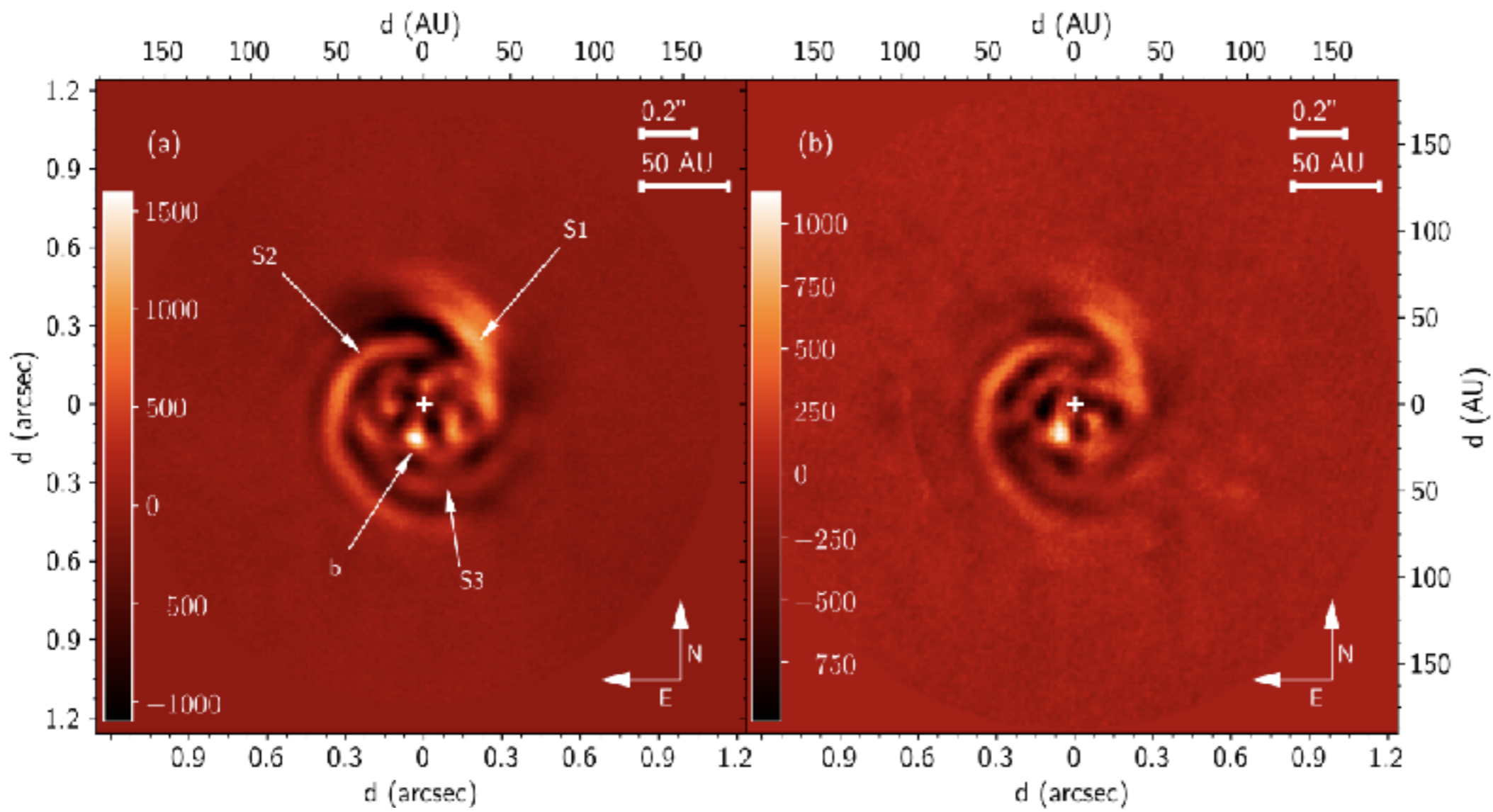
Zhu et al. 2015

Spirals: pitch angle



The pitch angle increases towards the planet

New Observations: Reggiani+ 2017

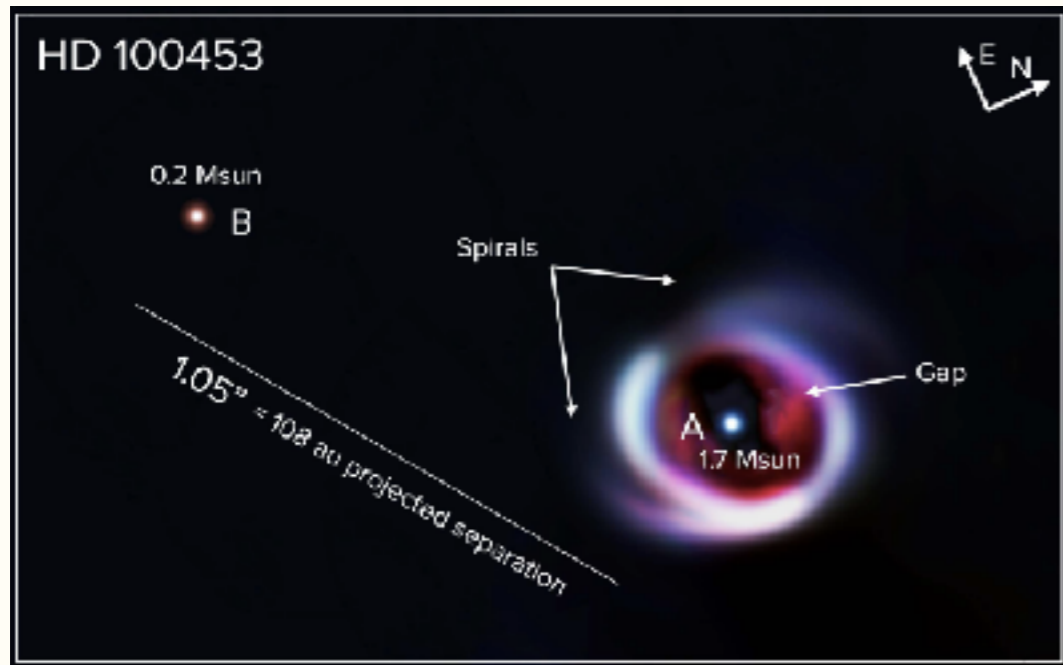


New developments:

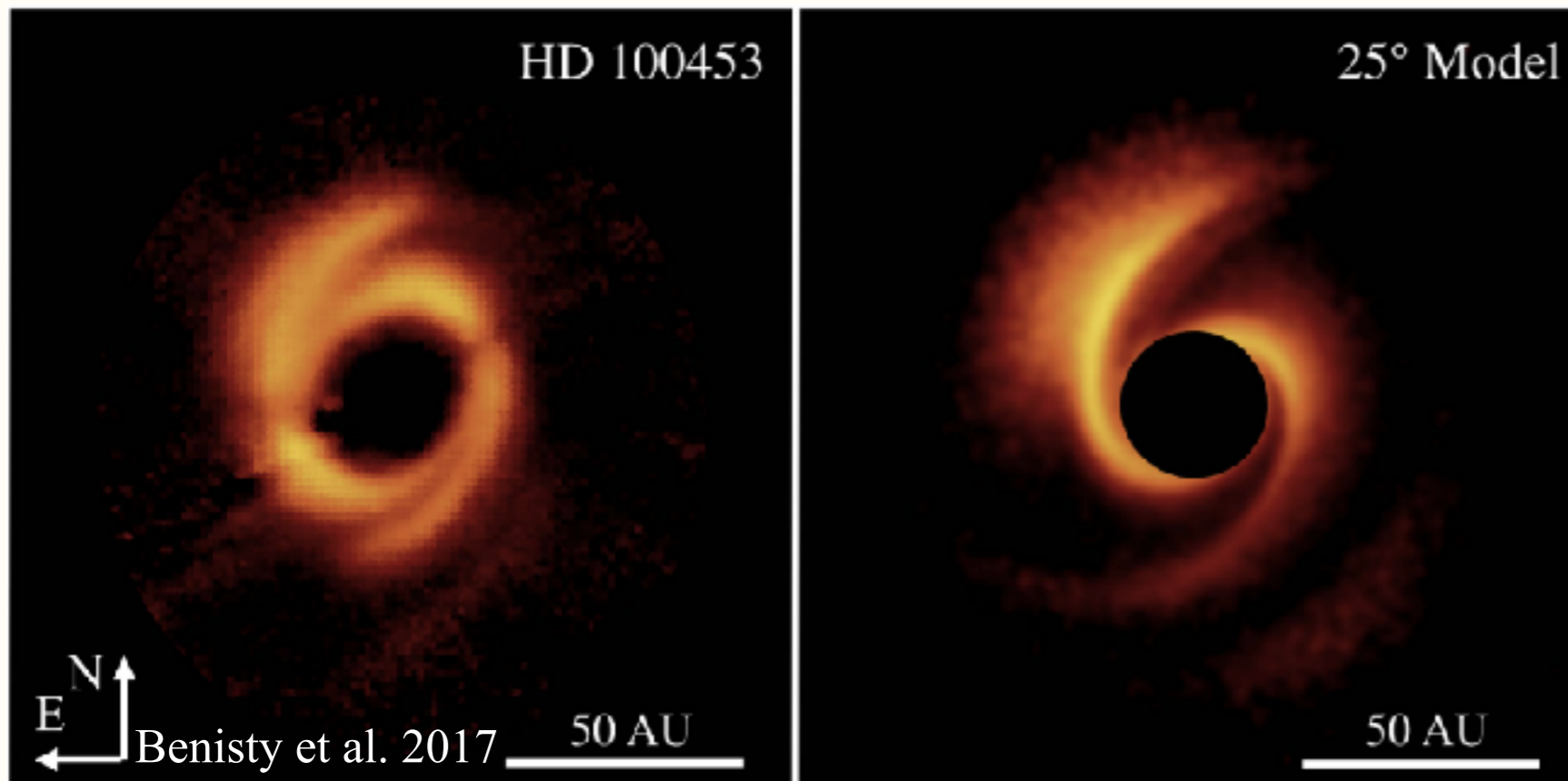
Fung & Dong 2015, Lyra et al. 2016, Bae et al. 2016ab, Dong & Fung 2017, Hord et al. 2017, Juhasz & Rosotti 2018

How to test the theory?

1. Use binaries as a test



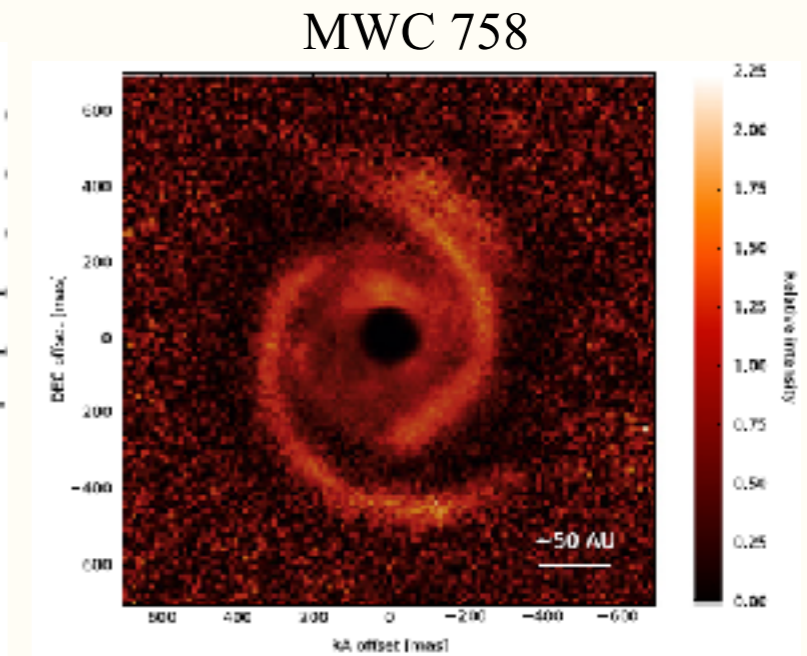
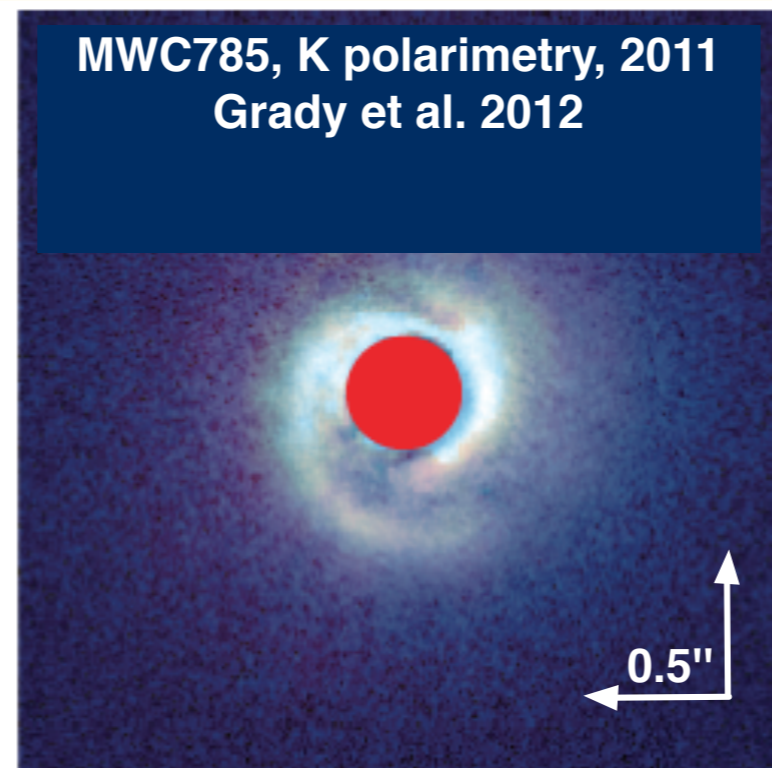
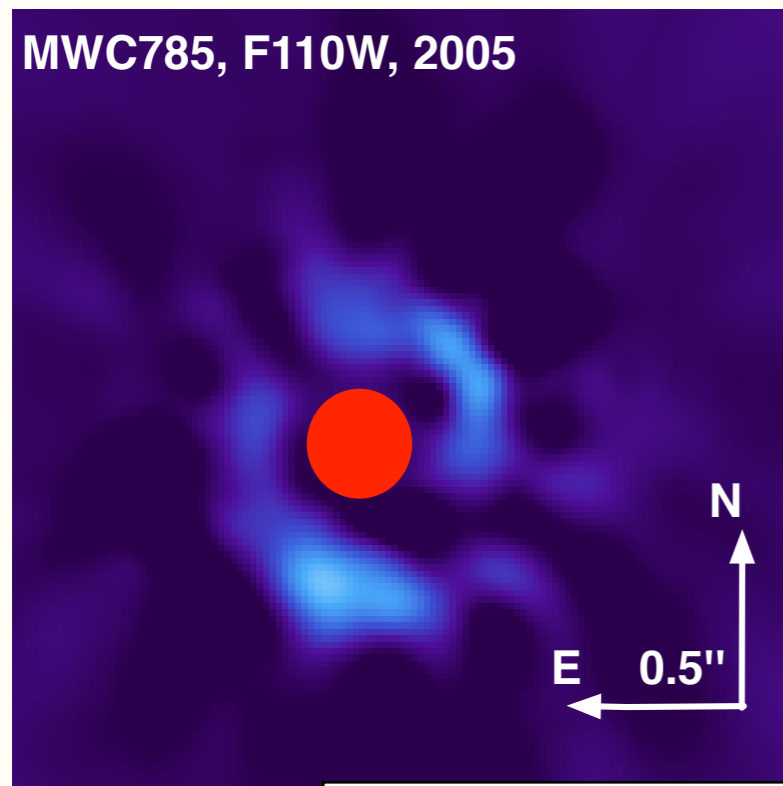
Wagner et al. 2015



Wagner et al. 2018

How to test the theory?

2. Spiral Patterns over Time

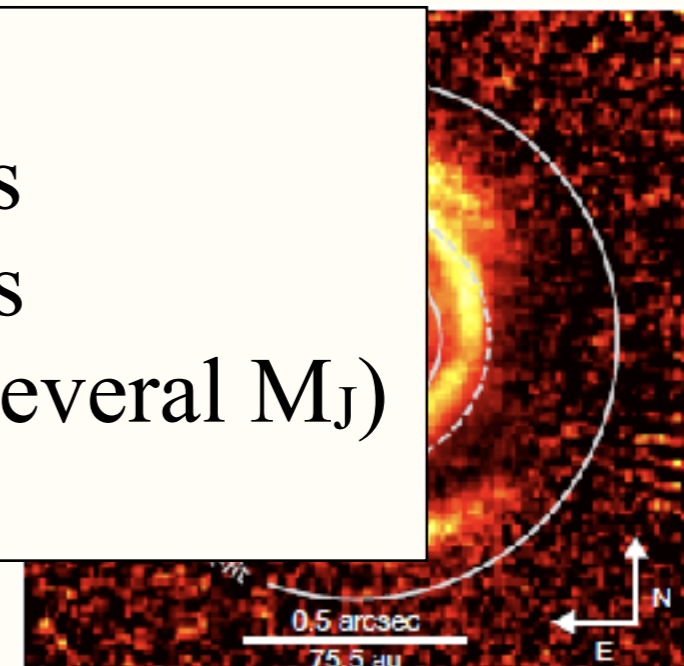


VLT Observations
by Benisty et al. 2015

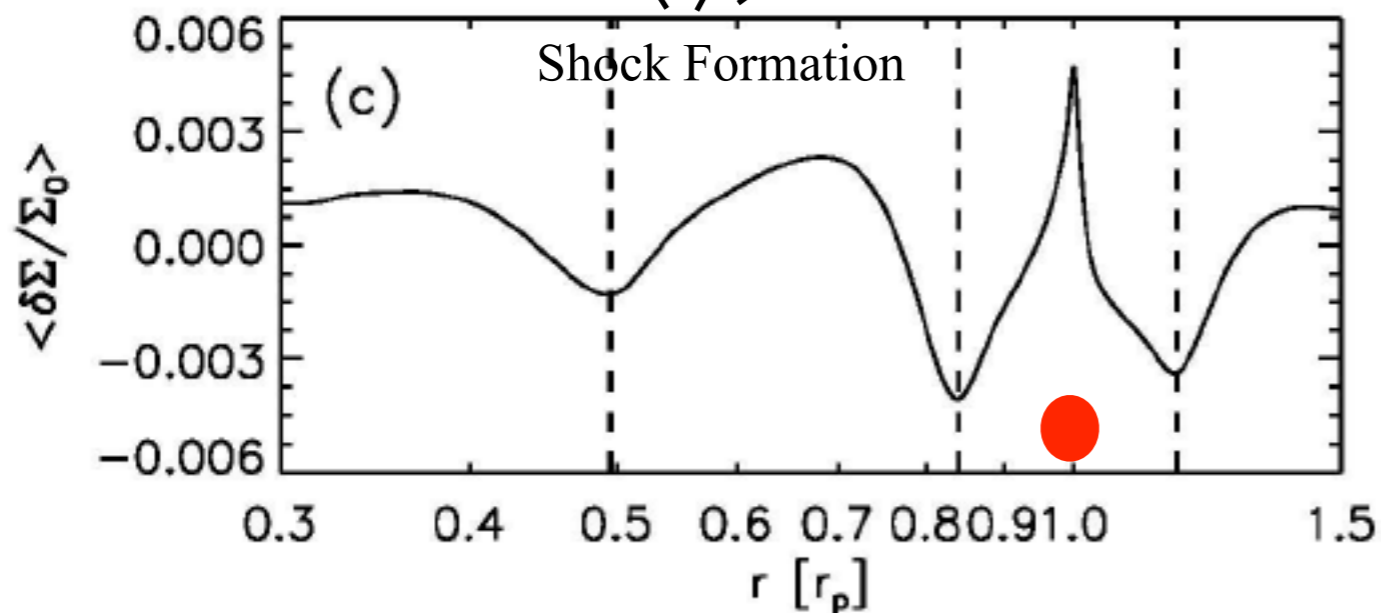
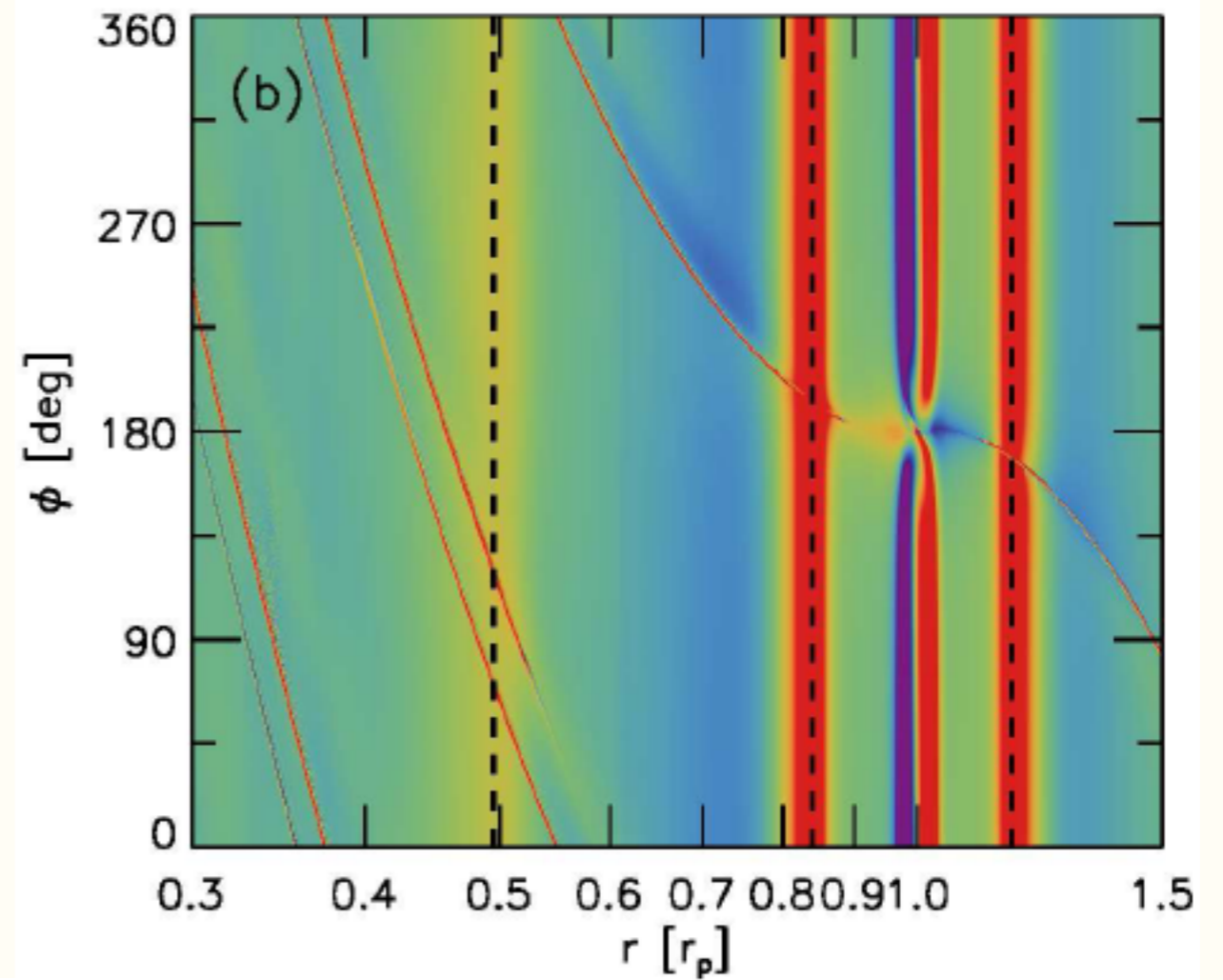
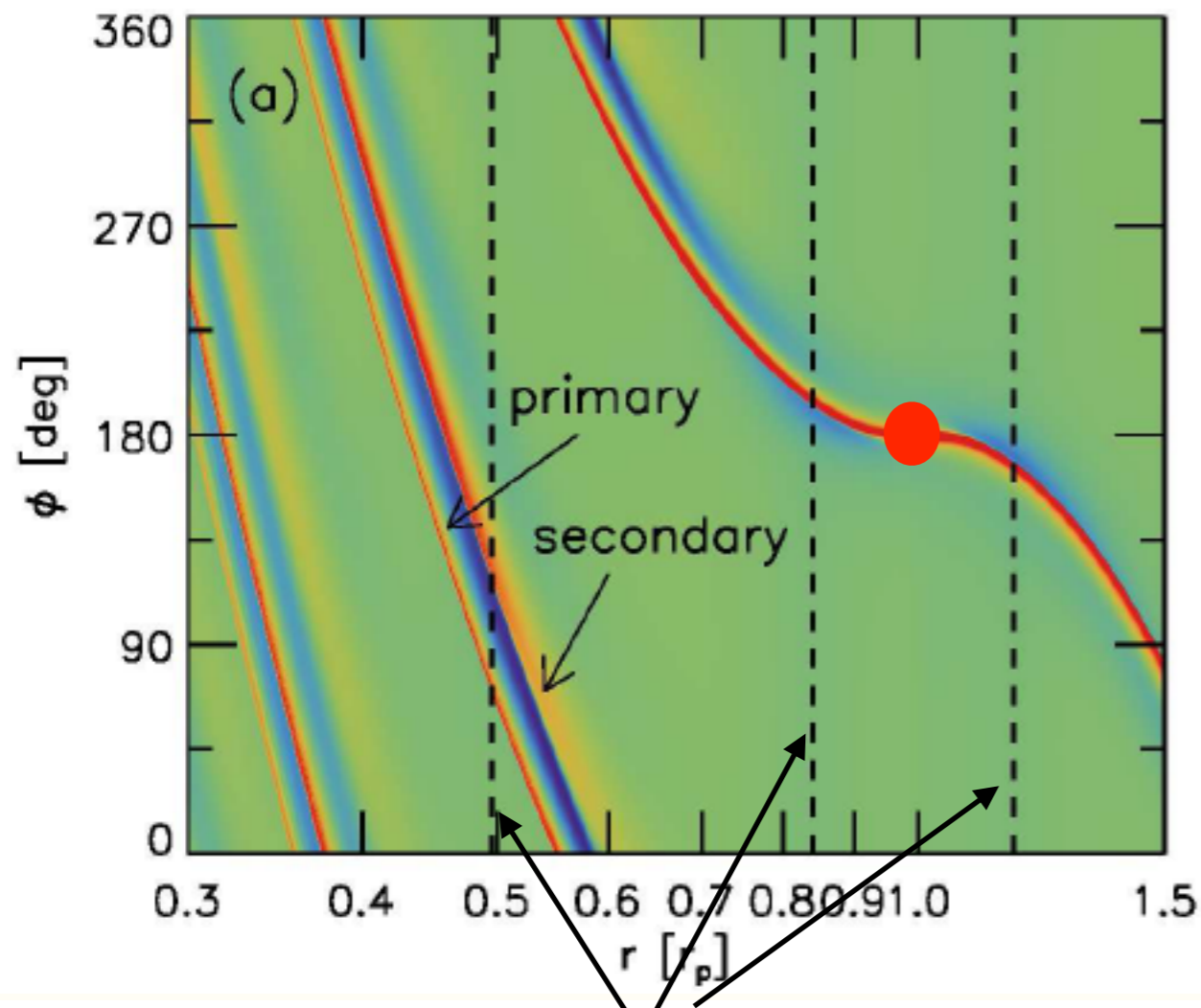
2005 Hubble

Planets
Planets

- + Can trace planet position and mass
- + Not many other ways to get spirals
- Only works for massive planets (several M_J)



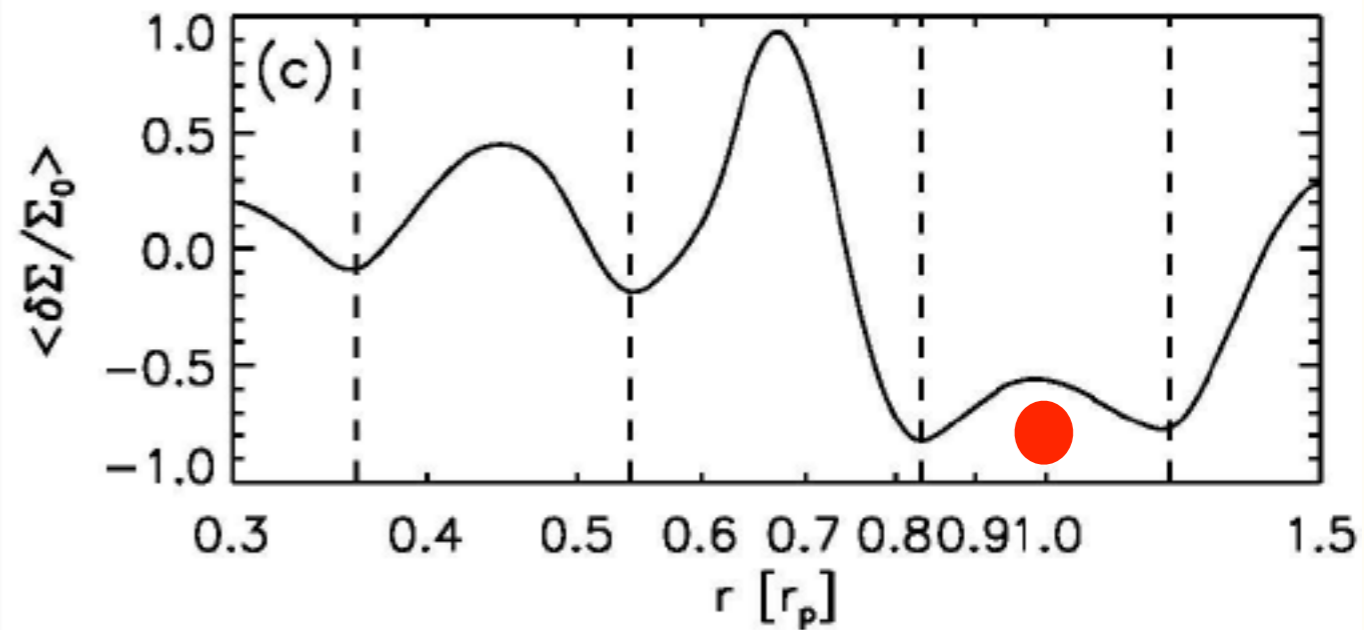
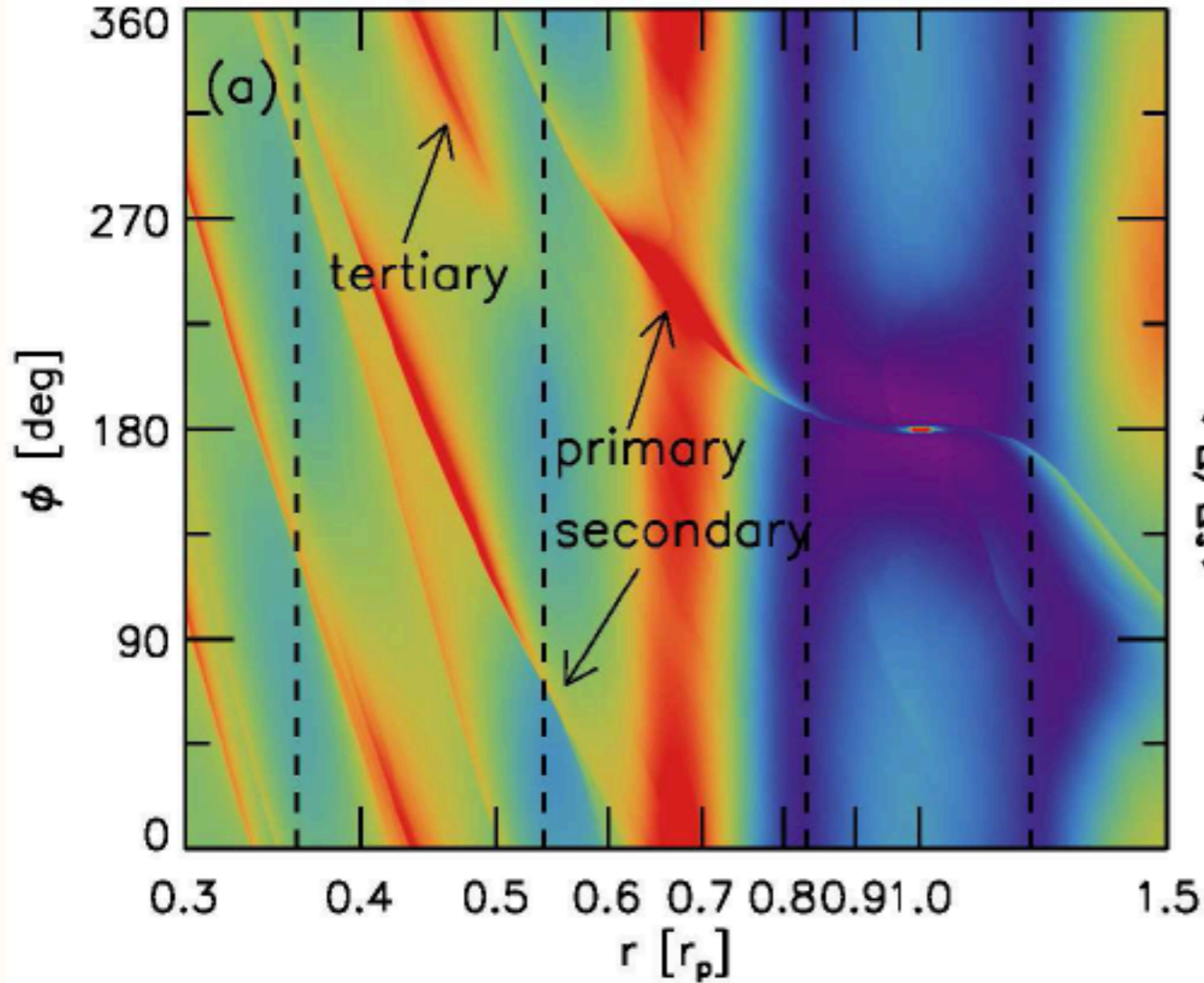
Multiple spirals with multiple gaps



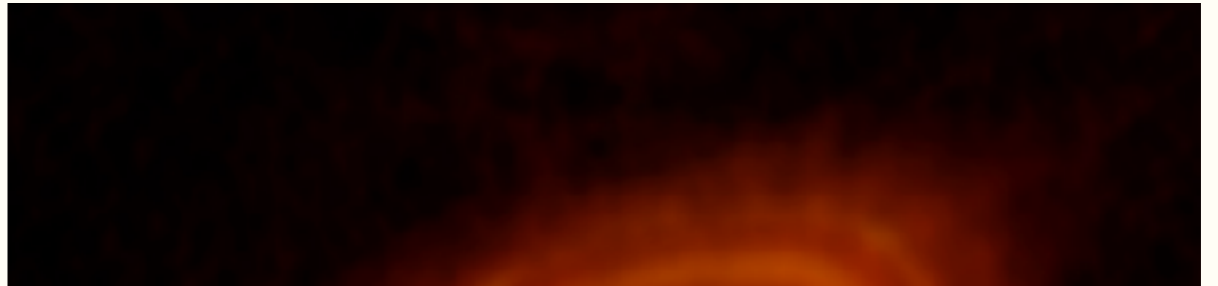
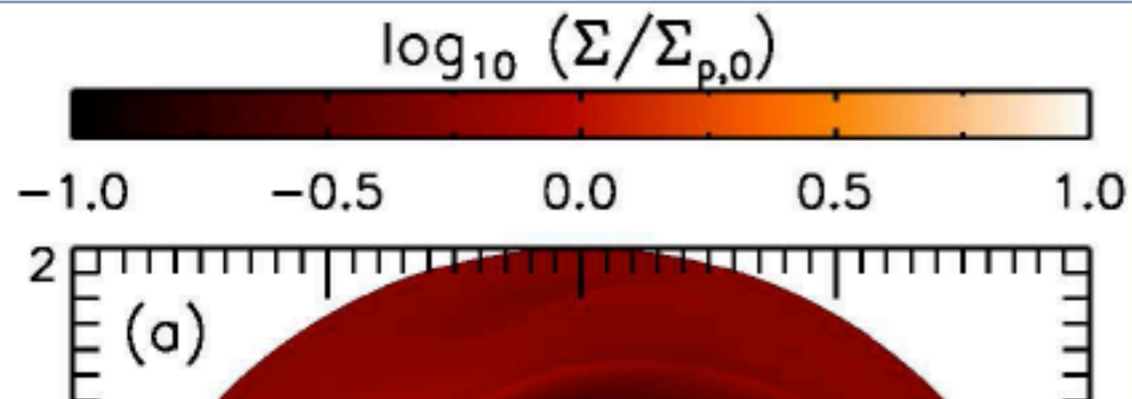
Potential Vortensity:

$$\zeta \equiv \frac{\nabla \times \mathbf{v}}{\Sigma}$$

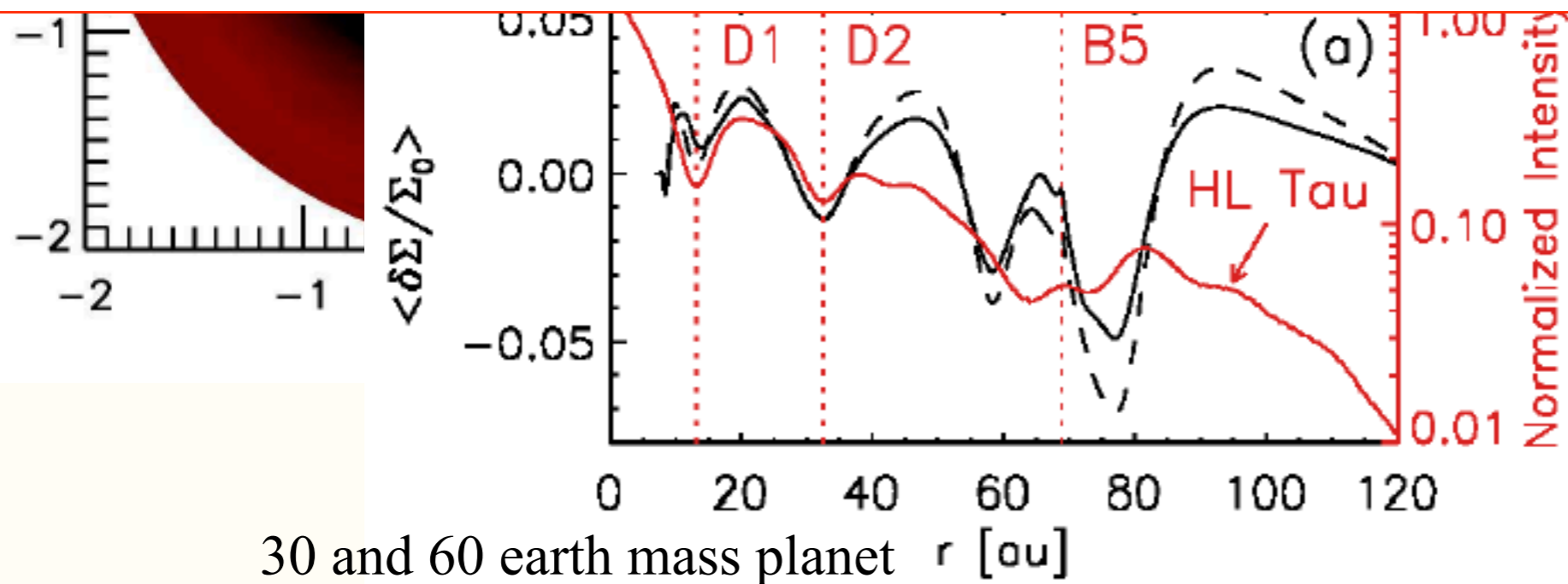
Each spiral can open its own gap



Multiple gaps by one planet



- A planet can open multiple gaps
- We can use gap position to estimate the planet mass (degeneracy with the temperature structure)



Bae, Zhu, Hartmann 2017
Dong et al. 2017

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Synergy between Near-IR and Submm

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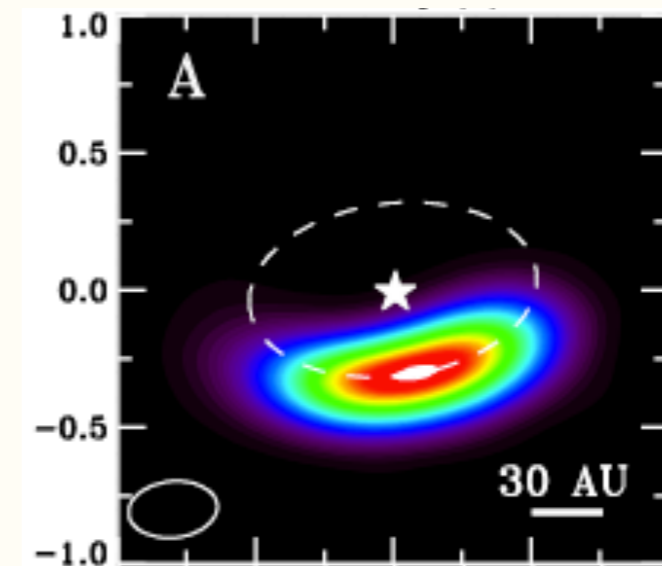
Gaps/rings

Spirals

Lopsided structures (theory, test theory, spirals lead to gaps)

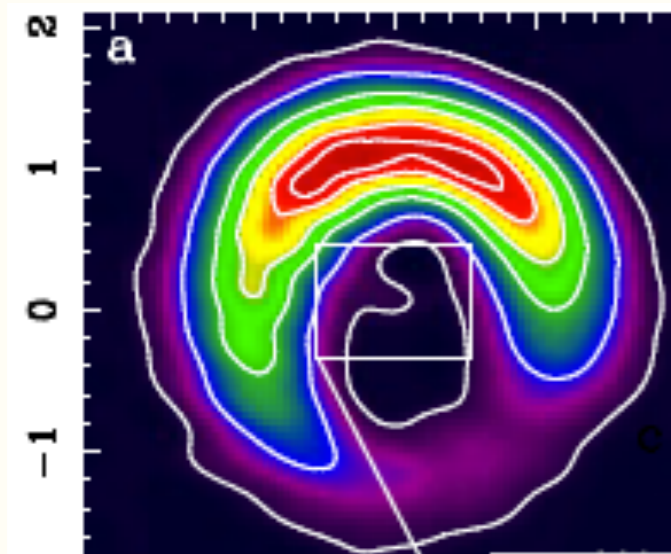
Shadows

CPDs

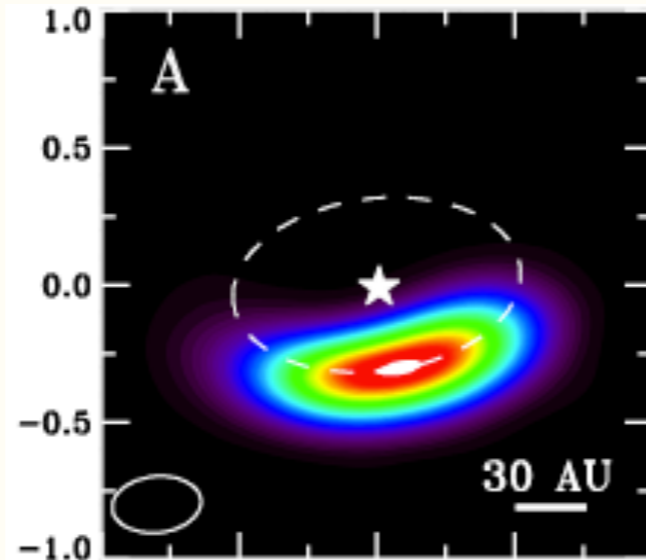


van der Marel+ (2013)

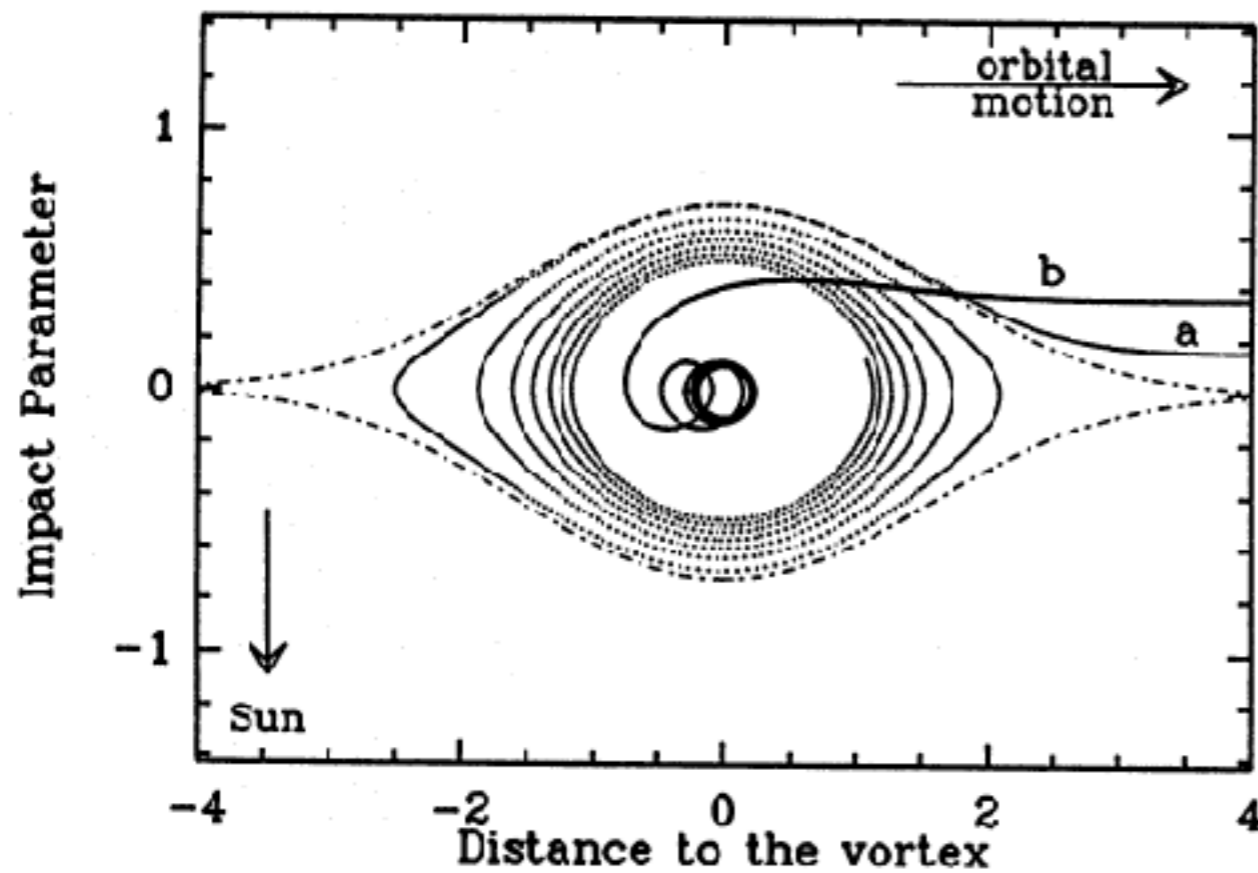
Lopsided structure: vortex



Casassus+ (2013)



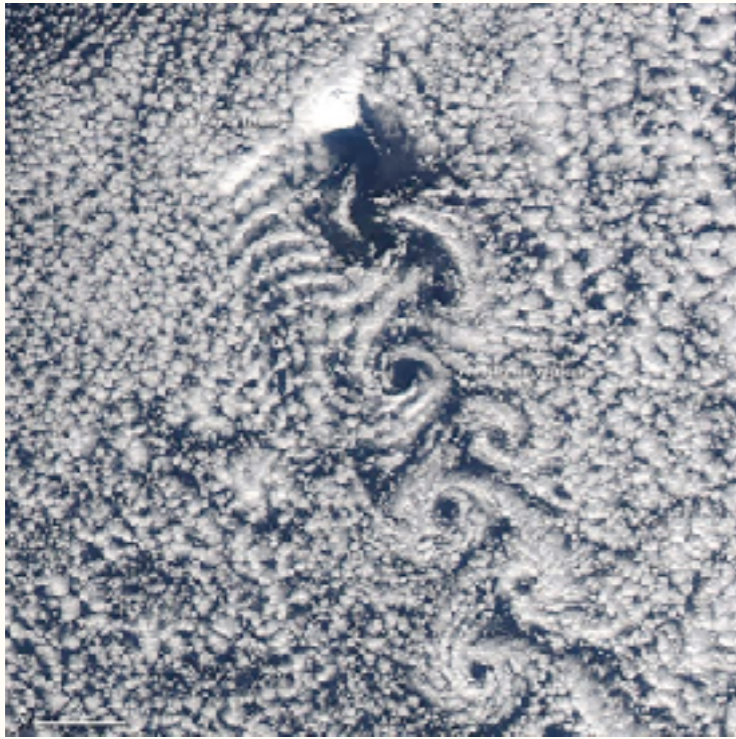
van der Marel+ (2013)



Barge & Sommeria (1995)

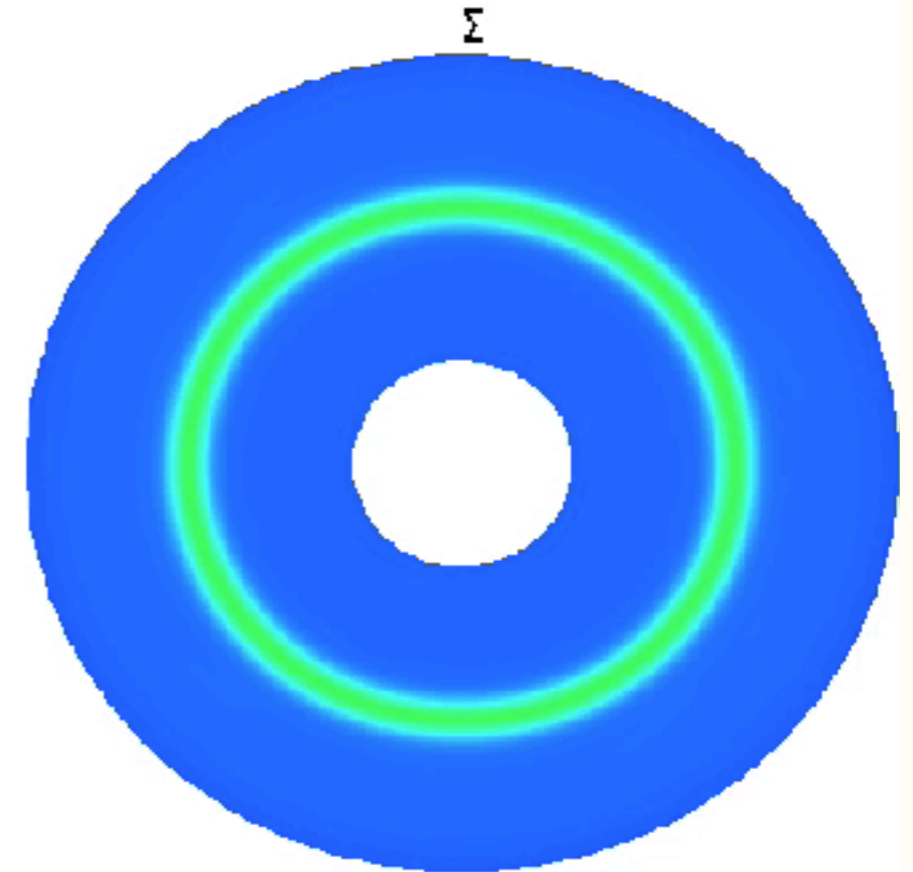
Vortex does not have to be associated with planets

- Vortices are natural outcomes of fluid instabilities.

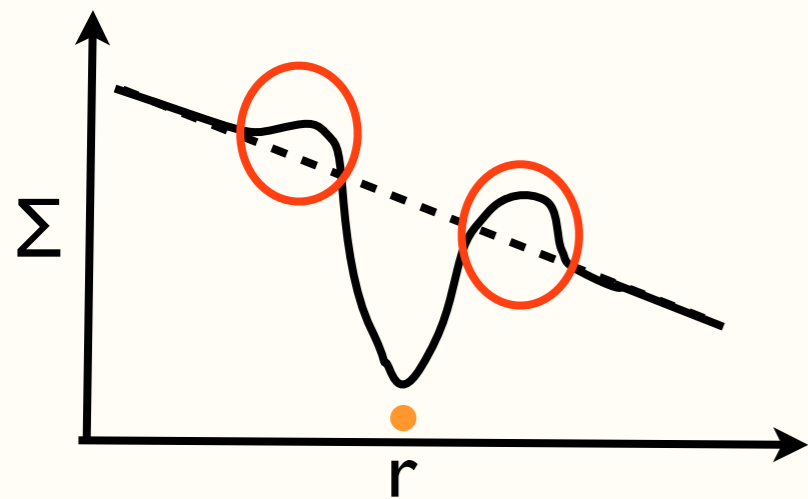


- In protoplanetary disks:
MRI, baroclinic instability,
Rossby wave instability

Papaloizou & Pringle 1984, 1985
Lovelace+ 1999, Li+ 2000, 2001
Meheut+ 2010, Yu & Lai 2013

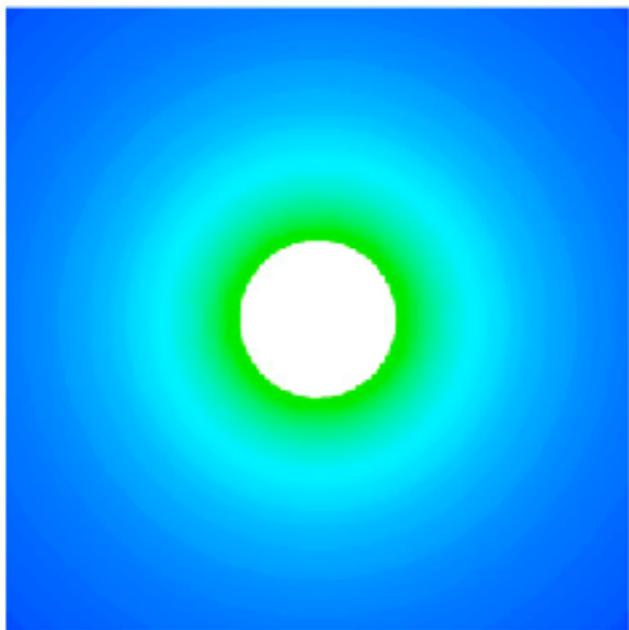


Planet-induced gap edge instability

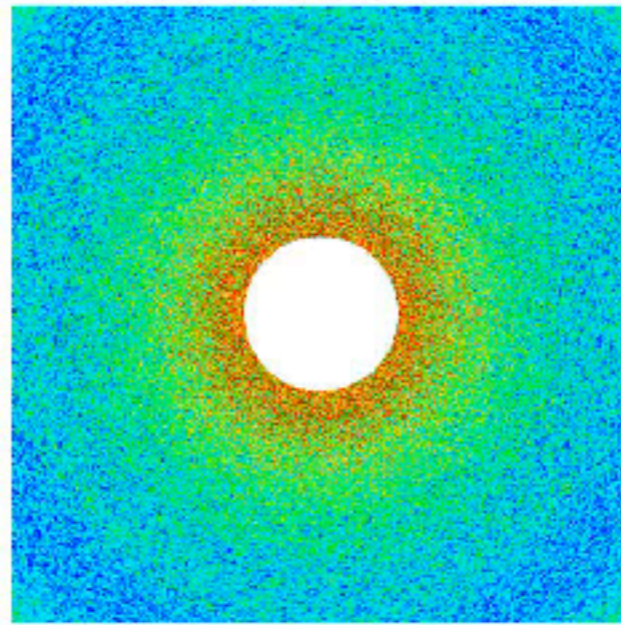


Papaloizou & Pringle 1984,1985 Lovelace et al. 1999, Li et al. 2000, 2001, Li et al. 2005, De Val-Borro 2007, Lyra et al. 2009, Meheut et al. 2010, Lin 2012, Altaie et al. 2013, Zhu et al. 2014, Fu et al. 2014, Surville et al. 2016, Regaly et al. 2012, 2017

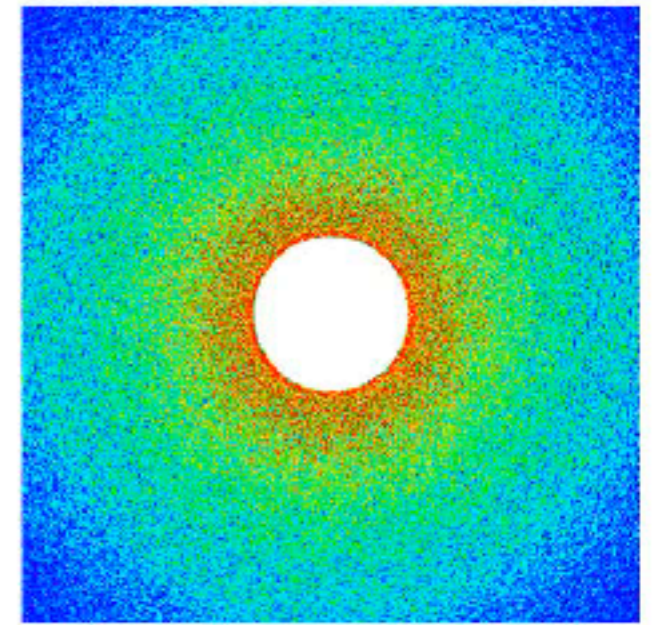
Gas



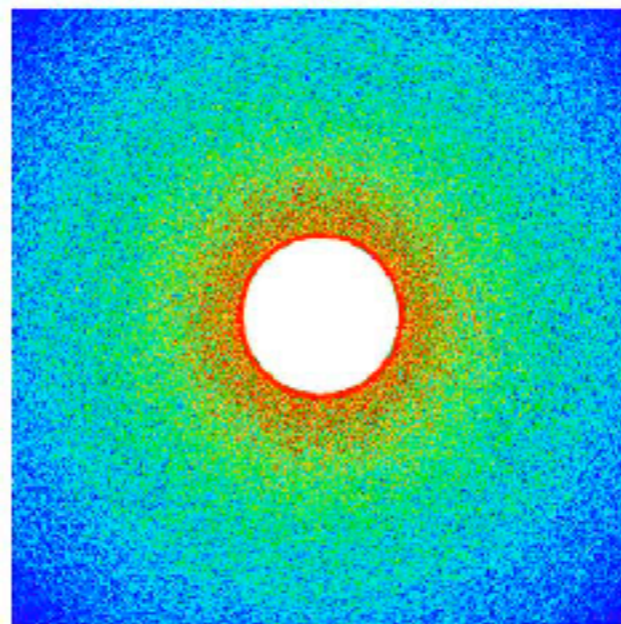
Dust particles



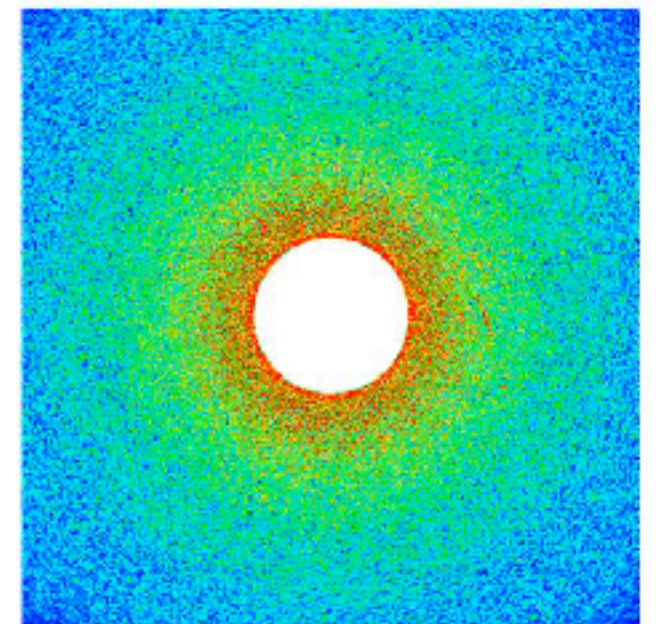
Par. a



Par. c



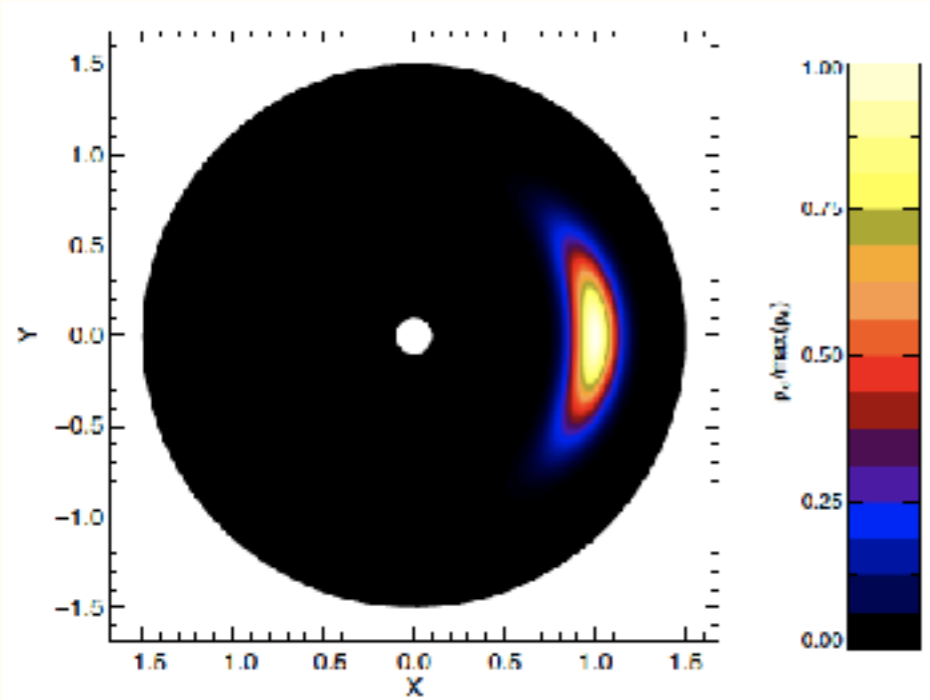
Par. d



Par. e

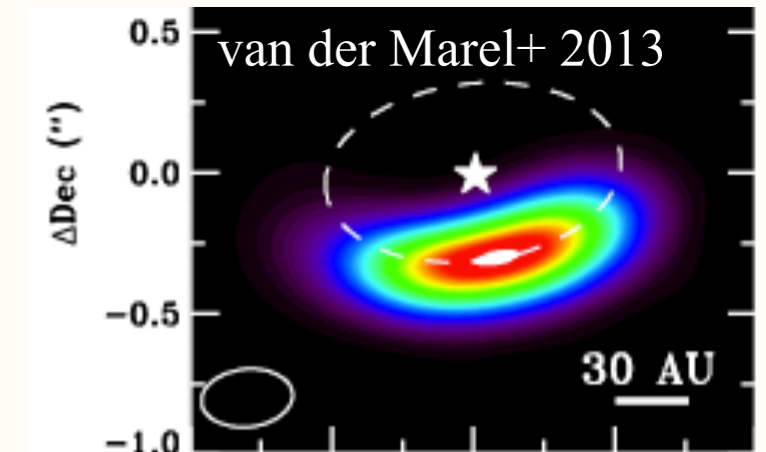
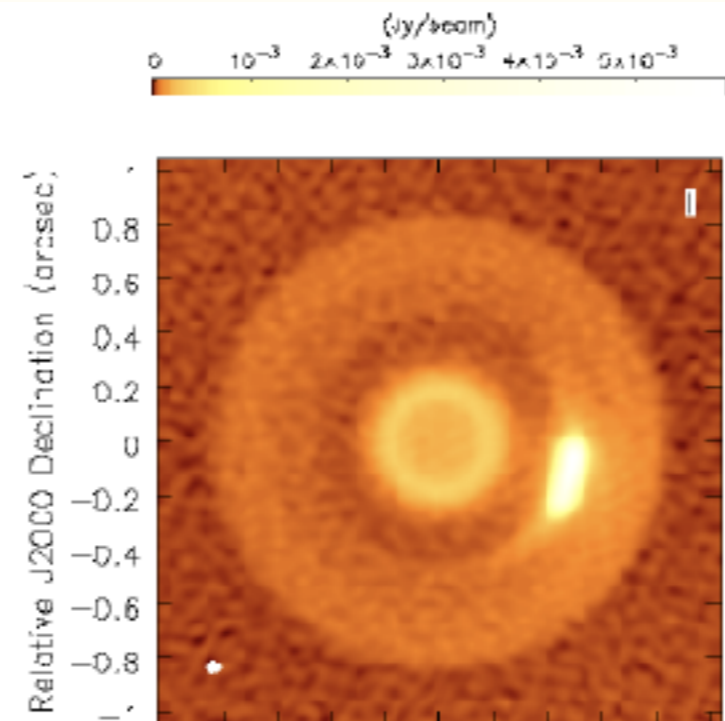
Compared with observations

Analytical Model

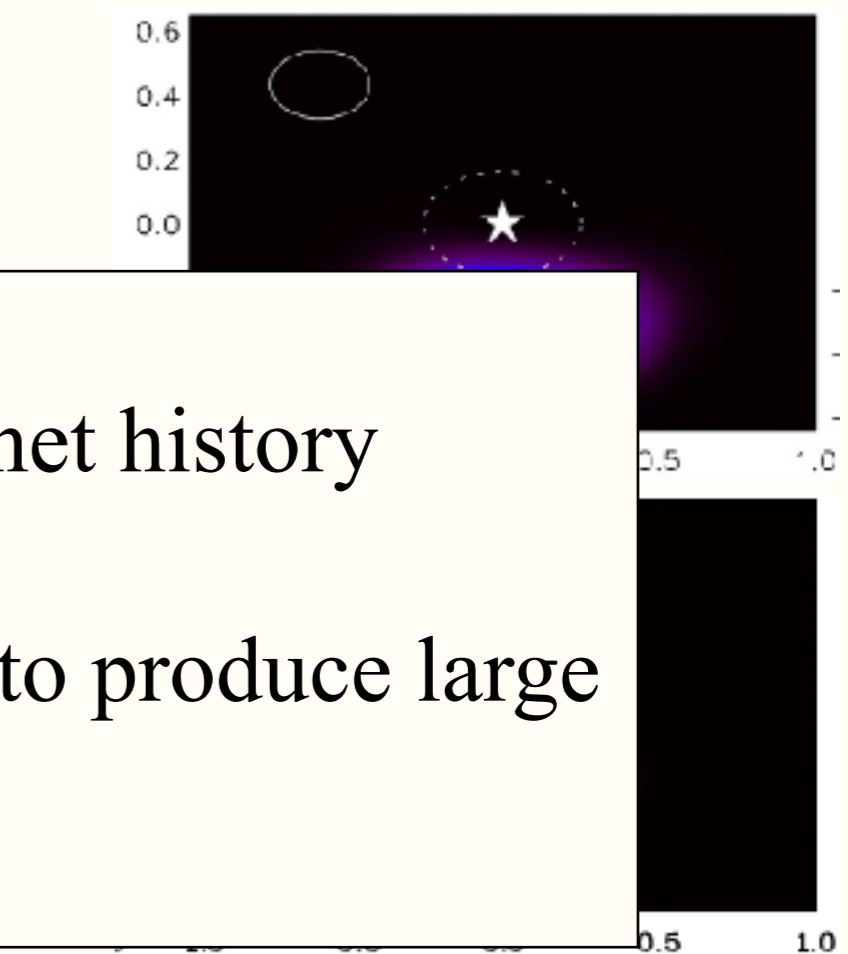


Lyra & Lin

Simulation+post processing



van der Marel+ 2013



- Too many disk parameters, planet history

(Hammer, Kratter, Lin 2018)

+ Vortex is the only known way to produce large scale disk asymmetry at submm.

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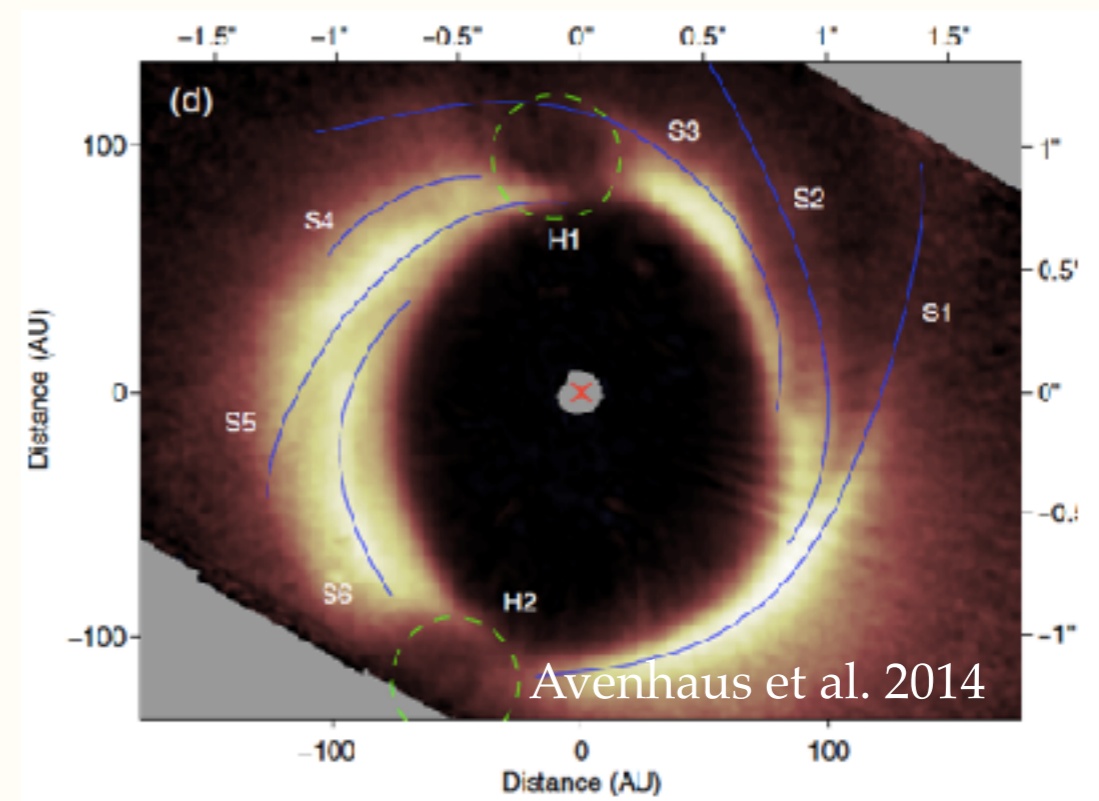
Gaps/rings

Spirals

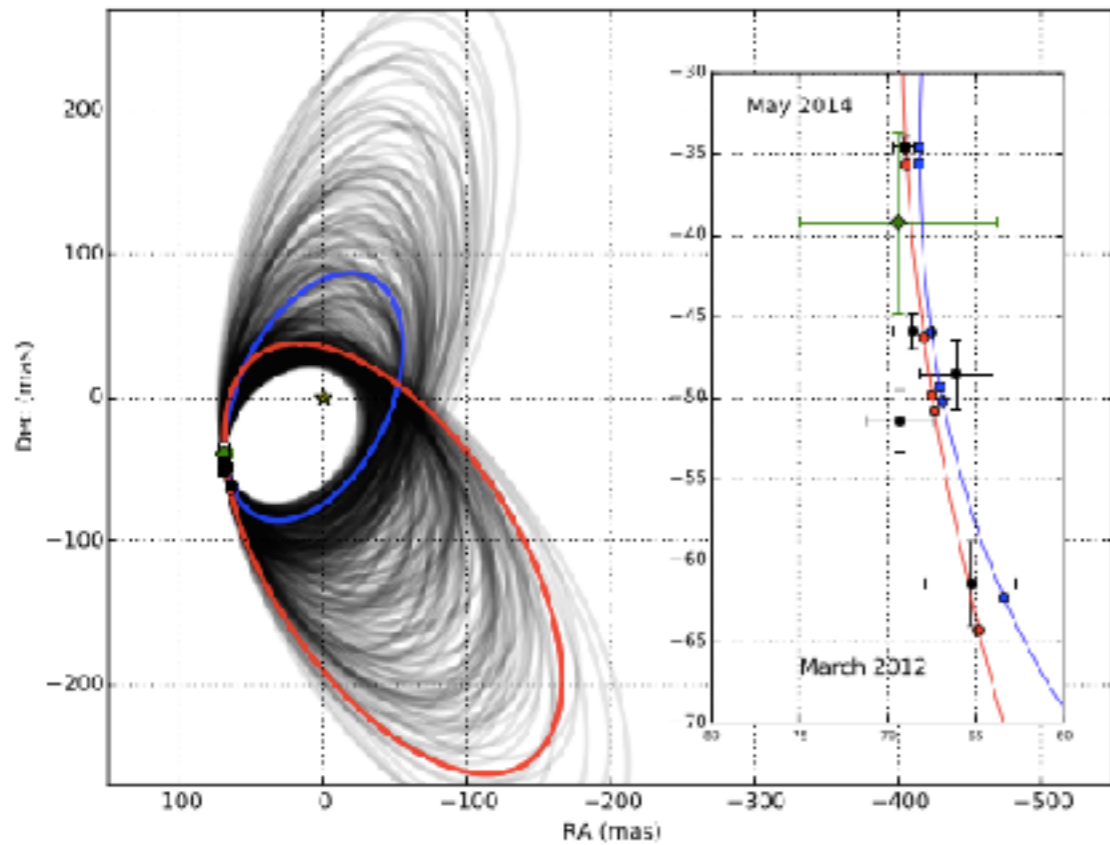
Lopsided structures

Shadows

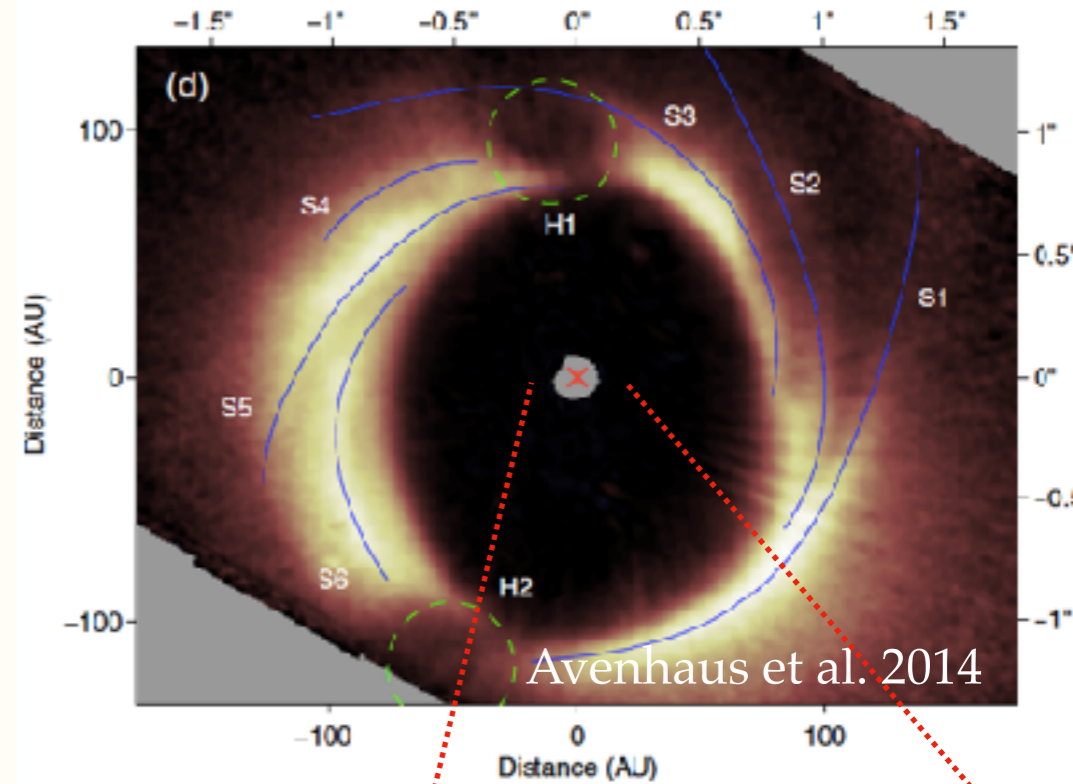
CPDs



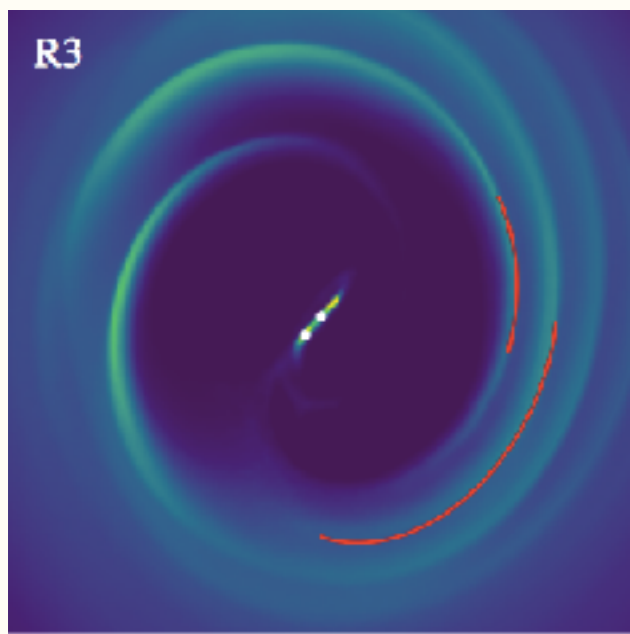
Inner/outer disk misalignment



Lacour et al. 2016

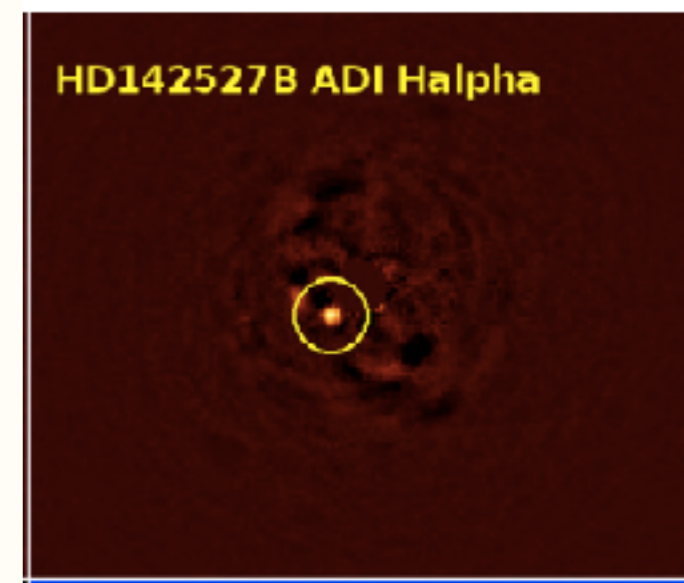


Avenhaus et al. 2014



- $0.2 M_{\odot}$ companion at ~ 12 au projected separation [Biller et al. 2012]
- ~ 40 - 50 au semi major axis, $e \sim 0.6$ - 0.7 , almost polar inclination [Price et al. 2018]

Price et al. 2018

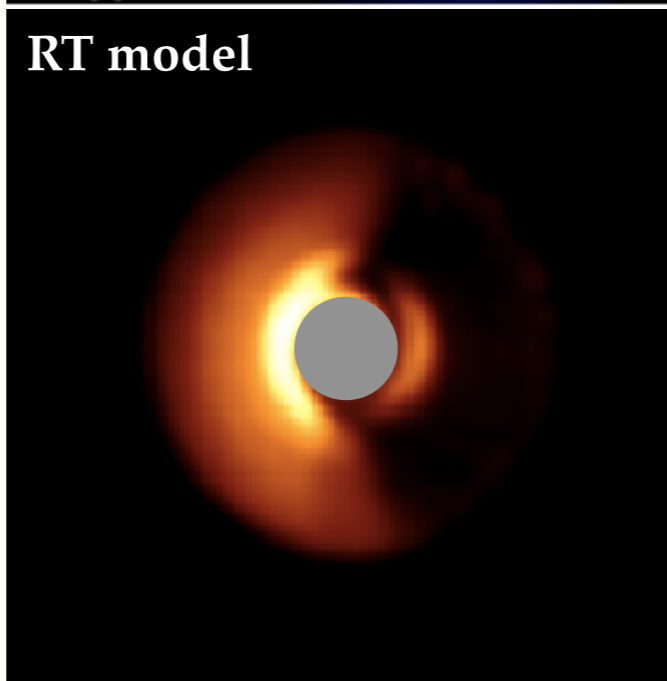
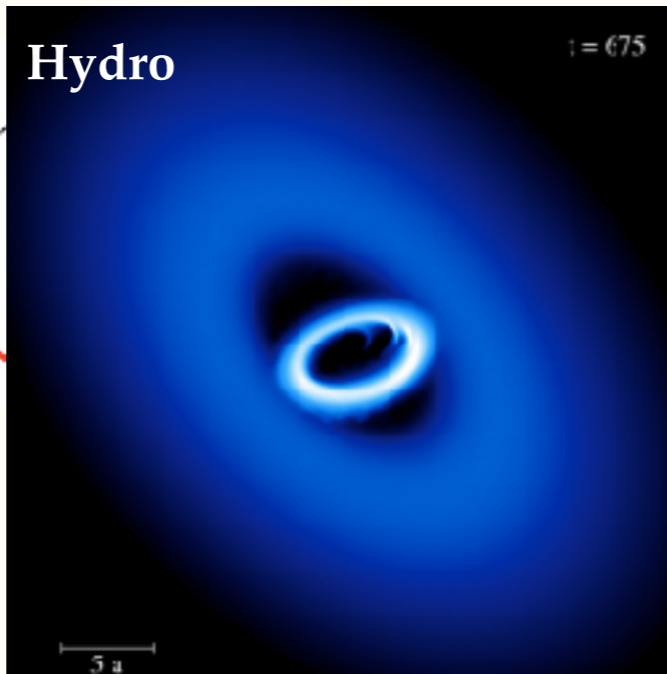
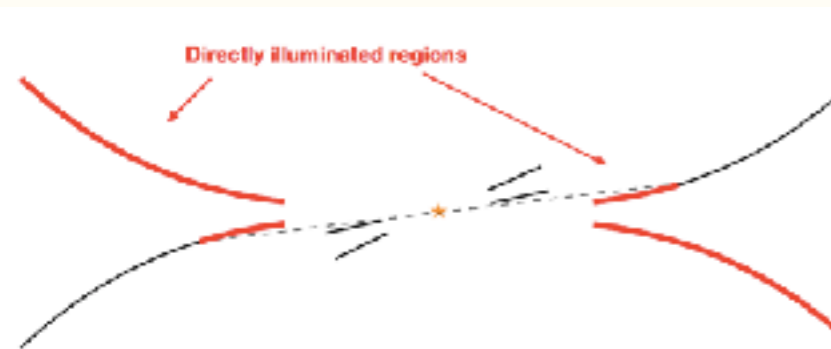


Close et al. 2014

Also Marino et al. 2015

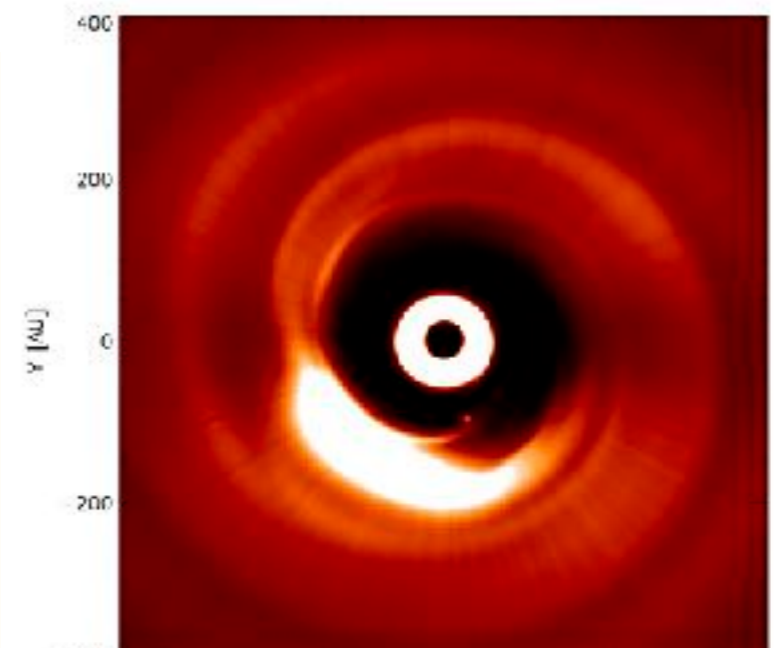
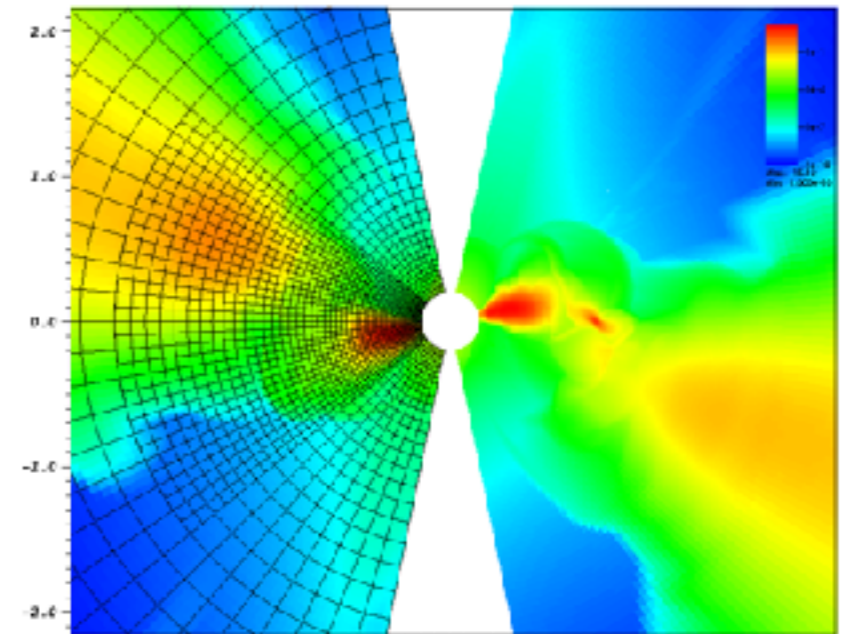
Inner/outer disk misalignment

Inclined binary torques the circumbinary disk



Facchini et al. 2018
Juhász & Facchini 2017

Inclined planet torques the circumstellar disk



Arzamasskiy, Zhu, Stone 2018
Zhu et al. In prep

- An equal mass binary, inclined by 60° , breaks the disk.
- A misalignment of ~ 30 deg (from VLTI, ALMA)

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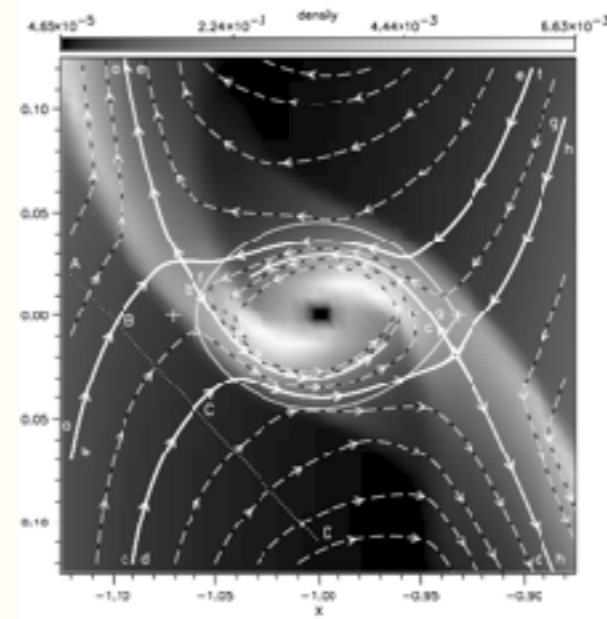
Gaps/rings

Spirals

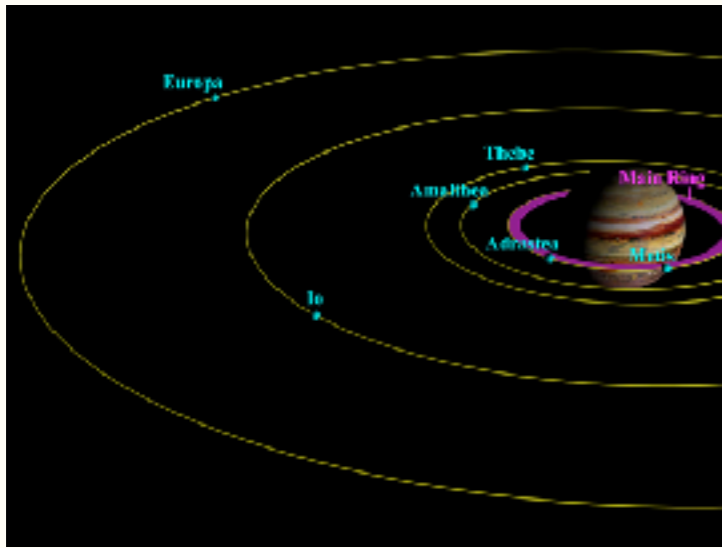
Lopsided structures

Shadows

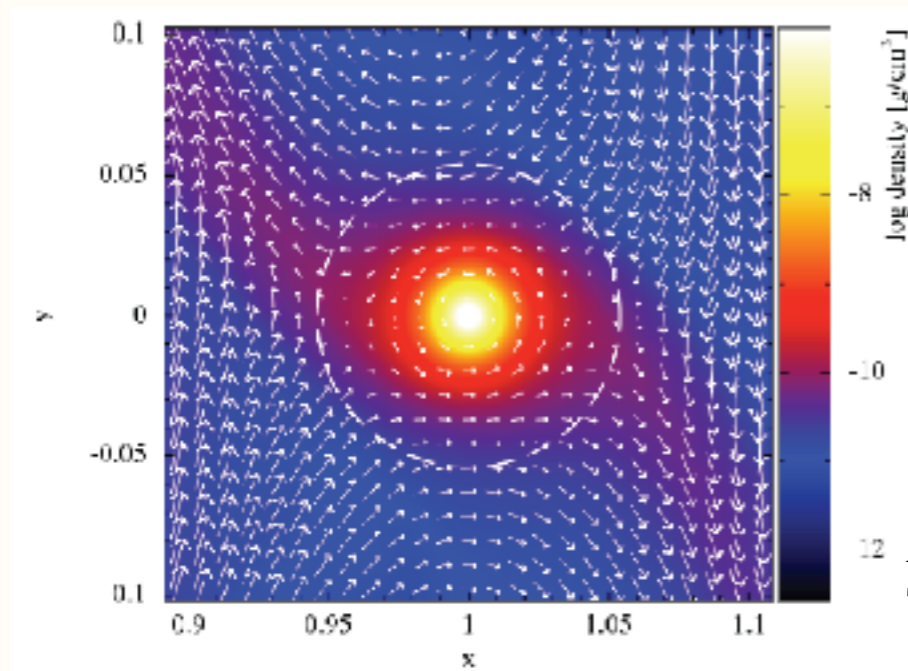
CPDs



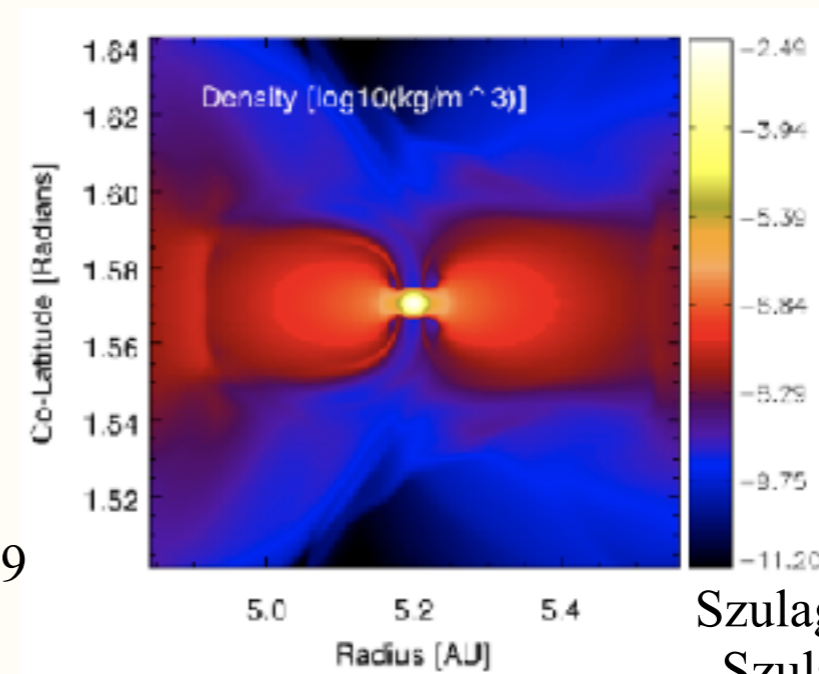
Circumplanetary Disks (CPD)



- Viscous model:



12 Ayliffe & Bate 2009
Tanigawa+ 2012



Szulagyi & Mordasini 2017,
Szulagyi et al. 2014, 2016

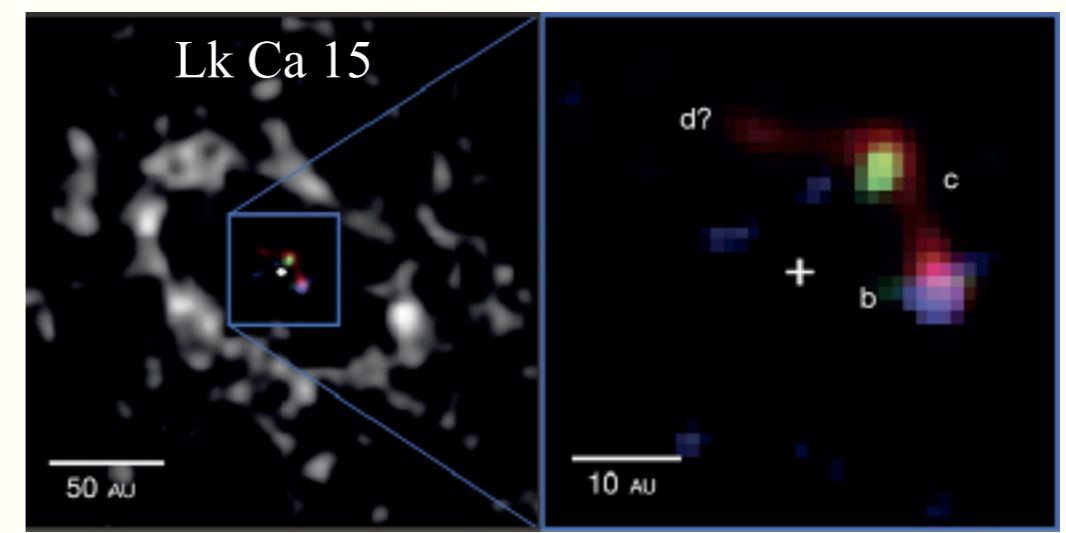
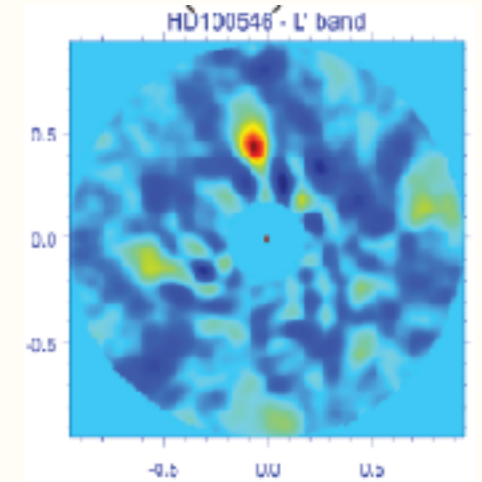
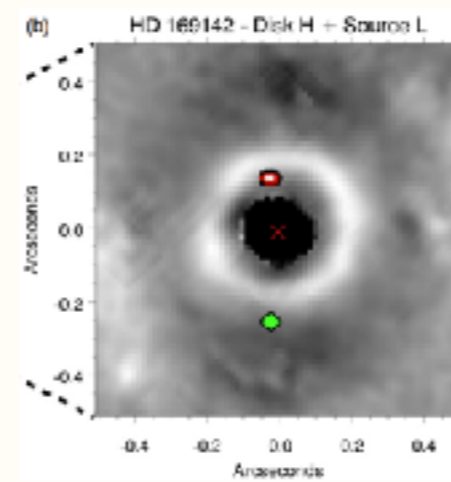
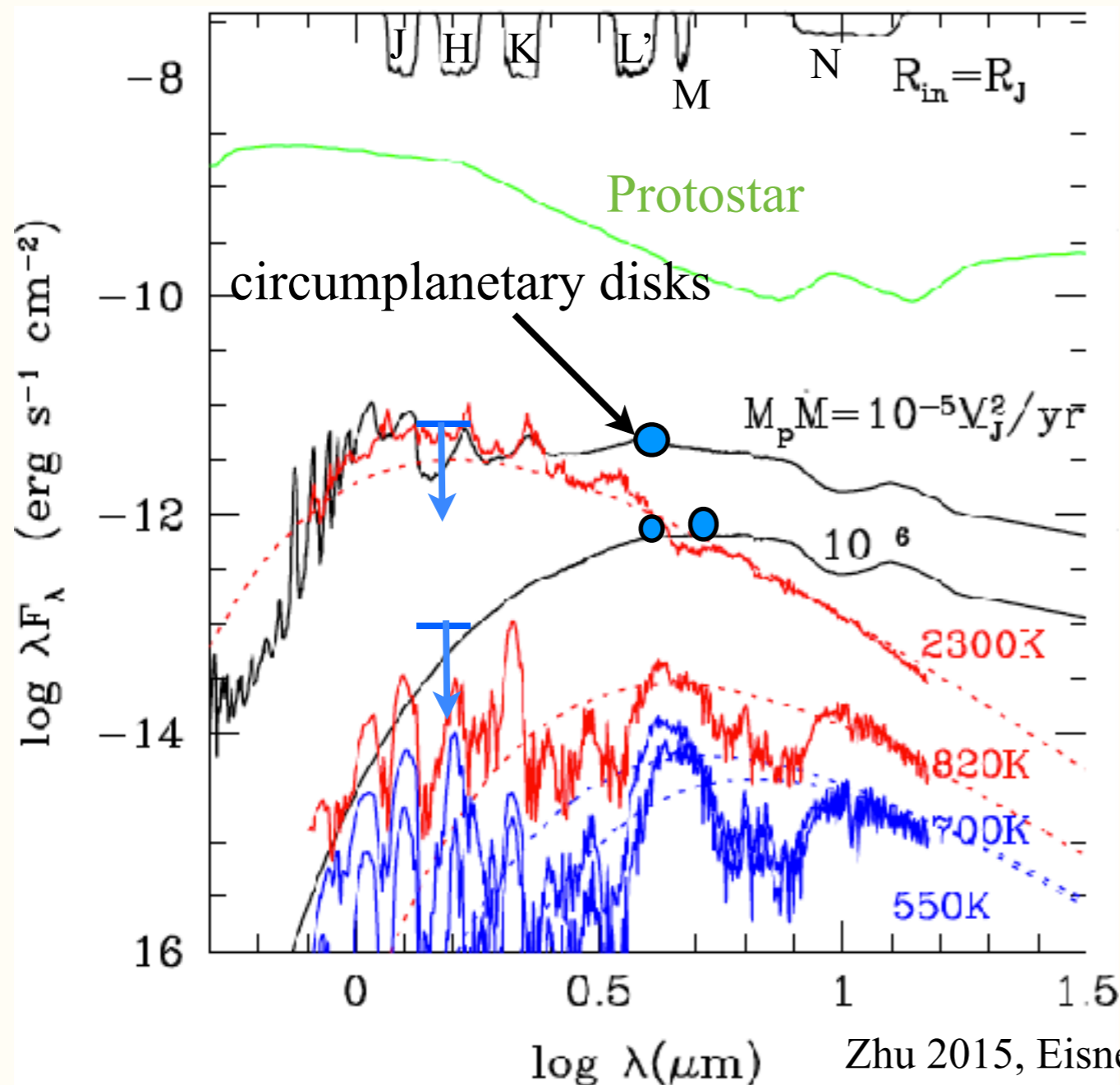
- Wind, non-ideal MHD: Turner et al. 2014, Fujii et al. 2014, Keith & Wardle 2015, Gressel et al. 2015
- Shock driven accretion: Zhu et al. 2016

CPD should be bright

If Jupiter is accreting at $\dot{M}=10^{-5} M_{\text{Jupiter}}/\text{yr}$

$$L_{\text{accretion}}=0.5 GM_{\text{Jupiter}}\dot{M}/R_{\text{Jupiter}}=1.5\times 10^{-3} L_{\text{sun}}$$

As bright as M type brown dwarfs!



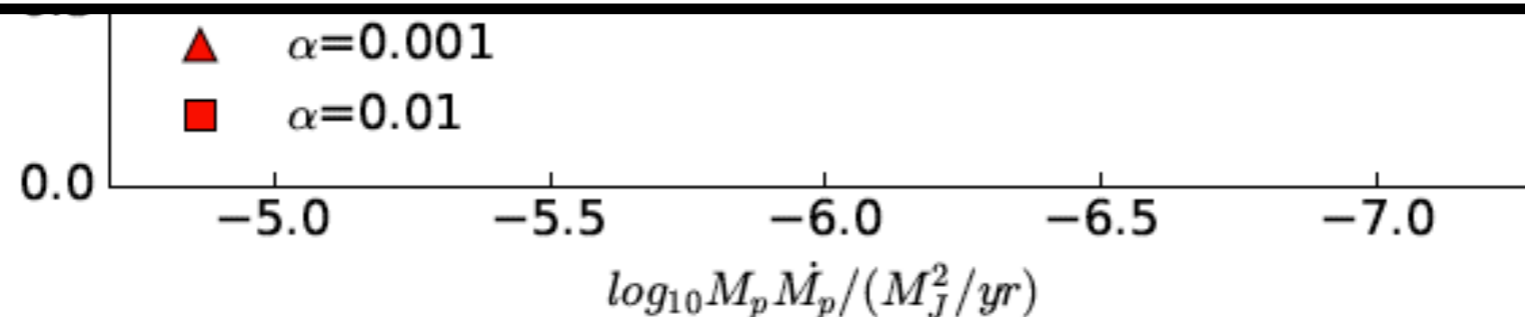
CPD should be bright at submm

Isella et al. 2014, Zhu, Andrews & Isella, 2018, Szulagyi et al 2018

submm flux from CPDs at 20 AU, assume dust-to-gas ratio 0.01

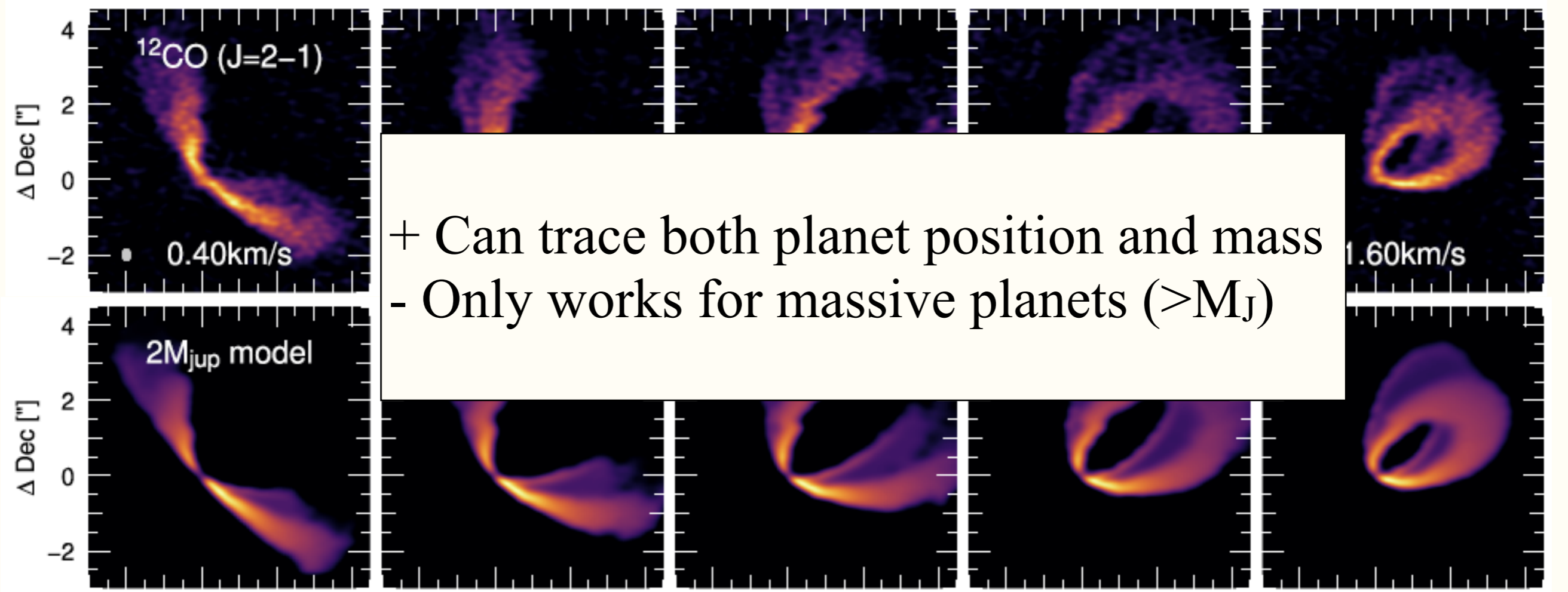
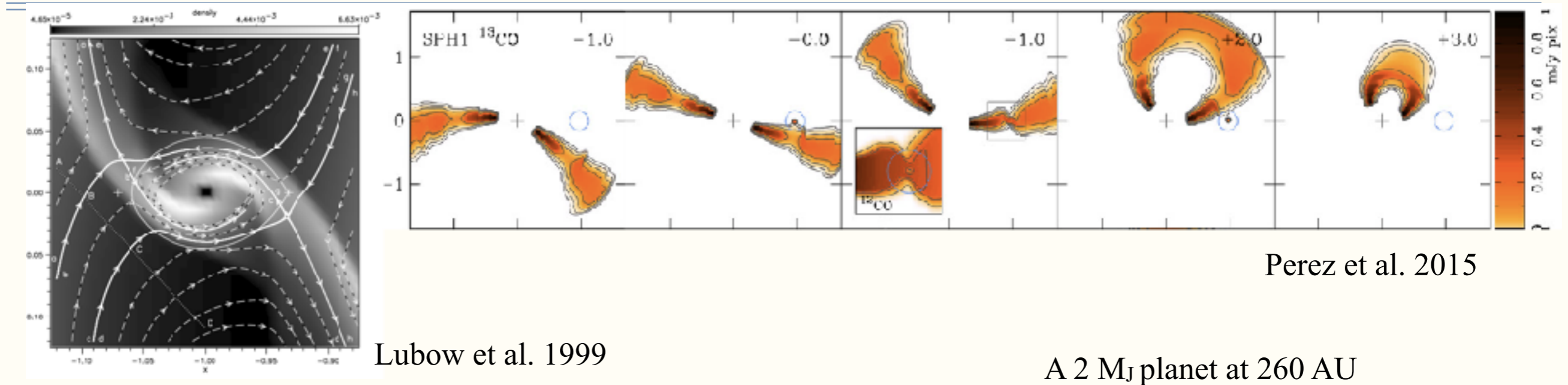


- CPDs should be bright at submm assuming dust-to-gas mass ratio of 0.01
- But if we consider dust radial drift, it may not be observable except under certain conditions
- Jet/Wind from CPD can be detected by ngVLA

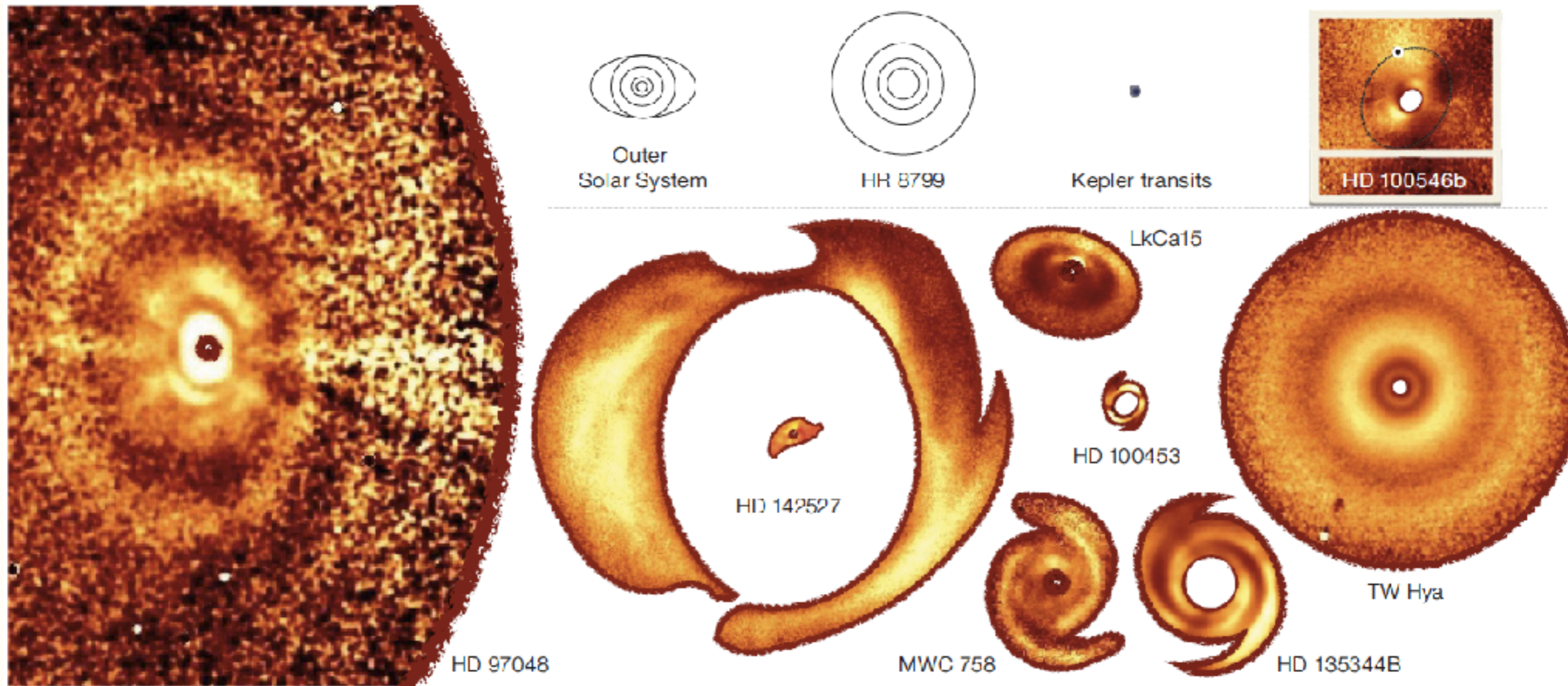


Zhu, Andrews & Isella, 2018

CPD kinematics



Overview: observations



Garufi et al. 2018

Overview: planet-disk interaction

$h/r=0.05$

$h/r=0.1$

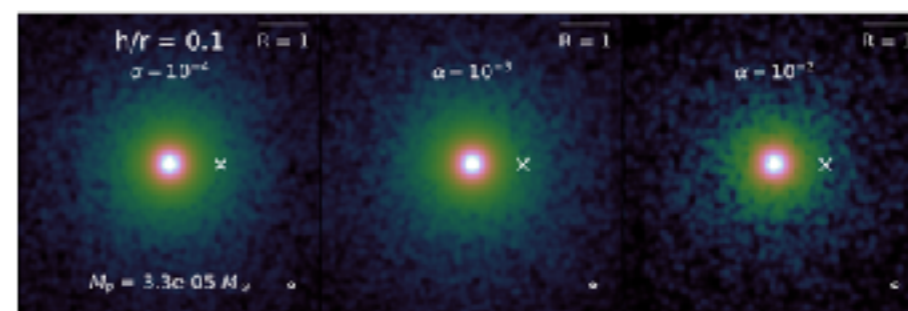
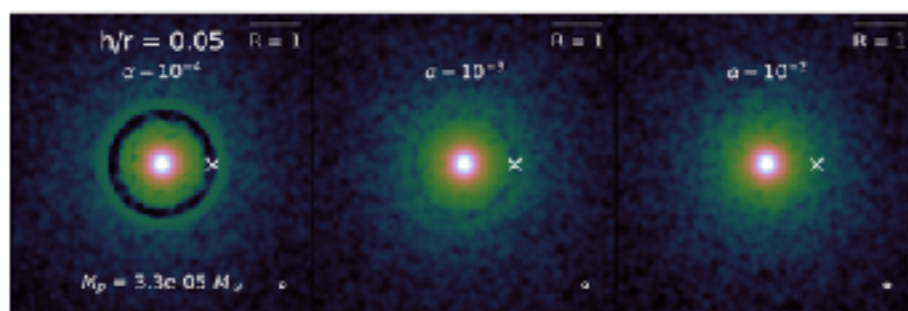
$\alpha=10^{-4}$

$\alpha=10^{-3}$

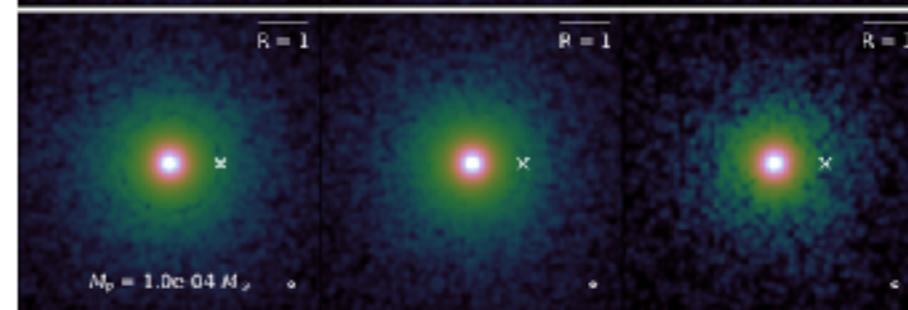
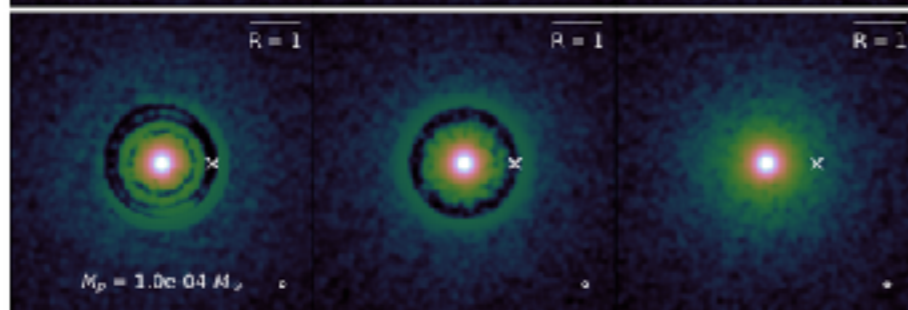
$\alpha=10^{-2}$

Zhang in prep.

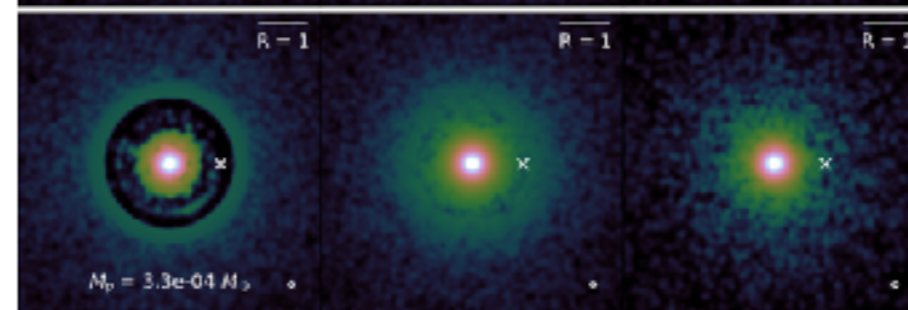
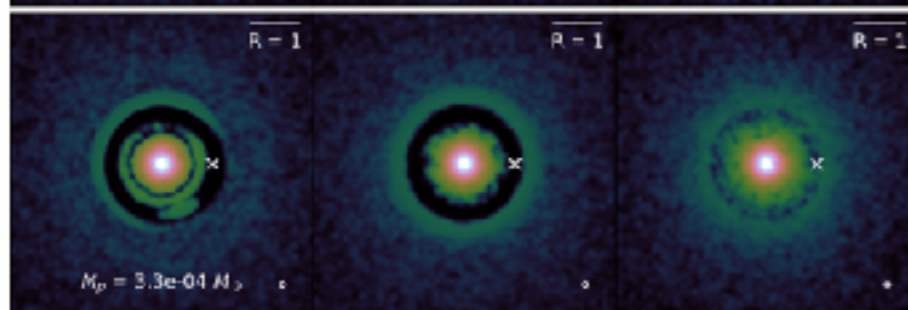
$M_p=10 M_\oplus$



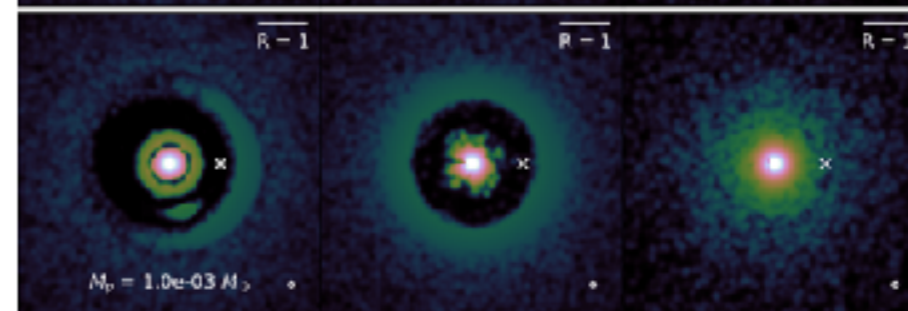
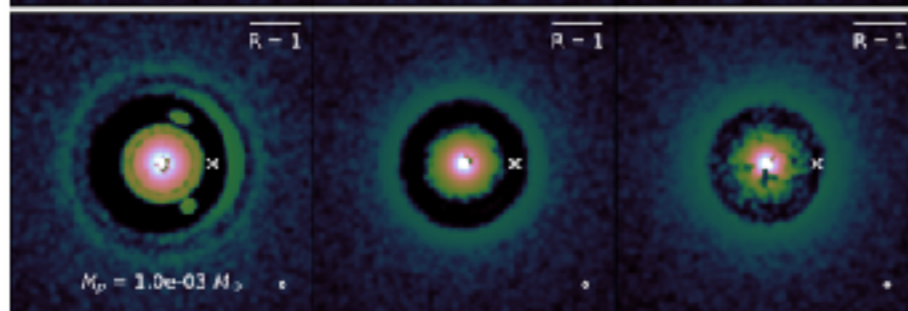
$M_p=30 M_\oplus$



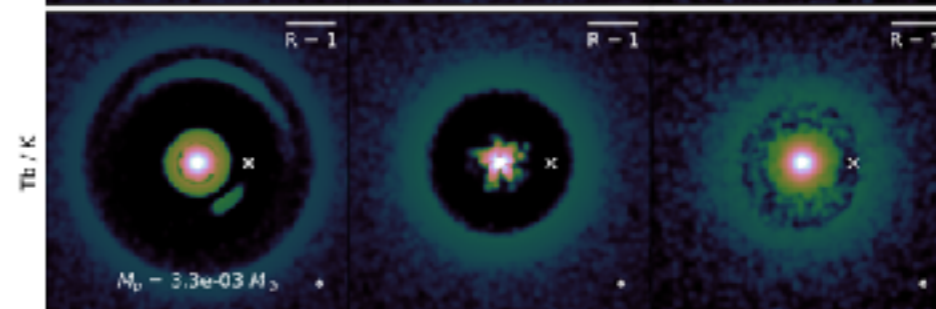
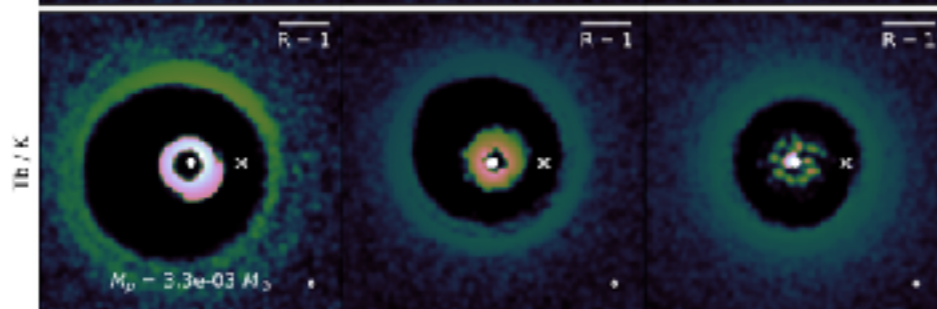
$M_p=100 M_\oplus$



$M_p=1 M_J$



$M_p=3 M_J$



Overview: indirect methods

Gaps/rings:

Depth/width at near-IR or submm

Deviation from Keplerian motion at the gap edge

Spirals:

Using spiral features (arm separation, contrast, opening angle)

Using pattern speed

Lopsided structures:

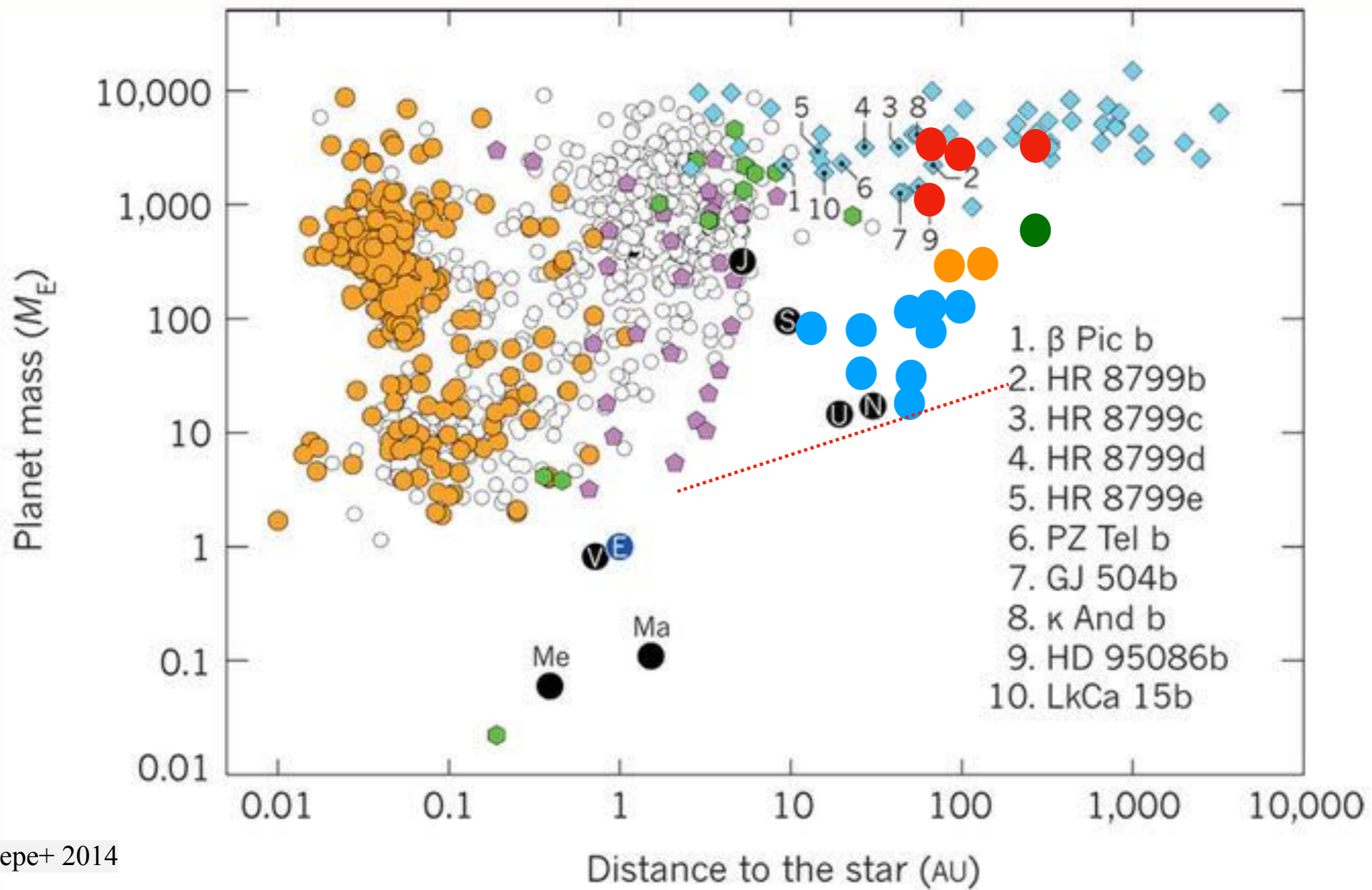
Vortex is the only known mechanism but may not be associated with planets

Shadows: misalignment

CPDs:

near-IR, $H\alpha$, submm

Kinematics

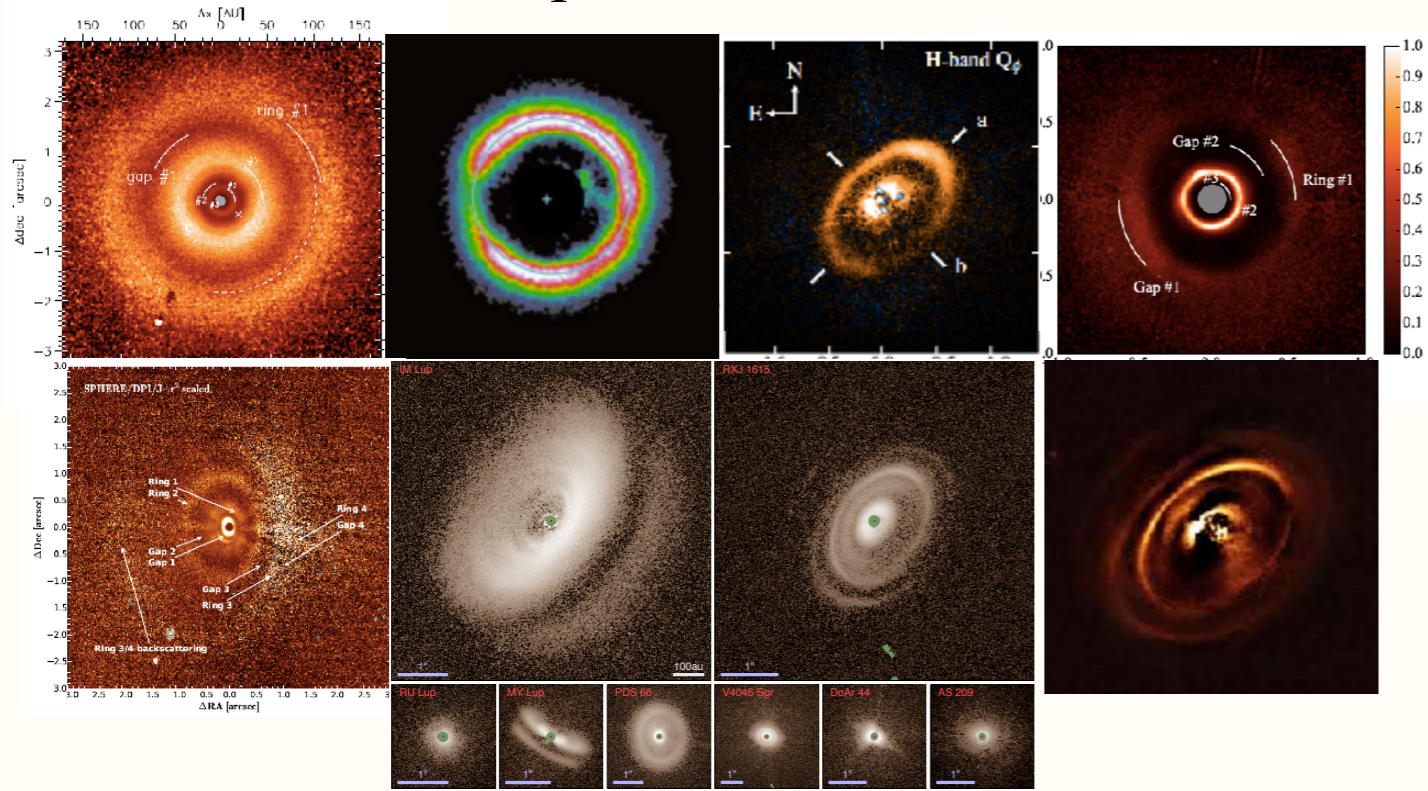


Pepe+ 2014

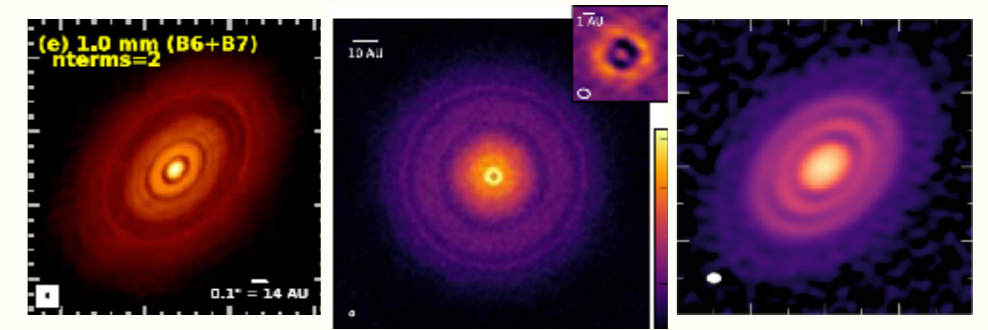
Dong+ 2015, Bae+ 2016, Isella+ 2016 Meru+ 2017, Dipierro+ 2018, Fedele+ 2018, Teague+ 2018, Pinte+ 2018

A lot more to come (ALMA large program PI: Sean Andrews)

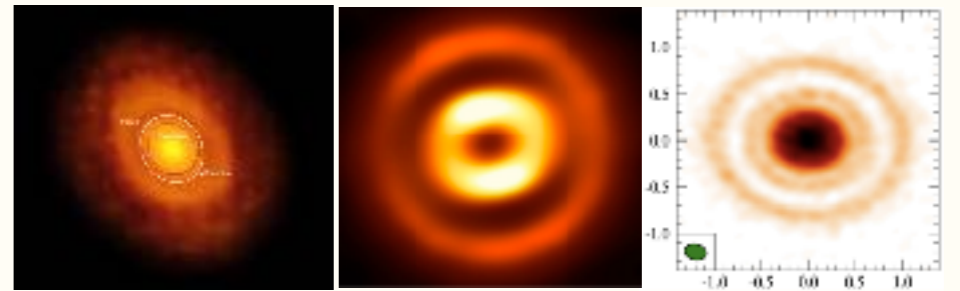
Optical/Near-IR



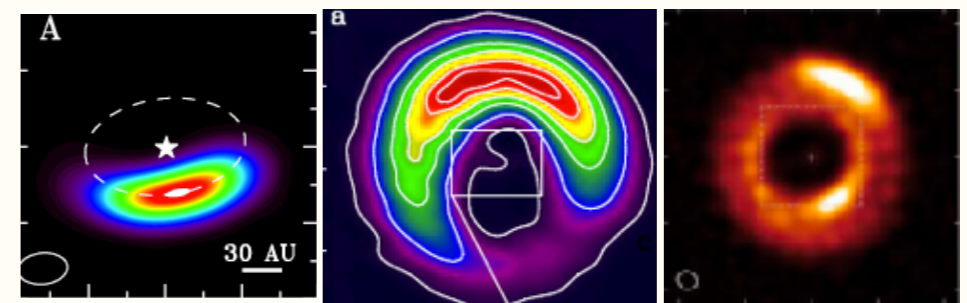
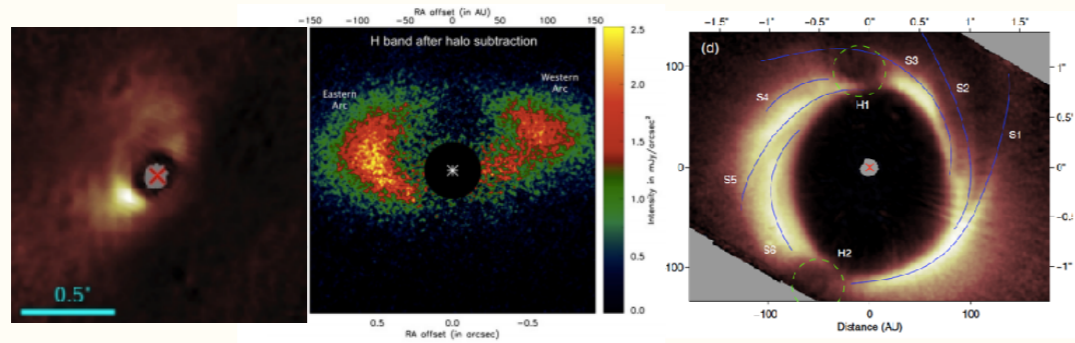
Radio



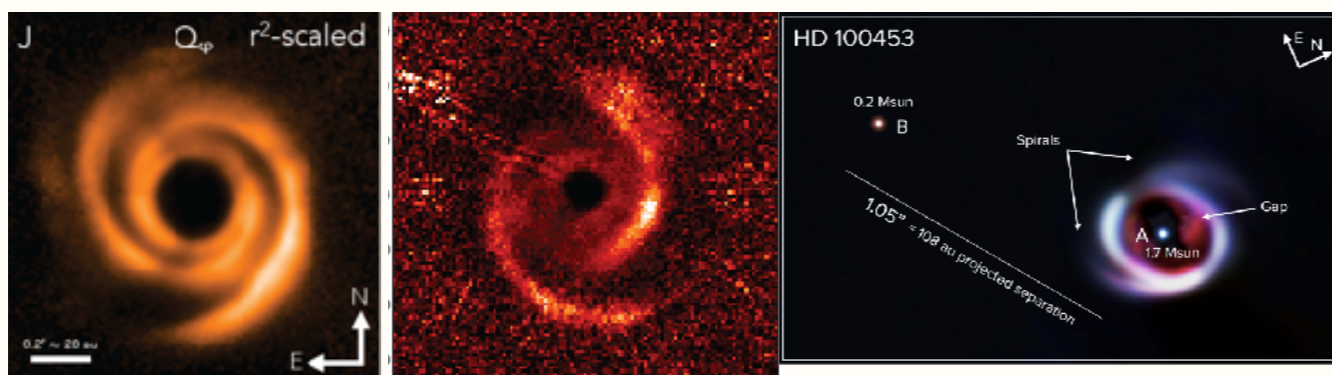
Fedele et al. 2017, 2018



Cieza et al. 2017



Boehler et al. 2017



Outline

- The traditional interests in planet-disk interaction

Migration

Gap opening

- New interests in planet-disk interaction

1. The imprints on the circumstellar disks

Spiral Wakes

Gaps/rings

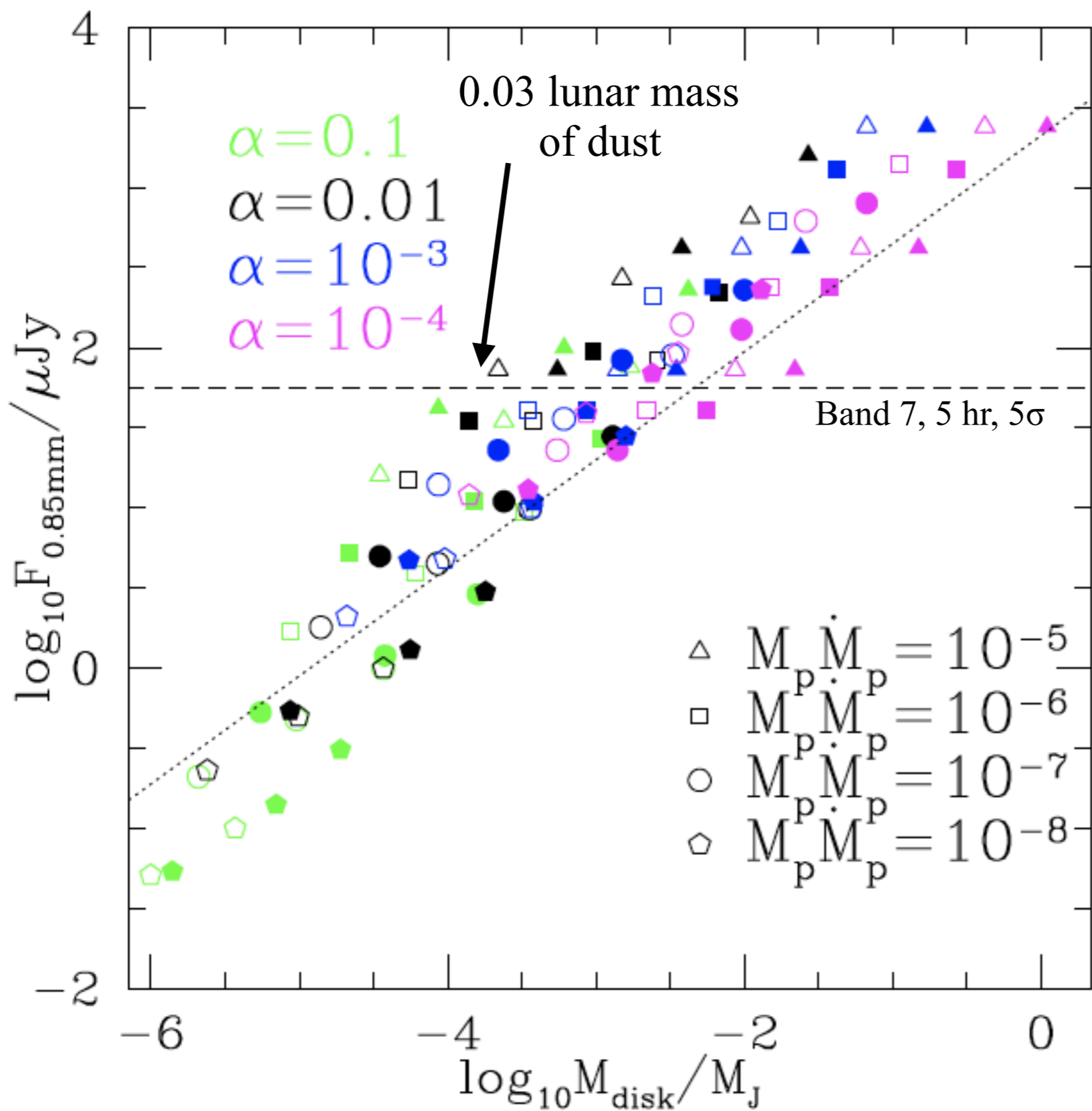
Vortices

2. Circumplanetary disks

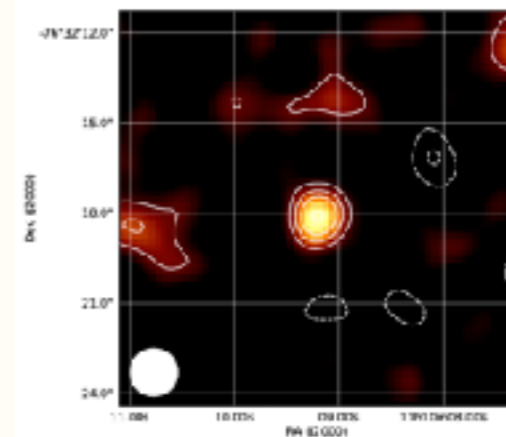
Summary

- Migration and gap opening depend on the disk property
- Planet-disk interaction can explain a lot of disk features (spirals, vortices, gaps/rings)
- Spirals to estimate planet mass/position
- Dust dynamics is the key for gaps/rings. Dust-to-gas feedback starts to be considered
- Vortices imply disk viscosity, mass, particle size
- CPD should be bright at near-IR to submm. We don't see many. Maybe radial drift, too compact ?
- **Where are the planets in protoplanetary disks ?**

Detection of dust emission in CPD by ALMA



OTS 44, 12 M_J

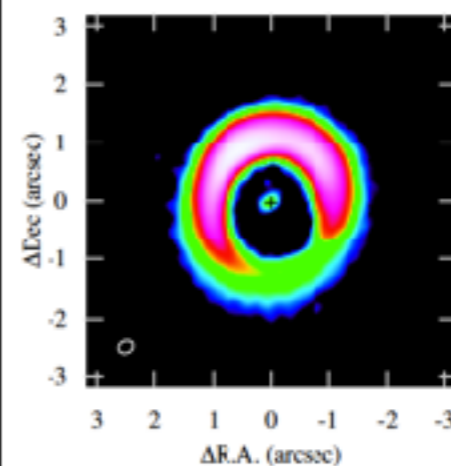


Bayo+ 2017

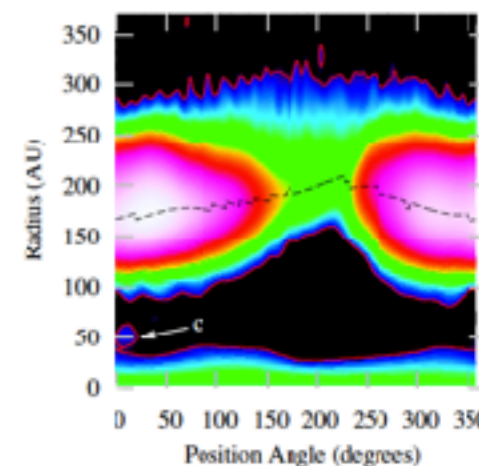
$\dot{M} \sim 10^{-7} M_J^2/\text{yr}$

$F = 100 \mu\text{Jy}$

HD 142527



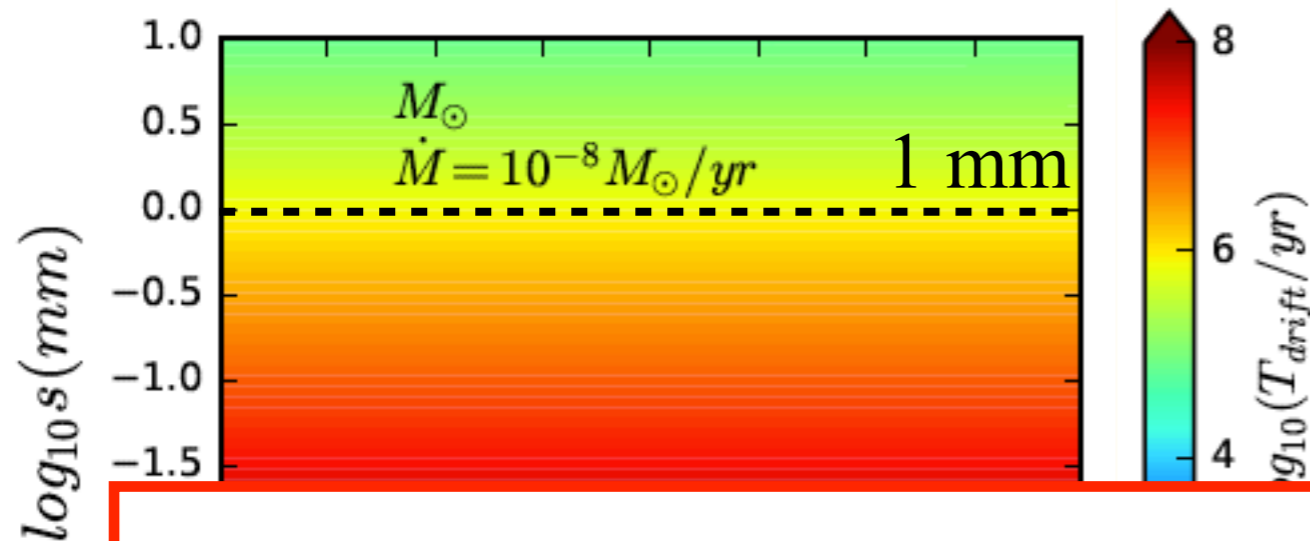
Boehler+ 2017



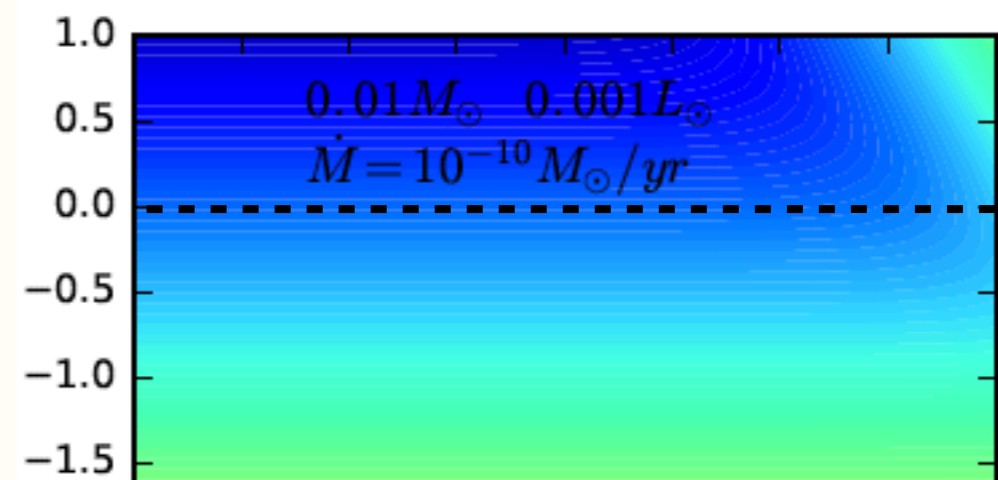
50 AU, 0.8 mJy

Dust drifts very fast in CPDs

Dust drift timescale in circumstellar disks



Dust drift timescale in CPDs



- CPDs should be bright at submm assuming dust-to-gas mass ratio of 0.01
- But if we consider dust radial drift, it may not be observable except under certain conditions
- Jet/Wind from CPD can be detected by ngVLA

b

In order to be detected at mm:

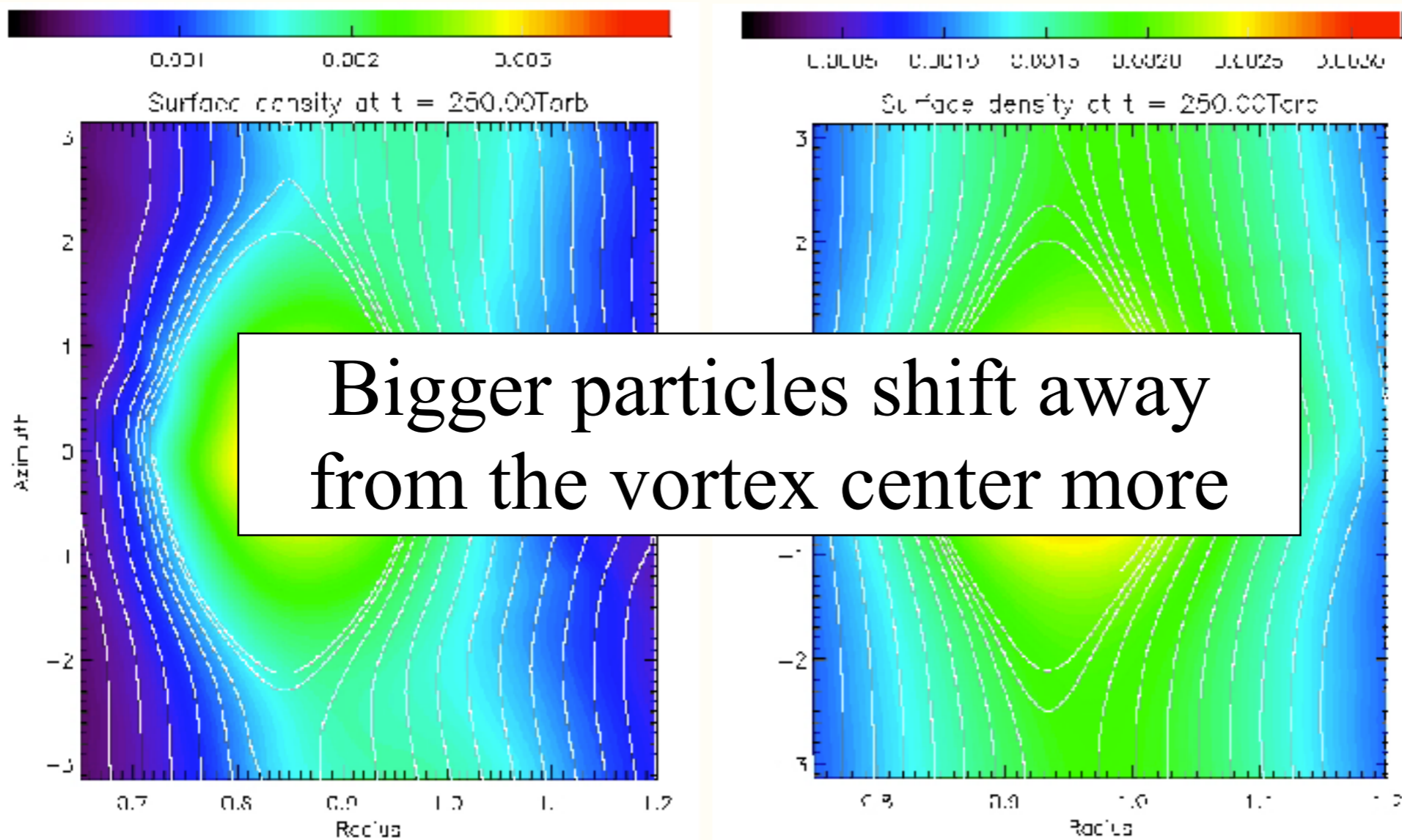
- 1) dust are micron sized
- 2) high gas surface density
- 3) substructures in CPD (HL Tau in HL Tau)

Vortex: gravity from gas to dust

No gravity from gas to dust

With gravity from gas to dust

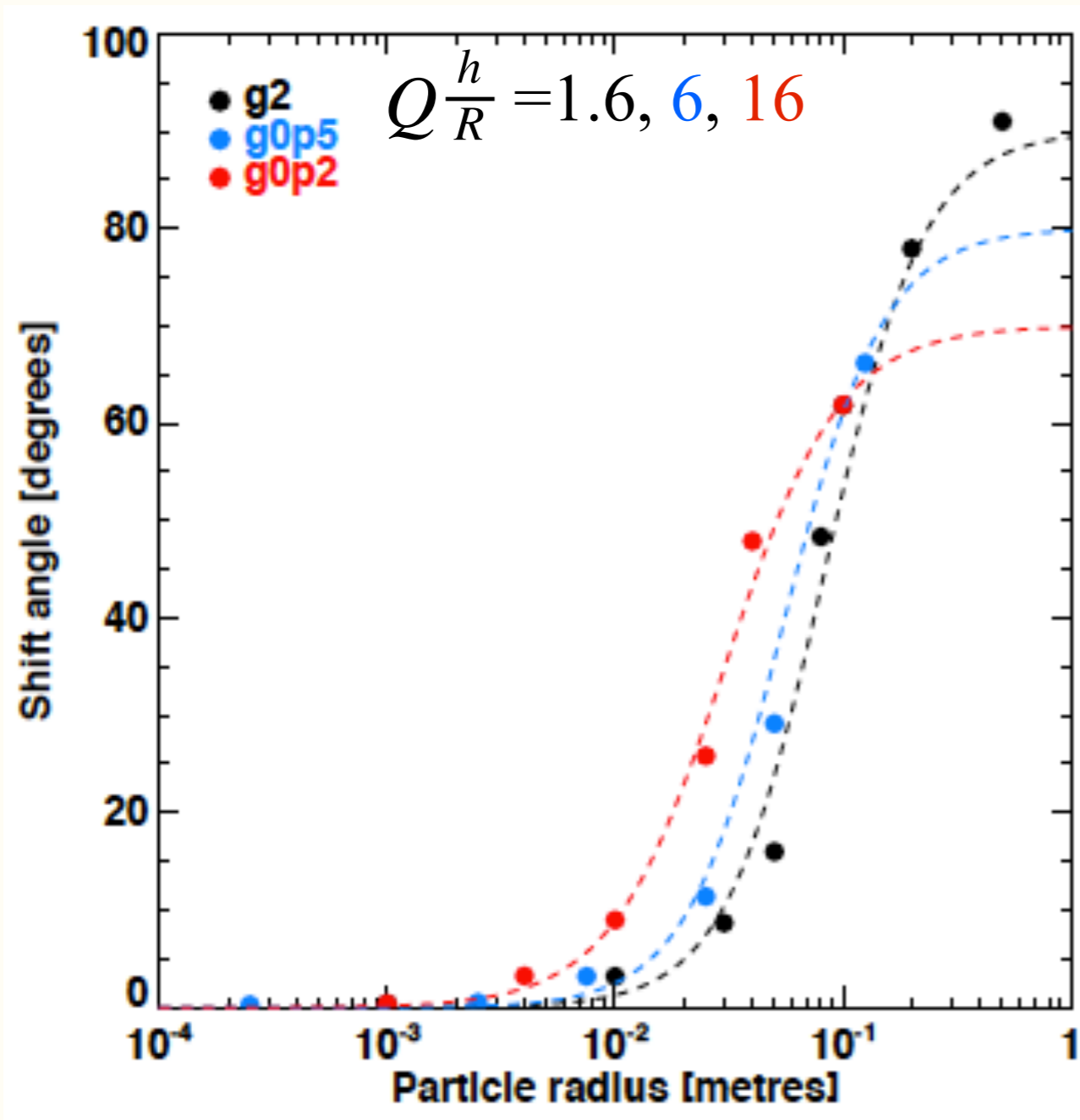
$Q=13$



Baruteau & Zhu 2015

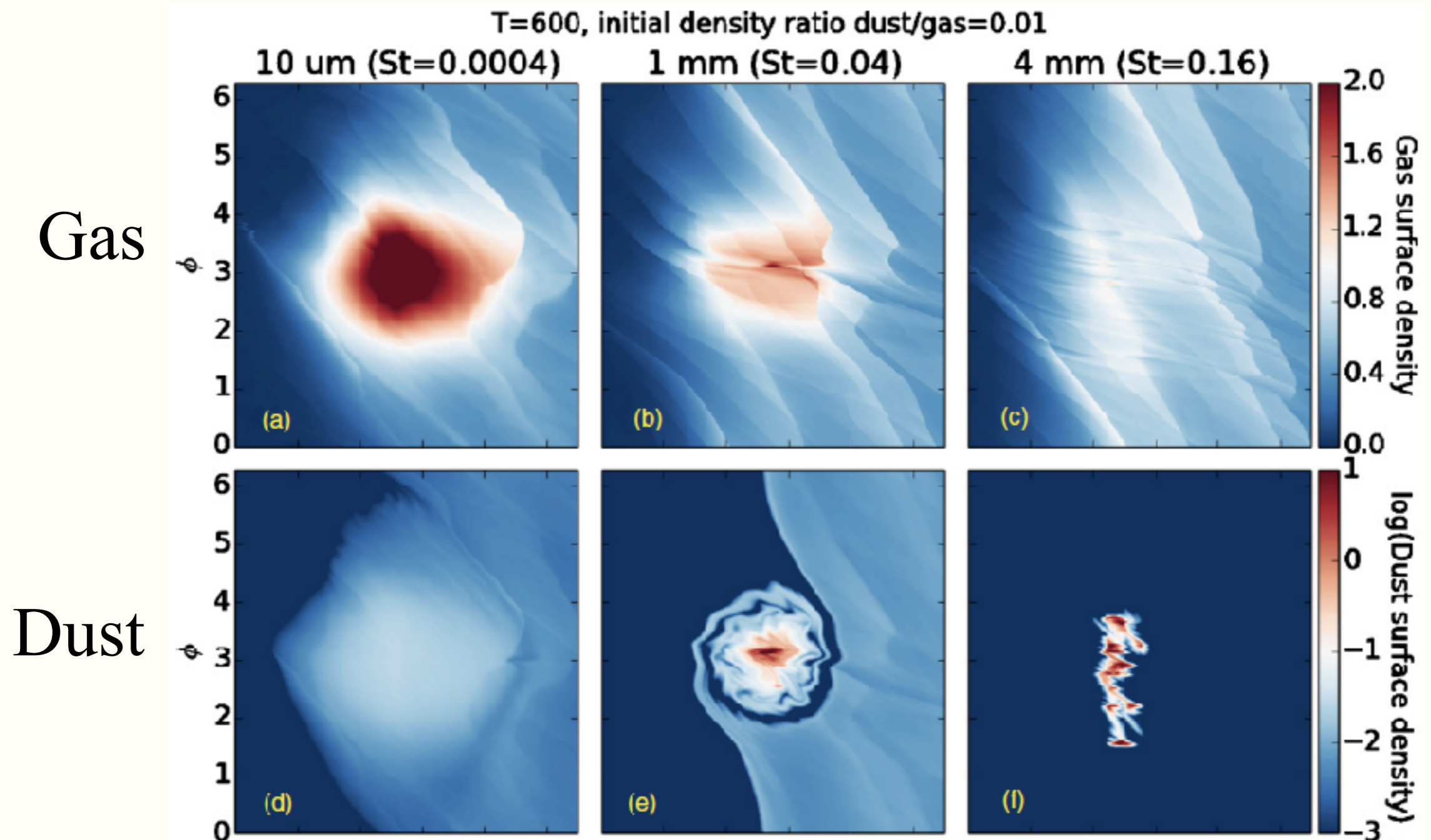
Applications

Planetesimal Formation



Baruteau & Zhu (2015)

Vortex: including dust-to-gas feedback



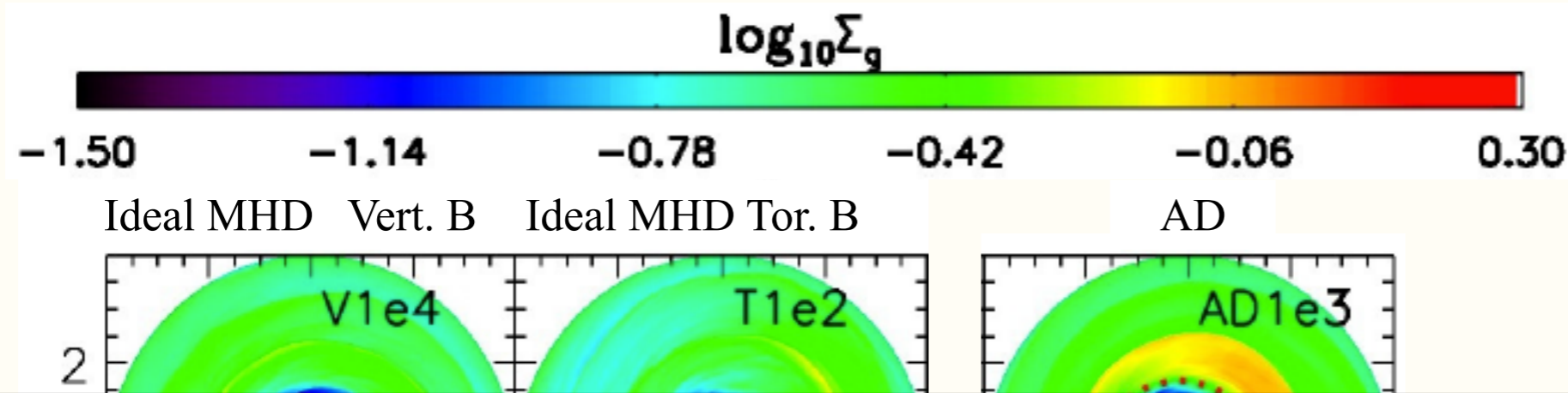
Fu et al. 2014

Crnkovic-Rubsamen et al. 2014

- Locally, dust can have higher density than gas
- signs of instability (Lesur & Papaloizou 2009, Chang & Oishi 2010, Raiton & Papaloizou 2014)

Ring or vortex ?

- If a gap edge is optically thick, a vortex will not show up
- For a shallow gaseous gap edge, it is more likely to be a ring !
- If you have turbulence/viscosity, it forms a ring !



The vortex only appears when turbulence/viscosity is weak!

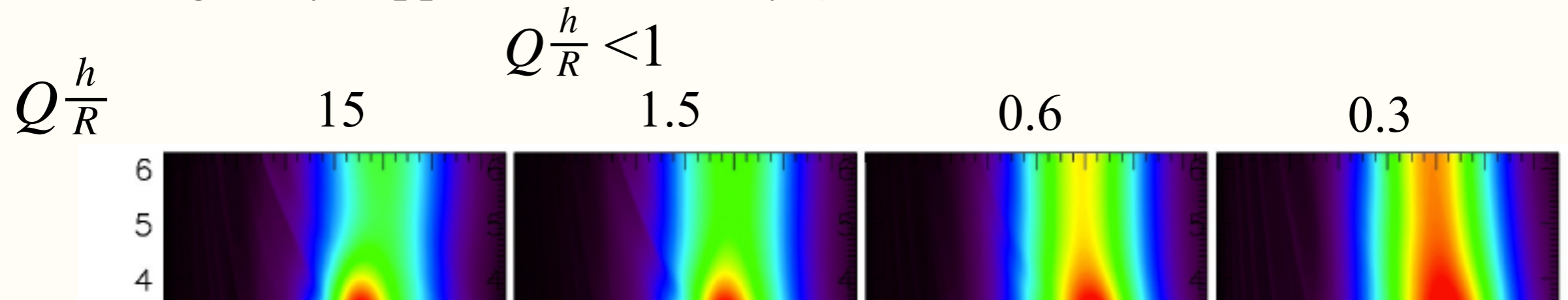
Turbulence is strong
 $\alpha \sim 0.01$

Turbulence
is weak
 $\alpha \sim 0.001$

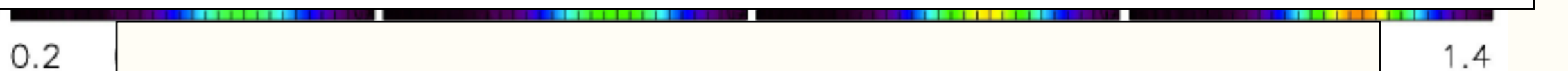
Zhu & Stone 2014
Fu et al. 2014
Hammer et al. 2017

Ring or vortex ?

- Gas self-gravity suppresses instability (Lin et al. 2011, Lovelace & Hohlfeld 2013)



The vortex only appears when disk self-gravity is weak!



- Too many disk parameters, planet history (Liang 2015)

(Hammer, Kratter, Lin 2018)

+ Vortex is the only known way to produce large scale disk asymmetry at submm.



van der Meer 2015

$Q \sim 4000$

$Q \sim 1$